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BY

G. A. WENTWORTH, A.M.,
PROFESSOR OF MATHEMATICS IN PHILLIPS EXETER ACADEMY.

FOR HIGH SCHOOLS AND ACADEMIES.

TEACHERS' EDITION.

BOSTON, U.S.A.:
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### PREFACE.

THIS edition is intended for teachers, and for them only. The publishers will make every effort to keep the book from pupils; and teachers are urged to exercise the utmost care not to lose their copies, or to leave them where pupils can have access to them.

It is hoped that young teachers will derive great advantage from studying the systematic arrangement of the arithmetical work, for such attention has been paid to this as the limitation of the page would allow.

It is also expected that many teachers, who are pressed for time, will find great relief by not being obliged to work out every problem in the Arithmetic.

G. A. WENTWORTH.

PHILLIPS EXETER ACADEMY, August, 1888.

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## ARITHMETIC.

45. Find the following sums: 231 + 764; 341 + 57.8; 430.31 + 58.61; 512.87 + 36.84 + 12.78 + 711.56 + 415.86.

			512.87
			36.84
			12.78
231	341.	430.31	711.56
764	57.8	58.61	415.86
995	398.8	488.92	1689.91

46. Add 1543.1 to 164.7; to 1728; to 402.56; to 1897.3; to 475.34; to 6897.65.

164.7	1728.	402.56	1897.3	<b>475.34</b>	6897.65
1543.1	1543.1	1543.1	1543.1	1543.1	1543.1
1707.8	3271.1	1945.66	3440.4	2018.44	8440.75

47. Add 1897.3 to 475.34; to 6897.65; to 1728; to 402.56; to 164.7; to .5236; to 2.71828.

<b>475.34</b>	<b>6</b> 80 <b>7.65</b>	1728.	402.56	164.7
1897.3	1897.3	1897.3	1897.3	1897.3
2372.64	8794.95	3625.3	2299.86	2062.

0.5236	2.71828	
1897.3	1897.3	
1897.8236	1900.01828	

**48.** Find the following sums: .7854 + 3.1416 + 2.71828; .7854 + 3.1416 + 30,103; 2.71828 + 402.56 + 1897.3; 2.7113 + 27.53 + 341.586.

0.7854	0.7854	2.71828	2.7113
3.1416	3.1416	402.56	<b>2</b> 7.53
<b>2.71828</b>	<b>30</b> ,103.	1897.3	341.586
6.64528	30,106.937	2284.57828	371.8273

49. Add 737.87 to each of the following numbers: 111; 1011; 2304; 222; 263; 373; 262.13; 561.2; 32.35; 604.3.

111.	1011.	2304.	222.	<b>263</b> .
737.87	737.87	737.87	737.87	737.87
848.87	1748.87	3041.87	959.87	1000.87
373.	262.13	<b>561.2</b>	32.35	604.3
737.87	737.87	737.87	737.87	737.87
1110.87	1000.	1299.07	770.22	1342.17

**50.** Find the five sums: 230.8 + 223 + 2.63 + 373.8 + 56.123; 32.358 + 821.9 + 23.04 + 73.7; 202.3031 + 71.575 + 65.813 + .0078 + 7.377; 653.03 + 65.303 + 6.5033; 939.303 + 65.746 + 8.2794 + 681.28.

230.8		202.3031		
223.	32.358	71.575		939.303
2.63	821.9	65.813	653.03	65.746
373.8	23.04	0.0078	65.303	8.2794
56.123	73.7	7.377	6.5033	681.28
886.353	950.998	347.0759	724.8363	1694.6084
<b>52.</b>	2.7182818	0.4342945	3.2808693	ı
•	3.1415927	4.8104774	2.5399772	
,	0.7853982	2.5399772	4.8104774	
	6.6452727	7.7847491	10.6313239	
	1.6093295	0.3047973	0.3937043	•
	15.4323487	0.3010300	0.3819660	•
	3.785	0.6213768	0.4342945	
	20.8266782	1.2272041	1.2099648	
<b>53</b> .	0.3010300	0.6180340	0.3819660	, ,
1	0.6180340	2.2360680	1.7320508	
	0.3819660	1.7320508	1.4142136	
	1.30103	4.5861528	3.5282304	. •
<b>.</b>	2.2360680	15.4323487	3.785	•
•	1.4142136	0.8450980	0.6213768	
•	15.4323487	0.264	1.6093295	
	19.0826303	16.5414467	6.0157063	

	0.6213768	1.6093295	0.3047973
	3.2808693	3.2808693	0.3937043
	0.3047973	0.3937043	2.5399772
	4.2070434	5.2839031	3.2384788
	0.3937043	0.3047973	2.7182818
	3.2808693	0.4342945	3.1415927
	4.8104774	0.5235988	0.5235988
	8.485051	1.2626906	6.3834733
<b>54</b> .	2.7182818	3.1415927	0.7853982
	3.1415927	0.5235988	0.4342945
	0.7853982	4.8104774	4.8104774
	0.5235988	2.5399772	0.3937043
	0.4342945	0.3937043	0.3047973
	7.603166	11.4093504	6.7286717
	0.3937043	1.6093295	1.6093295
	3.2808693	0.3047973	0.6213768
	1.6093295	0.3937043	3.785
	0.4342945	0.5235988	0.264
	4.8104774	0.4342945	15.4323487
	10.528675	3.2657244	21.712055
	0.6213768	3.785	15.4323487
	0.264	0.264	1.4142136
	15.4323487	<b>15.4323487</b>	2.2360680
	0.3937043	1.4142136	0.3819660
	3.2808693	1.7320508	0.6180340
	19.9922991	22.6276131	20.0826303
<b>55.</b>	0.4771213	2.7182818	0.3010300
	0.2908882	3.1415927	0.6180340
	1.6093295	0.7853982	0.3819660
	0.8450980	0.4342945	2.2360680
	0.3819660	4.8104774	1.7320508
	0.6180340	2.5399772	1.4142136
	0.3010300	0.3937043	15.4323478
	4.523467	14.8237261	22.1157111

1.6093295	0.3937043	3.785
0.6213768	0.3047973	15.4323487
3.785	3.2808693	0.6213768
0.264	1.6093295	1.4142136
15.4323478	0.6213768	3.2808693
1.4142136	3.785	0.3047973
1.7320508	0.264	4.8104774
24.8583194	10.2590772	29.6490831
57. Add by double	columns:	
45.68	154.31	73.86
73.91	<b>29</b> 6.8 <b>5</b>	<b>4</b> 53.71
<b>78.54</b>	736.48	137.64
534.69	345.19	98.87
134.70	<b>782.34</b>	643.48
<b>5</b> 81. <b>43</b>	78.43	462.71
1448.95	2393.60	1870.27
498.50	65.42	621.65
17.37	<b>63</b> 8.3 <b>4</b>	<b>167.32</b>
684.29	763.43	<b>856.96</b>
<b>2</b> 31.5 <b>6</b>	809.31	718.83
210.10	798.83	<b>501.49</b>
671.54	835.78	315.72
643.53	356.47	<b>768.44</b>
2956.89	4267.58	3950.41
791.52	32.54	<b>763</b> .89
<b>504.83</b>	<b>254</b> .63	78.23
879 <b>.26</b>	63.27	345.61
243.97	131.56	26.73
732.86	506.72	<b>489.56</b>
47.95	283.54	812.35
856.43	345.83	607.28
497.65	643.46	219.07
541.26	708.91	68.72
616.72	463.73	216.78
857.94	67.74	436.74
6570.39	3501.93	4064.96

**69.** 
$$8-3-2=3$$
;  $(8-3)-2=5-2=3$ ;  $8-(3-2)=8-1=7$ .  $8-2-3=3$ ;  $(8-2)-3=6-3=3$ ;  $8-(2-3)=8-(-1)=9$ .  $18-(7-3)=18-4=14$ ;  $18-(3-7)=18-(-4)=22$ ;  $18-3+7=22$ .

70. The following questions will illustrate the meaning of minus numbers:

Starting 90 miles south of Chicago, I go 50 miles due north; and the next day 80 miles, still north. How far from Chicago am I now? -90 + 50 + 80 = -90 + 130 = 40, the number of miles north. Ans.

With only \$67 I undertake to pay three bills, of \$47, of \$13, and of \$11. Can I pay the bills? How much shall I lack?

$$67 - (47 + 13 + 11) = 67 - 71 = -4$$
. I shall lack \$4. Ans.

73. Subtract 123 from each of the numbers: 234, 343, 424, 555, 676, 725, 839, 999, 1000, 10,101, 5120.

234	<b>343</b>	424	555	676	725
123	123	123	123	123	123
111	220	301	432	553	602
839	999	1000	10101	5120	
123	123	123	123	123	
716	876	877	9978	4997	

74. Subtract 456 from each of the numbers: 789, 879, 978, 6378, 6855, 6853, 7797, 7006, 3542, 4334, 9790, 3455.

789	879	978	6378	6855	6853
456	<b>45</b> 6	456	456	456	456
333	423	522	5922	6399	6397
7797	7006	3542	<b>4</b> 334	9790	3455
456	456	456	<b>456</b>	<b>456</b>	456
7341	6550	3086	3878	9334	2999

75. What is the difference between 779 and 974? 368 and 249? 479 and 2301? 2731 and 929? 708 and 394? 1123 and 1072? 891 and 773? 8103 and 5621? 19,001 and 3456? 792 and 2180?

974	368	2301	2731	708
779	249	479	929	394
195	119	1822	1802	314
1123	891	8103	19001	2180
1072	773	5621	3456	792
51	118	2482	15545	1388
Subtract:				
<b>\$</b> 183.45	\$716	3.43	\$647.51	\$270.04
76.47	628	3.74	<b>54</b> 9.64	128.31
<b>\$</b> 106.98	\$8	7.69	\$97.87	\$141.73
<b>\$</b> 125.	<b>\$ 24</b> '	7.9 <b>3</b>	\$641.87	\$56.27
101.50	129	9.47	333.95	29.89
\$23.50	<b>\$</b> 118	3. <b>46</b>	\$307.92	\$26.38

77. Subtract from 7854 each of the numbers: 788, 879, 567, 5006, 6107, 578, 867, 894, 463, 4603.

	<b>7854</b>	7854	<b>7854</b>	7854	<b>7854</b>
	788	879	<b>567</b>	5006	6107
	7066	6975	7287	2848	1747
	7854	<b>7854</b>	<b>7854</b>	7854	<b>7854</b>
	<b>578</b>	867	894	463	4603
	7276	6987	6960	7391	3251
78.	3.1415927		0.7853982		4.8104774
	2.7182818		0.5235988		0.4342945
	0.4233109		0.2617994		4.3761829
	2.5399772		0.3937043		3.2808693
	0.3937043		0.3047973		0.3047973
	2.1462729		0.088907	•	2.976072
•	3.2808693		3.785		15.4323487
	1.6093295		0.6213768		0.264
	1.6715398		3.1636232		15.1683487

	1.7320508	2.2360680	0.6180340
	1.4142136	0.3819660	0.3010300
	0.3178372	1.854102	0.317004
	2.2360680	2.2360680	0.3819660
	. 1.7320508	0.6180340	0.3010300
	0.5040172	1.618034	0.080936
79.	3.1415927	3.1415927	
	0.7853982	0.5235988	
	2.3561945	2.6179939	1.5707963
	0.7853982	0.5235988	0.5235988
	1.5707963	2.0943951	1.0471975
	0.7853982	0.5235988	0.5235988
	0.7853981	1.5707963	0.5235987
80.	1.	1.4142136	0.6180340
	0.3819660	0.6180340	0.3819660
	0.6180340	0.7961796	1.

- 81. In a school of 83 pupils, 37 are girls; the rest, boys. How many boys are there? 83 37 = 46. Ans.
  - 82. Take 1787 from 21,205, and what is the remainder? 21,205-1787=19,418. Ans.
- 83. Into a bowl containing 338 fine shot I poured a handful more, and the bowl then contained 720. How many did I pour in? 720-338=382. Ans.
- 84. From a box containing 209 oranges I took a basketful, and left 163 oranges. How many did I take in the basket?

209 - 163 = 46. Ans.

- 85. The minuend being 1718.754, and the subtrahend 1389.328, what is the remainder? 1718.754 1389.328 = 329.426. Ans.
- 86. If the minuend was 6532.18, and the remainder 1916.47, what was the subtrahend? 6532.18 1916.47 = 4615.71. Ans.
- 87. How many must be taken from 729,434 in order to leave 613,488? 729,434 613,488 = 115,946. Ans.

- 88. How many must be taken from 1,000,000 to leave 817,259? 1,000,000 817,259 = 182,741. Ans.
- 89. Subtract 4187.94 from 8010.101.

$$8010.101 - 4187.94 = 3822.161$$
. Ans.

90. Find the difference between 8,765,420 and 9,873,210. 9,873,210 - 8,765,420 = 1,107,790. Ans.

91. In a till are \$391 in bills, \$67.50 in gold, \$39.75 in silver, and \$2.77 in copper and nickel. How much money is in the till? \$391 + \$67.50 + \$39.75 + \$2.77 = \$501.02. Ans.

92. Starting out with \$315.75 in one wallet and \$54.37 in another, I pay the grocer \$127.38; the butcher, \$64.17; the shoemaker, \$21.40; the landlord, \$50; the tailor, \$35. What ought I to have left?

93. On a bill of \$753.43, I pay \$517.87. How much do I still owe? If I owe \$817.87, and have but \$637.50, how much do I lack of being able to pay?

<b>\$</b> 753.43	\$817.87
517.87	637.50
\$ 235.56	\$180.37

94. If a man was born January 1, 1812, how old was he January 1, 1878? How old December 31, 1857?

66			45	11	30
1812	1	1	1812	1	1
1878	1	1	1857	12	31

95. America was discovered in 1492. How many years after its discovery was each of the following events?

Settlement of Florida, 1565; of Virginia, 1607; of Massachusetts, 1620; of Quebec, 1608; French and Indian War, 1756; Declaration

of Independence, 1776; inauguration of Washington, 1789; war with England, 1812; Mexican War, 1846; Civil War, 1861.

1565	1607	1620	1608	1756
1492	1492	1492	1492	1492
73	115	128	116	264
1776	1789	1812	1846	1861
1492	1492	1492	1492	1492
284	297	320	354	369

96. How many days in common years, and in leap-years, between January 1 and March 1? January 4 and April 4? February 5 and May 5? February 7 and October 7? January 4 and July 4? March 4 and July 4?

Between January 1 and March 1, 58 days; 59 in a leap-year. Between February 5 and May . 5, 88 days; 89 in a leap-year. Between February 7 and October 7, 241 days; 242 in a leap-year. Between January 4 and July 4, 180 days; 181 in a leap-year. Between March 4 and July 4, 121 days; 121 in a leap-year.

97. The sum of two numbers is 3; their difference, 1. What are the numbers? The sum of two numbers is 5; their difference, 1. Required the numbers. What two numbers added together make 8, if the difference of the numbers is 2? If the difference is 0? if 4? if 6?

98. If the minuend is 9874, and remainder 3185, what is the subtrahend? The subtrahend being 7659, and remainder 675.68, what is the minuend?

9874	minuend.	<b>7659</b> .	subtrahend.
3185	remainder.	675.68	remainder.
6689	subtrahend.	8334.68	minuend.

99. The smaller of two numbers is 7.95764328; their difference is .00087692. What is the larger number?

7.95764328 + 0.00087692 = 7.9585202. Ans.

100. The larger of two numbers is 7.95764328, and their difference is 7.153485. What is the smaller number?

7.95764328 - 7.153485 = 0.80415828. Ans.

- 101. A hired man pumps out of my cistern in one hour 243.75 gallons; in the next hour, 227.5 gallons; in 45 minutes more, an additional 137.75 gallons; and the cistern is empty. How much was in it?

  243.75 + 227.5 + 137.75 = 609.

  609 gals. Ans.
- 102. From what number must I subtract 5 to leave 7? 8 to leave 9? From what number must I subtract 5.1736 to leave 8.1964? 6.231 to leave 9.6648? 74.213 to leave 25.787?

5	8	5.1736	6.231	74.213
7	9	8.1964	9.6648	25.787
-	<del></del>		<del></del>	
12	17	13.37	15.8958	<b>100</b> .

103. What must be subtracted from 1 to leave .5? to leave .53? to leave .5236? to leave .5235988?

1.	1.	1.	1.	<b>1.</b>
0.5	0.53	0.532	0.5236	0.5235988
0.5	$\overline{0.47}$	0.468	0.4764	0.4764012

104. I start on a journey of 3433 miles. The first day I make 428 miles; the second day, 511 miles; the third, 497 miles; the fourth, 513. How many miles of my journey remained for me at the close of each day? How many miles had I gone at the close of each day?

<b>3433</b>	
428	
3005 after first day.	428 end of first day.
511	511
2494 after second day.	939 end of second day.
497	497
1997 after third day.	1436 end of third day.
513	513
1484 after fourth day.	1949 end of fourth day.

105. Subtract 76,343 from the sum of 61,932, 51,387, 5193, 4674, and 8199; then subtract 23,657 from the remainder.

. 61,932 + .51,387 + 5193 + 4674 + 8199 = 131,385. 131,385 - 76,343 = 55,042 ; 55,042 - 23,657 = 31,385. Ans.

106. J. bought a farm and stock for \$7633.90; sold off the stock for \$305.75; then sold the farm for \$7325. What did he lose?

\$305.75 + \$7325 = \$7630.75; \$7633.90 - \$7630.75 = \$3.15; Ans.

107. If I gave \$4375 for my land, and paid for house, barn, sheds, and fences, \$2789.50; also \$973.75 for horses, cattle, tools, etc.; what did my farm and stock cost?

If I sold part of the land for \$675, and some cattle, etc., for \$217.50, what may I estimate as the cost of what I have left?

\$4375 + \$2789.50 + \$973.75 = \$8138.25. \$675 + \$217.50 = \$892.50.\$8138.25 - \$892.50 = \$7245.75. Ans.

108. Alfred the Great died at the age of 52, A.D. 901. In what year was he born? William the Conqueror began to reign A.D. 1066, and reigned 21 years. In what year did he die? Socrates was born B.C. 469, and died at the age of 70. In what year did he die? Plato was born B.C. 429, and died at the age of 82. In what year did he die? Demosthenes died at the age of 60, B.C. 322. In what year was he born? The battle of Marathon was fought B.C. 490; 560 years later Jerusalem was destroyed by Titus. In what year was Jerusalem destroyed?

A.D. 849	A.D. 1087	B.c. 399	в.с. 347	B.c. 382	A.D. 70
52	<u>21</u>	70	82	60	490
901	1066	469	429	322	560

109. John has 158 cents, James has 271 cents; James gives John 56 cents. Which has more than the other, and how many more?

116. Multiply 111 by 5; 123 by 3; 231 by 2; 114 by 3; 421 by 4; 512 by 5; 4328 by 4; 1187 by 6; 1782 by 8; 8.287 by 7; 9.6198 by 3; 62.818 by 7; 9.2758 by 8; 52.134 by 9.

111	123	231	114	421
5	3	2	3	4
555	369	462	342	1684
512 ·	4328	1187	1782	8.287
5	4	6	• 8	7
2560	17312	7122	14256	58.009
9.6198	62.818	9.2758	52.134	
3	7	8	9	
28.8594	439.726	74.2064	469.206	

117. Multiply 0.5235988 by 6; 0.7853982 by 4; 3.14159265 by 5, and the product by 5.

<b>3.14</b> 159265 <b>5</b>		
15.70796325	0.785398 <b>2</b> 4	0.5235988 6
78.53981625	3.1415928	3.1415928

118. Multiply 3.1416 by 11; by 12; by 10 and by 3, and add the two results; by 10 and by 4, and add the results; by 9 and by 6, and add the results. Multiply 2.236068 by 11; by 6 and by 7, and add the results; by 8 and by 9, and add the results; by 10 and by 7, and add the results (compare the sum of these two products with the sum of the last two products); by 10 and by 8, and add the results; by 12 and by 7, and add the results.

3.1416	3.1416	3.1416	3.1416	31.4160
11	12	10	3	9.4248
34.5576	37.6992	31.4160	9.4248	40.8408
3.1416	3.1416	31.4160	3.1416	3.1416
10	4	12.5664	9	6
31.4160	12.5664	43.9824	28,2744	18.8496

28.2744	2.236068	2,236068	2.236068	13.416408
18.8496	11	6	7	15.652476
47.1240	24.596748	13.416408	15.652476	29.068884
2.236068	2.236068	17.888544	2.236068	2.236068
8	9	20.124612	10	7
17.888544	20.124612	38.013156	22.360680	15.652476
22.360680	<b>2.236068</b>	2.236068	22.360680	2.236068
15.652476	10	8	17.888544	12
38.013156	22,360680	17.888544	40.249224	26.832816
2.236068	26.832816			
7	15.652476			
15.652476	42.485292			

120. How much is 10 times 3.14159265? 100 times? a million times? What will 10 barrels of apples cost, at \$3.75 a barrel? at \$2.17? at \$5.875? How much will 100 barrels cost at each of these prices, and at \$3.375? at \$5.125?

 $10 \times 3.14159265 = 31.4159265$ ;  $100 \times 3.14159265 = 314.159265$ ;  $1,000,000 \times 3.14159265 = 3,141,592.65$ ;  $10 \times \$3.75 = \$37.50$ ;  $10 \times \$2.17 = \$21.70$ ;  $10 \times \$5.875 = \$58.75$ ;  $100 \times \$3.75 = \$375$ ;  $100 \times \$2.17 = \$217$ ;  $100 \times \$5.875 = \$587.50$ ;  $100 \times \$3.375 = \$337.50$ ;  $100 \times \$3.375 = \$337.50$ ;  $100 \times \$5.125 = \$512.50$ .

122. What is a tenth of 2.36? a hundredth of 2.36? a thousandth of 0.63. Write the second members of the following equations, and then read them:

```
0.01 \times 7.8 = 0.001 \times 4.31 = 0.0001 \times 23.31 = 0.1 \times 0.065 = 0.01 \times 0.012 = 0.001 \times 0.
```

 $0.1 \times 2.36 = 0.236$ ;  $0.01 \times 2.36 = 0.0236$ ;  $0.001 \times 0.63 = 0.00063$ ;  $0.01 \times 7.8 = 0.078$ ;  $0.001 \times 4.31 = 0.00431$ ;  $0.0001 \times 23.31 = 0.002331$ ;  $0.1 \times 0.065 = 0.0065$ ;  $0.01 \times 0.012 = 0.00012$ .

123. Find the cost of 30 barrels of flour, at \$3.27 a barrel; of 70 barrels, at \$4.58; of 90 barrels, at \$6.76; of 100 barrels, at \$7.84; of 120 barrels, at \$8.57.

 $30 \times \$3.27 = \$98.10$ ;  $70 \times \$4.58 = \$320.60$ ;  $90 \times \$6.76 = \$608.40$ ;  $100 \times \$7.84 = \$784$ ;  $120 \times \$8.57 = \$1028.40$ .

124. Find the cost of 0.03 of a barrel of oil, at \$27.875 a barrel; of 0.7; of 0.009; of 0.17; of 0.019; of 0.13; of 0.8; of 0.83; of 0.014 of a barrel?

 $0.03 \times \$27.875 = \$0.83625$ ;  $0.7 \times \$27.875 = \$19.5125$ ;

 $0.009 \times \$27.875 = \$0.250875$ ;  $0.17 \times \$27.875 = \$4.73875$ ;

 $0.019 \times \$27.875 = \$0.529625$ ;  $0.13 \times \$27.875 = \$3.62375$ ;

 $0.8 \times \$27.875 = \$22.30$ ;  $0.83 \times \$27.875 = \$23.13625$ ;

 $0.014 \times \$27.875 - \$0.39025.$ 

### 125. What is the numerical value of the expressions:

 $30 \times 8.75$ ?  $700 \times 7.81$ ?  $300 \times 7.85$ ?  $0.07 \times 6.975$ ?  $8000 \times 65.432$ ?  $0.0009 \times 10356.78$ ?

 $30 \times 8.75 = 262.5$ ;  $700 \times 7.81 - 5467$ ;  $300 \times 7.85 = 2355$ ;

 $0.07 \times 6.975 = 0.48825$ ;  $8000 \times 65.432 = 523,456$ ;

 $0.0009 \times 10356.78 = 9.321102.$ 

129. Multiply 0.785398 by each of the following numbers: 2; 20; 3; 300; 5; 0.5; 0.005; 737; 7.37; 856; 85.6; 0.0856; 10; 1001; 1.001; 954; 0.00954.

0.785398 2	0.785398 <b>2</b> 0	0.785398 3	0.785398 300
1.570796	15.707960	2.356194	235.619400
<b>0.785398</b> . <b>5</b>	0.785398 0.5	0.785398 0.005	0.785398 737
$\overline{3.926990}$ $0.785398 \times 7.3$	0.3926990 $37 = 5.78838326.$	0.003926990	5497786 2356194 5497786
			578.838326

0.785398 856	$0.785398 \times 85.6 = 67.2300688.$		0.785398 10	
4712388 3926990	$0.785398 \times 0.0856$	$0.785398 \times 0.0856 = 0.0672300688.$		
6283184	0.785398	0.785398		
672.300688	1001	954		
	785398	3141592		
	785398	3926990		
	786.183398 7068582			
		749.269692		

 $0.785398 \times 1.001 = 0.786183398$ .

 $0.785398 \times 0.00954 = 0.00749269692$ .

130. Multiply 2150.42 by 0.1; by 0.001; by 0.75; by 0.075; by 0.083.

<b>2150.42</b> 0.083	2150.42 0.075	2150.42 0.75	2150.42 0.001	2150.42 0.1
645126 1720336	1075210 1505294	1075210 1505294	2.15042	215.042
178.48486	T61.28150	1612.8150		•

131. Multiply 1.4142136 by 0.7; by 0.707; by 0.7071; by 0.707107. Multiply 1.41421 by 1.4; by 1.4142; by 1.41422. Multiply 1.732 by 1.732; 2.23607 by 2.236; 0.618 by 618; 0.618034 by 0.618035. Subtract this last product from 1.

1.4142136 0.7	1.4142136 0.707	1.4142136 0.7071	1.4142136 0.707107
0.98994952	98994952	14142136	98994952
-	98994952	98994952	14142136
	0.9998490152	98994952	<b>9</b> 89 <b>94</b> 9 <b>52</b>
	0.0000100102	0.99999043656	98994952
			1.0000003360552

1.41421	1.41421	1.41421
1.41422	1.4142	1.4
282842	282842	565684
<b>2</b> 828 <b>42</b>	565684	141421
565684	141421	1.979894
141421	565684	1.010001
565684	141421	
141421	1.999975782	
2.0000040662	2003000	
0.618034	0.618	2.23607
0.618035	618	2.236
3090170	4944	1341642
1854102	618	670821
4944272	<b>370</b> 8	447214
618034	381 924	447214
3708204	001.021	4.99985252
0.381966643190		
	1.41422 282842 282842 565684 141421 565684 141421 2.0000040662 0.618034 0.618035 3090170 1854102 4944272 618034 3708204	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$

133. Find the value of the expressions:  $88 \times 718.54$ ;  $96 \times 6.8193$ ;  $6.3 \times 71.569$ ;  $1.32 \times 234.769$ .

234.769	71.569	6.8193	718.54
0.12	0.9	12	11
28.17228	64.4121	81.8316	7903.94
11	7	8	8
309.89508	450.8847	654.6528	63231.52

134. Multiply 291.47 by 16, and the product by 625. In like manner, find the continued products:	291.47 16
$8 \times 125 \times 278.56$ ; $8 \times 3.75 \times 3.33333$ ; $8 \times 625 \times 1.5708$ .	174882 29147
$8 \times 125 \times 278.56 = 1000 \times 278.56$	<b>4</b> 663.52
= 278,560.	625
$8 \times 3.75 \times 3.33333 = 30 \times 3.333333$	2331760
= 99.9999.	932704
$8 \times 625 \times 1.5708 = 5000 \times 1.5708$	<b>2</b> 798112
= 7854.	<b>2</b> 914700.00

135. One mile measures 5280 feet. How many feet in 3 tenths of a mile? in 0.7? in 0.17? in 0.573? in 0.846 of a mile?

 $0.3 \times 5280 = 1584$ ;  $0.7 \times 5280 = 3696$ ;  $0.17 \times 5280 = 897.6$ ;  $0.573 \times 5280 = 3025.44$ ;  $0.846 \times 5280 = 4466.88$ .

138. Multiply (using complements) 0.7854 by 9.9; by 0.99; by 0.099. Multiply 0.5236 by 99.7; by 9.989; by 9.87. Multiply 8537 by 0.0097; by 0.9995.

$0.7854 \times 10$	<b>-</b> 7.854	0.7854	$\times 1$	<b>-</b> 0.7854
$0.7854 \times 0.1$	-0.07854	0.7854	$\times$ 0.01	= 0.007854
$0.7854 \times 9.9$	<b>-</b> 7.77546	0.7854	× 0.99	<b>-</b> 0.777546
$0.7854 \times 0.1$	<b>-</b> 0.07854	0.5236	× 100	<b>-</b> 52.36
$0.7854 \times 0.001$	= 0.0007854	0.5236	$\times 0.3$	<b>-</b> 0.15708
$0.7854 \times 0.099$	<b>-</b> 0.0777546	0.5236	× 99.7	- 52.20292
$0.5236 \times 10$	<b>=</b> 5 236	0.5236	×10	<b>-</b> 5.236
$0.5236\times0.11$	= 0.0057596	0.5236	$\times$ 0.13	<b>-</b> 0.068068
$0.5236 \times 9.989$	<b>-</b> 5.2302404	0.5236	× 9.87	<b>-</b> 5.167932
8537 × 0.01	<b>=</b> 85.37	8537	×1	<b>-</b> 8537
$8537 \times 0.0003$	B = 2.5611	8537	$\times$ 0.0005	<b>4.2685</b>
8537 × 0.0097	7 = 82.8089	8537	× 0.9995	<del>=</del> 8532.7315

139. Multiply 0.61803 by 147; by 373; by 7.56; by 8.93; by 9.93. Multiply 0.5236 by 5.99; by 7.99; by 8.997; by 699.98.

0.61803	<b>0</b> .61803	0.61803	0.61803	0.61803
147	373	7.56	8.93	9.93
432621	185409	370818	185409	185409
247212	432621	309015	556227	556227
61803	185409	432621	<b>4</b> 94424	556227
90.85041	230.52519	4.6723068	5.5190079	6.1370379

0.5236	0.5236	0.5236	699.98
5.99	7.99	8.997	0.5236
47124	47124	36652	419988
47124	47124	47124	209994
26180	36652	47124	139996
3.136364	4.183564	41888	349990
		4.7108292	366.509528

140. Multiply 0.7854 by 0.618; by 0.382; by 0.7854; by 0.302. Multiply 2.718 by 0.618; by 0.382; by 0.7854; by 0.607.

0.7854	0.7854	0.7854	, -	0.7854
0.618	0.382	0.7854	•	0.302
62832	15708	31416	ŧ	15708
7854	62832	39270		23562
47124	<b>235</b> 62	62832	•	0.2371908
0.4853772	0.3000228	54978		
		0.61685316		
2.718	2.718	2.718	****	2.718
0.618.	0.382	0.7854		0.607
21744	5436	10872	•	19026
<b>2718</b>	21744	13590		16308
16308	8154	21744		1.649826
1.679724	1.038276	19026		
4		2.1347172		

141. Find the continued products:  $0.477 \times 101 \times 0.708$ ;  $15.43 \times 0.4343 \times 3$ ;  $4 \times 0.175 \times 3.28$ ;  $0.615 \times 0.771 \times 10$ ;  $3.2809 \times 5 \times 0.71$ ;  $0.785 \times 0.7 \times 0.202$ ;  $0.471 \times 0.807 \times 22$ ;  $3.28 \times 25 \times 0.909$ .

0.477	15.43	0.175	0.615
	0.4343	4	0.771
477	4629	0.799	615
477	6172	3.28	4305
48.177	4629	2.296	4305
0,708 385416 337239	$\frac{6172}{6.701249}$		0.474165
34.109316	25.103747	<u>.</u>	· ·

3.28	0.471	0.785	3.2809
25	0.807	0.7	5
1640	3297	0.5495	16,4045
<b>656</b> <sub>.</sub>	3768	0.202	0.71
82.99	0.380097	10990	164045
0.909	22	10990	1148315
738	760194	0.1109990	11.647195
<b>73</b> 8	760194	ŧ	
74.538	8.362134		
		,	

144. Find the product, to the fifth fractional place, of 3.14159265 by 2.236. Find  $1414.2136 \times 14142.136$ , to the second place; 0.618034 by 0.618034, to the sixth place; 2.236068 by 2236.068, to the third place; 1.73205 by 1732.0508, to the second place.

3.141592	65	1414.2136000		0.6180340	)
6322		63124141	· -	4308160	)
6283185		14142136000		3708204	-
628318		5656854400		61803	
94248	•	141421360		49442	
18849		56568544		185	•
7 094808		2828427		24	
7.02460Ø		141421	•	0.3819658	
		42426	•	· · · 0.381966.	Ans.
		8485		V.301900.	A1768.
		20000001.063		* * *	
	2,2360680			1.732050	
	8606322			80502371	
	44721360		•	1732050	
	4472136			1212435	
	670820		•	51962	
	134163			3464	
	1341		_	87	
	178 '	•		1	
	4999.9998		-	2999.999	-
	5000. Ans.	• . •		3000. Ans.	

147. 1. What will a man earn in a year if he has \$2 a day, omitting Sundays? Suppose that the year begins on Sunday? Suppose the year to be leap-year, and not begin on Sunday? Suppose it leap-year, and to begin on Saturday?

$$(365-52) \times \$2 = \$626;$$
  $(365-53) \times \$2 = \$624;$   $(366-52) \times \$2 = \$628;$   $(366-53) \times \$2 = \$626.$ 

2. If a field of corn averages 2 ears to a stalk, how many ears on 673 stalks?

3. At 27 bushels an acre, how much wheat to the square mile of 640 acres, deducting 47 acres for roads and waste land?

16,011 bu. Ans.

4. How much money would be required to give \$7000 to each of 7568 men?

5. In a certain book of 378 pages, the words average 7 letters to a word, and 10 words to a line. There are, on an average, 29 lines to a page. How many letters in the book?

252,321.5 bu. Ans.

6. How many bushels of wheat in a township of 37 square miles, if we deduct 47 acres to the square mile for roads and waste, and suppose that half the remainder is in wheat averaging 23 bushels to an acre?

47	640	
37	37	
329	4480	
141	1920	
1739	23680	
	1739	
	21941	
	0.5	
	10970.5	•
	23	real multiplicand.
	329115	,
	<b>2194</b> 10	
	252321.5	
		222224

7. If 5700 persons, each paying 1 cent toll, and 324 carriages, each paying 5 cents toll, pass over a bridge in a day, how much money will be received?

8. A merchant bought 960 pounds of cheese at 7 cents a pound, and 147 pounds of butter at 20 cents. He gave in payment 12.5 yards of cloth at 1 dollar a yard, 2 barrels of sugar, each weighing 226 pounds, at 9 cents a pound, and the remainder in cash. How much money had he to pay?

960 226 0.07 real multiplicand. 2 real multiplicand. 67.20 452 0.09 real multiplicand. 40.68 12.50 147 53.18 0.20 real multiplicand. 96.60 --29.40 67.20 53.18 96.60 43.42 \$43.42. Ans.

148. 1. Express the product of  $7^5 \times 7^3$ ;  $8^2 \times 8$ ;  $2^6 \times 2$ ;  $5^4 \times 5^2$ .  $7^5 \times 7^3 = 7^3$ ;  $8^2 \times 8 = 8^3$ ;  $2^6 \times 2 = 2^9$ ;  $5^4 \times 5^2 = 5^6$ .

- 2. Express the product of:  $3.01^2 \times 3.01$ ;  $0.67^2 \times 0.67^8$ ;  $0.208 \times 0.208^3$ .  $3.01^2 \times 3.01 = 3.01^3$ ;  $0.67^2 \times 0.67^8 = 0.67^{10}$ ;  $0.208 \times 0.208^3 = 0.208^4$ .
- 3. Express the product of:

 $2.003^2 \times 2.003^4$ ;  $20.03^3 \times 20.03$ ;  $20.03 \times 20.03^2$ .  $2.003^2 \times 2.003^4 = 2.003^6$ ;  $20.03^3 \times 20.03 = 20.03^4$ ;  $20.03 \times 20.03^2 = 20.03^3$ .

153. Divide 963 by 3; 846 by 2; 846 by 3; 846 by 6; 848 by 4; 52.05 by 5; 84.028 by 7; 13.31 by 11; 1.728 by 12.

3) 963	2) 846	3) 846
321	423	282
6)846	4)848	5) 52.05
141	212	10.41
7)84.028	11) 13.31	12)1.728
12.004	1.21	0.144

158. 1. Divide 0.003 by 0.07; 0.003 by 110; 110 by 0.003.

7) 0.30000 11) 0.000300 3) 110000.00000 0.04286 0.000027 36666.66667

2. Divide 0.07 by 0.003; 110 by 0.07; 1.3 by 0.07.

3) 70.00000 7) 11000.00000 7) 130.00000 23.33333 1571.42857 18.57143 3. Divide 1.7 by 0.07; 0.07 by 110; 1.3 by 110.

7) 170,00000 24,28571

11)0.00700 0.00064 0.01182

4. Divide 1.7 by 110; 0.07 by 1.2; 0.003 by 1.2.

11<u>)0.17000</u> 0.01545 12) 0.70000 0.05833

12) 0.0300 0.0025

5. Divide 110 by 1.2; 1.7 by 1.2; 17 by 1.2.

12)1100.00000 91.66667 12) 17.00000 1.41667

12) 170.00000 14.16667

6. Divide 136 by 0.06; 136 by 0.12; 136 by 1100.

6) 13600.00000 2266.66667 12<u>) 13600.00000</u> 1133.33333

11)1.36000 0.12364

7. Divide 256 by 0.8; 2.56 by 0.08; 0.0256 by 0.008.

8) <u>2560</u> 320 8)256 32

8) <u>25.6</u> 3.2

8. Divide 256 by 8000; 1.06 by 0.9; 1.06 by 9000.

8) <u>0.256</u> 0.032

9)10.60000

9) 0.00106 0.00012

160. 1. Divide 1.6093295 by 0.479; by 0.917; by 0.017; by 0.0087.

3.35977	1.75499	94.66644	184.98040
479) 1609.3295	917) 1609.3295	17) 1609.3295	87)16093.2950
1437	917	153	87
1723	6923	79	739
1437	6419	68	696
2862	5042	113	433
2395	4585	102	348
4679	4579	112	852
4311	3668	102	783
3685	9115	109	699
3353	8253	102	696
332	862	75 68 7	350 348 2

2. Divide 3 by 1.7; by 1.73; by 1.732; by 1.7321.

1.76471	1.73410
17)30.0000	173) 300.0000
17	173
130	1270
119	1211
110	590
102	519
80	710
68	692
120	180
· 119	173
1	7
1.73210	1.73200
1732)3000.0000	17321)30000.0000
1732	17321
12680	126790
12124	121247
5560	55430
5196	51963
3640	34670
	010,0
3464	34642
3464 1760	-

3. Divide 1.6093295 by 5280, and the quotient by 12.

28

0.0003048	0.0000254
<b>528</b> ) 0.16093295	12)0.0003048
1584	
2532	
2112	
4209	

4. Divide 2 by 1.4142; 5 by 2.236.

165. Perform the work in the following questions by the use of reciprocals:

1. 
$$8 \times 0.25 = 8 + 4 = 2$$
.  
2.  $171 + 0.25 = 171 \times 4 = 684$ .  
3.  $876 \times 1.25 = 876 + 0.8$   
 $= 8760 + 8$   
 $= 1095$ .  
4.  $132 \times 2.5 = 132 + 0.4$   
 $= 1320 + 4$   
 $= 330$ .  
5.  $591 + 2.5 = 591 \times 0.4$   
 $= 236.4$ .  
6.  $756 + 0.125 = 756 \times 8$   
 $= 6048$ .  
7.  $268 \times 25 = 268 + 0.04$   
 $= 26800 + 4$   
 $= 6700$ .  
9.  $567 + 625 = (567 + 5) \times 0.008$   
 $= 113.4 \times 0.008$   
 $= 0.9072$ .  
10.  $1764 \times 0.025 = 1764 + 40$   
 $= 215,240$ .  
 $= 215,240$ .  
 $= 59,616 + 7$   
 $= 8516.6$ .  
13.  $651 \times 0.33333 = 651 + 3$   
 $= 217$ .  
14.  $456 \times 6.66667 = 456 + 0.15$   
 $= 45,600 + 15$   
 $= 3040$ .

8. 753 + 25

 $= 753 \times 0.04$ 

**- 30.12.** 

15.  $1554 \times 0.16667 = 1554 + 6$ 

= 259.

16. 
$$432 + 1.33333 = 432 \times 0.75$$
  
= 324.  
17.  $375 + 16.667 = 375 \times 0.06$ .  
= 22.50.  
18.  $225 + 6.6667 = 225 \times 0.15$   
= 33.75.

167. 1. Taking 7 as unity, what would be the value of 14? of 28? of 35? of 3.5? of 2.8105? of 6.31415?

$$7)14$$
  $7)28$   $7)35$   $7)3.5$   $7)2.8105$   $7)6.31415$   $2$   $4$   $5$   $0.5$   $0.4015$   $0.90202$ 

2. If the side of a square is 10 inches, and its diagonal 14.14214, express the side in terms of the diagonal as unity.

- 3. If the diagonal of a square is one foot, what decimal of a foot must its side be? 1 + 1.414214 = 0.70710. (See 167, 2.)
- 4. If the diameter of a circle is 11.3 inches, and its circumference 35.5 inches, what is the circumference in terms of the diameter? What is the diameter in terms of the circumference?

3.14159	0.31831
113)355.00000	355) 113.00000
339	1065
160	650
, 1 <b>13</b>	355
470	2950
452	2840
180	1100
113	1065
670	350
565	•

1050 1017 5. What decimal fraction of 87 is 47? 53? 43.5? 29?

0.54023	0.60919	0.5	0.333
87)47.00000	87) 53.00000	87)43.5	87) 29.000
435	522	43.5	261
350	800		290
- 348	783		<b>2</b> 61
200	170		290
174	87		<b>261</b>
260	830		29
	783		

6. How many times 393 is 587? 7857? 131? 196.5?

0.5	0.33	19.99	1.49
393) 196.5	393) 131.00	393) 7857.00	393) 587.00
196.5	1179	393	393
-	1310	3927	<del>1940</del>
	1179	3537	1572
	131	3900	3680
		3537	<b>3537</b>
		363	

7. How many 684's are there in 1368? in 1760? in 342? in 77? in 6.84? in 0.0785?

$ar{2}$	0.5	0.01
684) 1368	684) 342.0	$684)\overline{6.84}$
1368	342 0	6 84
	<del></del>	
2.57	0.1126	0.00011
684) 1760.00	684) 77.000	684) 0.0785
1368	684	684
3920	860	101
3420	684	
5000	1760	
<b>4788</b> .	1368	
	392	

168. 1. Divide 11.4285285	4. Divide 0.0053 by 72.654 to
by 3.1415927 to six decimal	eight decimal places.
places.	0.00007294
3.637813	72854) 5.30000
31 <b>475927</b> ) 114285285	508578
94247781	21422
20037504	14531
18849556	6891
1187948	6539
942478	gramma-strike
245470	352
219911	300
25559	5. Divide 6 by 0.1573 to three
<b>25132</b>	decimal places.
427	38.144
314	1573) 60000.0
113	4719
94	12810
<b>*</b>	12584
2. Divide 0.004239239 by	2260
3.2783278 to five decimal places.	1573
0.00129	687
32783278) 42392.39	<b>629</b>
3278328	
960911	6. Divide 0.11 by 1937.43 to
655675	eight decimal places.
305236	0.00005677
295049	193743)11.0000
9 Divido 427 by 915 952 to	96872
3. Divide 437 by 215.253 to three decimal places.	13128
2.030	11624
215253) 437000.	1504
43051	1356
• 649	148
646	133

# 7. Divide 46 by 0.00751515151 to three decimal places.

6120.968

169. 1. Find the value of  $10^{0}$ ;  $10^{1}$ ;  $10^{2}$ ;  $10^{3}$ ;  $10^{4}$ ;  $10^{5}$ ;  $10^{5}$ .  $10^{6} = 1$ ;  $10^{1} = 10$ ;  $10^{2} = 10 \times 10 = 100$ ;  $10^{3} = 10 \times 10 \times 10 = 1000$ ;  $10^{4} = 10 \times 10 \times 10 \times 10 = 10,000$ ;  $10^{5} = 10 \times 10 \times 10 \times 10 = 100,000$ ;  $10^{6} = 10 \times 10 \times 10 \times 10 \times 10 \times 10 = 1,000,000$ .

- 2. Find the value of  $10^{\circ}$ ;  $10^{-1}$ ;  $10^{-2}$ ;  $10^{-8}$ ;  $10^{-4}$ ;  $10^{-5}$ ;  $10^{-6}$ .  $10^{\circ} = 1$ ;  $10^{-1} = 0.1$ ;  $10^{-2} = 0.1^{2} = 0.01$ ;  $10^{-8} = 0.1^{8} = 0.001$ ;  $10^{-4} = 0.1^{4} = 0.0001$ ;  $10^{-5} = 0.1^{5} = 0.00001$ ;  $10^{-6} = 0.1^{6} = 0.000001$ .
- 3. Find the value of  $10^{0} \times 10^{0}$ ;  $10^{1} \times 10^{-1}$ ;  $10^{2} \times 10^{-2}$ ;  $10^{8} \times 10^{-8}$ ;  $10^{4} \times 10^{-5}$ .

$$10^{0} \times 10^{0} = 10^{0} = 1$$
;  $10^{1} \times 10^{-1} = 10^{0} = 1$ ;  $10^{2} \times 10^{-2} = 10^{0} = 1$ ;  $10^{3} \times 10^{-8} = 10^{0} = 1$ ;  $10^{4} \times 10^{-5} = 10^{-1} = 0.1$ .

4. Find the value of  $10^8 + 10^{-1}$ ;  $10^{-2} + 10^2$ ;  $10^{-1} + 10^{-3}$ ;  $20^{-2} + 10^{-4}$ .

$$10^{3} + 10^{-1} = 10^{4} = 10,000$$
;  $10^{-2} + 10^{2} = 10^{-4} = 0.1^{4} = 0.0001$ ;  $10^{-1} + 10^{-8} = 10^{3} = 100$ ;  $10^{-2} + 10^{-4} = 10^{3} = 100$ .

5. Find the value of  $10^{-8} \times 10^{2}$ ;  $10^{8} + 10^{8}$ ;  $10^{-8} + 10^{2}$ ;  $10^{-8} + 10^{-8}$ .  $10^{-8} \times 10^{2} = 10^{-1} = 0.1$ ;  $10^{8} + 10^{2} = 10^{1} = 10$ ;  $10^{-8} + 10^{2} = 10^{-5} = 0.1^{5} = 0.00001$ ;  $10^{-8} + 10^{-8} = 10^{1} = 10$ .

- 6. Find the value of  $10^2 + 10$ ;  $10^2 + 10^3$ ;  $10^0 + 10^{-1}$ ;  $10^{-1} + 10^{-1}$ .  $10^2 + 10 = 10$ ;  $10^2 + 10^3 = 10^{-1} = 0.1$ ;  $10^0 + 10^{-1} = 10$ ;  $10^{-1} + 10^{-1} = 10^0 = 1$ .
- 7. Find the value of  $1.01^2 + 1.01^{-1}$ ;  $1.01^2 \times 1.01^{-1}$ ;  $1.01^{-2} + 1.01^{-1}$ .  $1.01^2 + 1.01^{-1} = 1.01^3 = 1.030301$ ;  $1.01^2 \times 1.01^{-1} = 1.01$ ;  $1.01^{-2} + 1.01^{-1} = 1.01^{-1} = 1 + 1.01 = 0.99009$ .

#### EXERCISE I.

1. Express in words, 327.244.

Three hundred twenty-seven and two hundred forty-four thousandths.

- 2. Express in words, 80.9056. Eighty and nine thousand fifty-six ten-thousandths.
- 3. Express in words, 0.390012.
  Three hundred ninety thousand twelve millionths.
- 4. Express in words, 20000.002.

  Twenty thousand and two thousandths.
- 5. Express in words, 0.0000008. Eight ten-millionths.
- 6. Express in words, 41.27105.

six millionths.

Forty-one and twenty-seven thousand one hundred five hundredthousandths.

7. Write in figures, two hundred thirty-five and eight hundred thirty-five thousandths.

235.835.

8. Write in figures, seventy-four and two hundred three thousand

74.203006.

9. Write in figures, twelve hundred and eight thousand three tenmillionths.

1200.0008003.

- 10. Write in figures, five thousand sixty-four millionths. 0.005064.
- 11. Write in figures, one million and four tenths.
  1000000.4.
- 12. Write in figures, six hundred-millionths.
  0.0000006.
- 13. Multiply and divide 789.365 by 10; by 100; by 100,000. 7893.65; 78.9365; 78936.5; 7.89365; 78,936,500; 0.00789365.
- 14. Multiply and divide 0.004 by 100; by 10,000; by 1000. 0.4; 0.00004; 40; 0.0000004; 4; 0.000004.
- 15. Multiply and divide 436 by 1,000,000; by 1000; by 10. 436,000,000; 0.000436; 436,000; 0.436; 4360; 43.6.
- 16. Multiply and divide 0.1 by 10; by ten millions. 1; 0.01; 1,000,000; 0.00000001.
- 17. Find the value of 21.3706 + 15.243 + 1.8954 + 0.26891 + 5.328 + 29.74.

21.3706 15.243 1.8954 0.026891 5.328 29.74 73.603891

18. Find the value of 57 + 0.0057 + 6.8 + 1200 + 0.847 + 159.2 + 3.

57. 0.0057 6.8 1200. 0.847 159.2 3. 1426.8527 19. Find the value of 0.0012 + 10 + 5.8281 + 5 + 39.43 + 0.6827 + 1.

0.0012 10. 5.8281 5. 39.43 0.6827 1.

**20.** Find the value of 23.9875 - 12.4764; 35.14732 - 27.62815.

61.942

 23.9875
 35.14732

 12.4764
 27.62815

 11.5111
 7.51917

21. Find the value of 102.1274 - 83.072; 39.801 - 17.9645.

 102.1274
 39.801

 83.072
 17.9645

 19.0554
 21.8365

22. Find the value of 30 - 5.2817; 1.7 - 0.8469.

 30.0000
 1.7000

 5.2817
 0.8469

 24.7183
 0.8531

23. Find the value of 1 - 0.54237; 100 - 0.00176.

 $\begin{array}{ccc}
1.00000 & 100.00000 \\
0.54237 & 0.00176 \\
\hline
0.45763 & 99.99824
\end{array}$ 

**24.** Find the value of 24.271 - 3.5485 + 15.271 - 13.256 - 14.125.

3.6485 24.271 13.256 39.542 15.271 14.125 31.0295 39.542 31.0295 8.5125

25. Find the value of 52 + 0.52 - 17.8946 - 30.254 - 0.5 + 21.12. **52**. 17.8946 30.254 0.52 73.64 21.12 0.5 48.6486 73.64 48.6486 24.9914 **26.** Find the value of  $41.289 \times 0.5$ ;  $0.268 \times 0.9$ ;  $0.112 \times 0.2$ . 41.289 0.268 0.112 0.5 0.9 0.2 20.6445 0.2412 0.0224 27. Find the value of  $2.435 \times 4.23$ ;  $71.651 \times 3.37$ ;  $0.251 \times 0.04$ . 2.435 71.651 0.251 4.23 3.37 0.04 0.01004 7305 501557 4870 214953 9740 **2**14953 10.30005 241.46387 28. Find the value of  $0.0012 \times 0.005$ ;  $2.26823 \times 200$ ;  $5.6125 \times 10^{-2}$ 0.0768. 0.0012 2.26823 5.6125 0.005 200 0.0768 0.000006 453.646 449000 336750 392875 0.43104 **29.** Find the value of  $0.7 \times 7 \times 0.07$ ;  $0.15625 \times 23.7 \times 0.00192 \times 5$ . 0.7 0.15625 3.703125 7 23.7 0.00192 4.9 109375 7406250 0.07 46875 33328125 3703125 31250 0.343 3.703125 0.00711 5

0.03555

30. Find the value of  $(2.465 + 1.121) \times (3.2 - 2.89)$ .

 $(2.465 + 1.21) \times (3.2 - 2.89)$ 

 $-3.675\times0.31$ 

**- 1.13925.** 

31. Find the value of  $(3.01)^2$ ;  $(0.045)^2$ ;  $(0.0081)^3$ ;  $(5.1004)^3$ ;  $(0.76)^3$ .

		•
3.01	0.045	0.0081
3.01	0.045	0.0081
301	225	81
903	180	<b>64</b> 8
9.0601	0.002025	0.00006561
	5.1004	0.76
	5.1004	0.76
	204016	456
	51004	532
	<b>25</b> 5020	0.5776
	<b>26.014</b> 08016	0.76
_	5.1004	<del>34656</del>
1	0405632064	40432
	1408016 040080	0.438976
132.68	2214448064	

32. Find the value of  $(0.125)^2 \times (0.32)^3$ .

0.125	0.32	0.032768
0.125	0.32	0.015625
625	64	163840
250	<b>9</b> 6	65536
125	0.1024	196608
0.015625	0.32	163840 32768
	<b>2048</b> <b>3</b> 072	0.000512
	0.032768	

33. Divide 291.84 by 6; 0.12936 by 12; 7.92801 by 0.9.

6) 291.84 48.64 12) 0.12936 0.01078

9)7.92801

34. Divide 58.383 by 0.39; 0.28744 by 0.08; 491.205 by 0.065.

149.7	·	7557
39) 5838.3 39	8) 28.744 3.593	65) 491205 455
193		362
156		325
378		370
351		325
<b>2</b> 73		455
<del>273</del>		455

35. Divide 68.325 by 6.25; 0.732 by 1.6; 1208.88 by 0.438.

10.932	0.4575	<b>276</b> 0
625) 6832.500	16) 7.3200	438) 1208880
625	64	876
5825	92	3328
5625	80	3066
2000	120	2628
1875	112	2628
1250	80	-
1250	80	·
<del></del>	-	

36. Divide 498 by 0.0125; 7 by 0.007; 1000 by 0.0001.

The reciprocal of 0.0125 is 80.

498 80 39840 7)7000

1)10000000 10000000 37. Divide 0.235 by 10.24; 27 by 12; 0.00507702 by 0.0283.

0.02295		0.1794
1024)23.50000	12) 27.00	283) 50.7702
2048	2.25	283
3020		2247
2048		1981
9720	•	2660
9216		2547
5040		1132
		1132

38. Divide 89.3 by 0.00752; 74.1 by 0.0256; 1 by 0.128.

11875	2894.53125	7.8125
752) 8930000	256)741000.00000	128)1000.0000
752	512	896
1410	2290	1040
<b>752</b>	2048	1024
6580	2420	160
6016	2304	128
5640	1160	320
5264	1024	256
3760	1360	640
3760	1280	640
-	800	- Control
	768	
	320	
	256	•
	640	
	512	
	1280	•
	1280	

39. Divide 0.39842 by 3.7164; 281.5 by 13.789; 0.0005 by 0.0028.

0.10720	20.41482	0.17857
37164) 3984.20000	13789) 281500.00000	28) 5.00000
37164	27578	<b>28</b>
267800	57200	220
<b>2</b> 60148	55156	196
76520	20440	240
74328	13789	224
21920	66510	160
23.20	55156	140
	113540	200
	110312	196
	32280	
	27578	
<b>40.</b> Divide 63.0412	8 by 912.85; 287.209	by 0.00493; 2000
by 0.0059. 0.06905	58257.40365	338983.05084
91285) 6304.12800	493) 28720900.00000	59) 20000000,00000
547710	2465	177
•		•
827028 821565	4070 3944	230 177
<del>(2,-2'</del>		
<b>54</b> 6300 <b>4</b> 56425	1269 986	530 <b>4</b> 72
100120	-	•
	2830 2465	580 531
	<del>(</del>	
	3650 3451	490 472
	1990	180
	1972	177
A	1800	300
1.7	1479	<b>295</b>
** :	3210	500
•	2958	<b>472</b>
÷.	2520	280
	<b>2465</b>	236
	<del></del>	<del></del>

EXERCISE II.

1. 
$$1.4 + 2.08 + 3.895 =$$

1.  $4$ 
2.08
3.  $1.667 + 0.4 + 0.286 + 6.08$ 
4.  $0.636 + 0.931 =$ 
2.08
3.  $0.4$ 
3.  $0.286$ 
3.  $0.286$ 
3.  $0.286$ 
4.  $0.286$ 
4.  $0.28$ 
4.  $0.28$ 
5.  $0.28$ 
6.  $0.28$ 
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9

$$= 10 - (6.25 - 5.545) - 0.295$$

$$= 10 - 0.705 - 0.295$$

$$= 10 - 1$$

$$= 9.$$

9. 
$$1.5 \times 0.08 \times 0.5 =$$

$$\begin{array}{c}
1.5 \\
0.08 \\
\hline
0.12 \\
0.5 \\
\hline
0.06
\end{array}$$
10  $0.1204 \times 0.0168 \times 100 =$ 

$$\begin{array}{c}
0.1204 \\
0.0168 \\
\hline
9632 \\
7224 \\
\hline
1204 \\
\hline
0.00202272 \\
\hline
100 \\
\hline
0.202272 \\
\end{array}$$

11.	$0.04 \times 3.25 \times 0.06 =$	<b>12</b> . 36×0.00	$2 \times 2.05 \times 0.00765 =$
	3.25	36	0.1476
	0.04	0.002	0.00765
	0.13	0.072	7380
	0.06	2.05	8856
	0.0078	360	10332
		144	0.00112904
		0.1476	
13.	$0.139 \times 28 + 42 \times 0.002 +$ $= 3.892 + 0.084 +$ $= 4 - 1$ $= 3.$		<b>20</b> .
14.	$(10-1.25)\times0.2+0.02\times2$ $= 8.75\times0.2+0.02\times2$ $= 1.75+0.056+27.3$ $= 29.106-16.106$ $= 13.$	$(2.8 + (8.03 - 5.3) \times$	•
15.	28.3696 + 1.49 =	<b>17.</b> 8.8779 +	175.8 =
	19.04	_	0.0505
	149) 2836.96	1758	88.7790
	149	·	8790
	1346		8790
	1341		8790
	596		
	<u>596</u>		
16.	$0.27 \div 0.00225 =$	<b>18.</b> 0.0427	+ 92.3 =
	120		0.00046
	225) 27000	923	0.42700
	225		3692
	450		5780
	450		<b>5538</b> .

#### 19. 0.28744 + 800 =

# 8)0.0028744 0.0003593

24. 
$$2+0.01-(0.2+0.02+0.8+10)+36.48+8-(4+0.05-2+0.6+1.25$$
  
=  $200-(10+0.08)+4.56-(80-2+0.48)$   
=  $200-10.08+4.56-78.48$   
=  $204.56-88.56$   
=  $116$ .

25. 
$$72.2 + 10 - 2 + (0.5 + 1.60) + 2.125 + (1.75 - 0.5)$$
  
=  $72.2 + 10 - 2 + 0.3125 + 2.125 + 1.25$   
=  $7.22 - 6.4 + 1.7$   
=  $8.92 - 6.4$   
=  $2.52$ .

# EXERCISE III.

1. What number subtracted 88 times from 80,005 will leave 13 as a remainder?

		909
80,005		88) 79992
13	4	792
79,992		792
•		792

2. If 7 men can build a wall in 16 days, how many men will it take to build a wall three times as long in half the time?

3. How many minutes are there between 25 minutes past 8 in the morning and midnight?

4. The velocity of sound being 1090 feet per second, at what distance is a gun fired, the report of which I hear 11 seconds after seeing the flash? (5280 feet make a mile.)

	2.27083
1090	5280) 11990.00000
11	10560
1090	14300
1090	10560
11990	37400
	36960
	44000
	42240
	17600
	15840

5. How long would it take to travel 30.2375 miles at the rate of 8.85 miles per hour?

6. The circumference of a circle being 3.1416 times the diameter, find the circumference of a circle whose diameter is 6.8 feet; also, find the diameter of a circle whose circumference is 20 inches.

	6.366
3.1416	31416) 200000.000
6.8	188496
251328	115040
188496	94248
21.36288	207920
- 21.363 ft. Ans.	188496
	194240
	188496
	•

7. How much wire will be required to make a hoop 30 inches in diameter, allowing two inches for the joining?

8. How many times would such a hoop turn in going half a mile?

	<b>3</b> 36.
2)5280	94248) 31680000.
2640	282744
2640	340560
12	282744
<del>5280</del>	578160
2640	<b>5</b> 6548 <b>8</b>
31680	<del></del>

9. Cork, whose weight is 0.24 of that of water, weighs 15 pounds per cubic foot. What is the weight of 6 cubic feet of oak, the weight of oak being 0.934 of that of water?

62.5	
24) 1500.0	62.5
144	<b>6</b>
60	375.
48	0.934
$\overline{120}$	1500
120	1125
<b>Contracts</b>	3375
	350.25

10. From what number can 847 be subtracted 307 times, and leave a remainder of 49?

847	
307	
5929	
2541	
260029	
49	
260078	

11. What is the 235th part of 141,235?

	601
235) 1	41235
1	410
_	235
	235

12. What will 343 barrels of flour cost, at \$6.37 a barrel?

\$6.37 343	
1911	
2548	
1911	
<b>\$</b> 2184.91	

13. 12 make a dozen, and 12 dozen make a gross. How many steel pens in 28 gross? What will a gross of eggs cost, at 27 cents a dozen?

14. How much must be added to \$4429 in order to make the sum 43 × \$241?

15. What number deducted from the 26th part of 2262 will leave the 87th part of the same number?

87	<b>26</b>	
26) 2262	87)2262	87
208	174	26
182	522	61
182	522	

16. At an ordinary rate, 123 words a minute, how long will it take a man to deliver a speech of 15 pages, each of 28 lines, and each line containing 11 words? How long would it have taken Daniel Webster to deliver the same speech, at the rate of 93 words a minute?

	37.6	49.7
15	123)4620.0	93)4620.0
28	369	372
120	930	900
30	861	837
420	690	630
11		
420		
420		
4620		

17. How long would it take a railway train to go from New York to San Francisco, 3310 miles, at the rate of 1973 feet a minute?

minute !	. 8858
3310	1973) 17476800
5280	15784
264800	16928
6620	15784
16550	11440
17476800	9865
	15750

18. How long will it take to count a million, at the rate of 67 a minute?

19. If you put into a box 17 cents a day including Sundays, beginning January 1 and ending

July 4, how much money will there be in the box?

31	185
28	0.17
31	1295
<b>3</b> 0	185
31	
30	31.45
4	<b>=</b> \$31.45.
185	

20. If a man's income is \$3000 a year, and his daily expenses average \$7.68, what does he save in a year?

21. In a question of division the quotient was 87.83, the divisor 759. What was the dividend?

22. It is 3.1416 times as far round a wheel as across it. How many times will a wheel 4.5 feet across turn round in going 23 miles of 5280 feet each?

		8590
5280	3.1416	141372) 1214400000
23	4.5	1130976
15840	157080	834240
10560	125664	706860
121440	14.1372	1273800
		1272348
		14520

23. How many gallons of 231 cubic inches are contained in a cubic foot (1728 cubic inches)? in a bushel of 2150.42 cubic inches? How many cubic feet in a bushel? How many bushels in 31.5 gallons?

(i.)		(ii.)
7.48		9.309
<b>231)</b> 1728.00		<b>231)</b> 2150.420
1617		2079
1110		714
924		<b>693</b>
1860		2120
1848		2079
(iii.)		(iv.)
1.244		3.38
1728)2150.420	31.5	215042) 727650.00
1728	231	645126
4224	315	825240
<b>34</b> 56	945	645126
7682	630	1801140
6912	7276.5	1720336

24. Seven children had left to them \$7186 apiece; one died, and his share was divided among the surviving six. How much had each then?

25. What is the nearest number to 7196 that will contain 372 without a remainder?

19	
372) 7196	7196
372	128
3476	7068
3348	
128	

26. How long will it take 2 men to do what 1 man can do in 6 days? what 4 men can do in 3 days? what 3 men can do in 4 days?

6 days 
$$+ 2 = 3$$
 days  
 $2 \times 3$  days  $= 6$  days.  
 $(3 \times 4 \text{ days}) + 2 = 6$  days.

27. Divide \$1.80 among Thomas, Richard, and Henry in such a way that Henry shall receive 3 cents for every 5 cents that Thomas gets, and Richard shall receive 2 cents for every 3 cents that Henry gets.

28. Divide \$87.84 between B and C so that C shall get \$19 as often as B gets \$17.

	2.44
19	36)87.84
17	72
<del></del>	158
	144
	144
	144
<b>\$</b> 2.44	<b>\$</b> 2.44
19	17
2196	1708
244	244
\$46.36 = B's.	\$41.48 = C's.

29. Three partners received for goods: one, \$371.63; the second, \$285.40; the third, \$411.91. They paid for the goods \$879.34, and divided the balance equally among them. How much did each receive?

30. At 12 inches in a foot, how many inches long is a wall 35 feet in length? A brick and its share of mortar being 8.4 inches long, how many bricks in length is the wall?

<b>3</b> 5	50
12	$84)\overline{4200}$
70	420
35	0
420	

31. A brick and mortar being 2.4 inches in height, how many bricks are required to build the wall 12 feet high, if the wall be two bricks wide?

32. What is the total weight of the wall, if a brick and its share of the mortar weigh 4.13 pounds? What is the weight after a long rain, when the weight is increased to 4.27 pounds for each brick?

$$\begin{array}{ccc}
4.13 & 4.27 \\
\underline{6000} & \underline{6000} \\
24780 & 25620
\end{array}$$

33. How many pounds does each foot in length of the wall weigh?

708	732
35)24780	35)25620
245	245
280	112
<b>2</b> 80	105
	70
	70
	<del></del>

34. If 60.98 cubic inches of brick weigh 4 pounds, how many cubic inches of brick weigh 1 pound? How many pounds would a cubic foot (1728 cubic inches) weigh?

35. If a cubic foot of water weigh 62.5 pounds, how many times as heavy as water is brick?

36. Light moves through the air at 186,500 miles in a second. How many times can it go around the earth in a second, the distance round the earth being 24,897.714 miles?

$$\begin{array}{r}
 7.5 \\
 24897714 \overline{\smash{\big)}\ 186500000.0} \\
 \underline{174283998} \\
 \underline{122160020}$$

37. Light moves through the air at 300,190 kilometers in a second. How many times can it go around the earth in a second, the distance round the earth being 40,007.5 kilometers?

38. A minute is 60 seconds. How many miles and how many kilometers can light travel through air in a minute?

39. An hour is 60 minutes. How many miles and how many

kilometers can light travel in an hour?

40. The distance round the earth, given in Ex. 37, is measured on a north and south line. Around the equator the distance is 40,075.45 kilometers. How many times could light move round the equator in one minute?

41. Find the reciprocal of the difference between 31.24 and 31.23768.

	431.034
<b>232</b> ):	100000.000
·	928
•	720
	<b>696</b>
	240
	<b>2</b> 32
	800
	696
	1040
	928

42. The Hanoverian mile is 25,400 Hanoverian feet long, each foot being 0.9542 of an English foot. Find to four places of decimals the fraction that an English mile of 5280 English feet is of a Hanoverian mile.

0.9542

 $\begin{array}{r} 25400 \\ \hline 3816800 \\ 47710 \\ \hline 19084 \\ \hline \hline 24236.6800 \\ \hline 0.2178 \\ 2423668) \overline{528000.0000} \\ 4847336 \\ \hline \hline 4326640 \\ 2423668 \\ \hline \hline 19029720 \\ 16965676 \\ \hline \hline 21640440 \\ 19389444 \\ \hline \end{array}$ 

43. Express in inches the length of a meter, given that a meter is one ten-millionth of a quarter of the earth's circumference, that the circumference is 3.14159 times the diameter, that the diameter is 7911.7 miles, and that a mile is 5280 × 12 inches.

5280 12 10560 5280 63360 7911.7 443520 63360 63360 570240. 443520 501285312. 3.14159 4511567808 2506426560 501285312 2005141248 501285312 1503855936 4)1574832923.32608 393708230.83152 0.0000001 39.370823083152 =39.3708 in. Ans.

44. How must a number be altered to double its reciprocal?

Divided by 2.

45. What effect is produced on the sum of two numbers, if each number is increased by the same number? What effect on the difference?

It is increased by two times the number; not any.

46. What effect is produced on the product of two numbers, if both numbers are multiplied by the same number? What effect on the quotient?

It is multiplied by the square of the number; not any.

47. What effect is produced on the *remainder*, if both divisor and dividend are multiplied by the same number? If both are divided by the same number?

It is multiplied by the number; it is divided by the number.

48. In going from one planet to another light probably moves faster than in air. Suppose it moves at 309,800 kilometers a second, how long would it take light to perform each of the following journeys:

_	_		_							
Moon to Earth	•	•	•	•	•	•	•		375,500	kilometers.
Sun to Earth.	•			•	•	•	•	147,5	250,000	46
Sun to Mercury	•	•	•	•		•	•	56,9	900,000	66
Sun to Venus.	•	•	•	•		•	•	106,4	100,000	66
Sun to Mars .	•	•	•	•	•	•		•	100,000	
Sun to the Astero	ide	3		•	•	•	•	400,0	000,000	66
Sun to Jupiter.	•	•	•	•	•	•	•	765,4	100,000	66
Sun to Saturn.	•	•	•	•	•			•	000,000	
Sun to Uranus.	•	•	•	•	•	•	2	,817,0	000,000	66
Sun to Neptune	*	•	•	•		•	4	,421,0	000,000	44
Sun to the neares	st s	taı	•	•	2	4,0	00,	,000,0	000,000	46
1.21					47	<b>5.3</b>				183.7
3098) 3755.00	3	098	8)1	473	250	0.0			3098)	569000.0
3098			1	23	92				,	3098
6570			_	23	 330					25920
• •				-						
6196				Z1	686	_				24764
3740				1	644	0				11560
<b>30</b> 98				1	<b>54</b> 9	0				9294
					95	00				22660
					92	94				21686

343.4	723.4	1291.1
3098)1064000.0	3090) 2241000.0	3098) 4000000.0
9294	21686	3098
13460	7240	9020
12392	6196	6196
10680	10440	28240
9294	9294	27802
13860	12460	3580
12392	12392	<b>3</b> 098
		4820
		3098
2470.6	4528.7	9092.9
3098)7654000.0	3098)14030000.0	3098) 28170000.0
6196	12392	27882
14580	16380	28800
12392	15490	27882
21880	8900	9180
21686	6196	6196
19400	27040	29840
18588	24784	27882
	22560	
	21686	
14270.5	7	7469335
3098) 44210000.0	3098) 24000	0000000
3098	21686	8
13230	2314	<del>10</del>
12392	2168	36
8380	145	•
6196	123	9294
21840		10860
21686	-	3588 9294
15400		28920 15660
15490	2	27882 15490

49. A kilometer is about 0.6214 of a mile.	How many miles is
each of the planets from the sun?	•

•		
14725	5690	10640
<b>6214</b> .	6214	6214
58900	22760	42560
14725	5690	10640
<b>294</b> 50	11380	21280
88350	34140	63840
Earth, 91,501,150	Mercury, 35,357,660	Venus, 66,116,960
22410		76540
6214		6214
89640		306160
22410		76540
44820	<b>6214</b>	<b>1530</b> 80
134460	40000	<b>4</b> 59240
Mars, 139,255,740	Asteroids, 248,560,000	Jupiter, 475,619,560
140300	281700	442100
6214	6214	6214
561200	1126800	1768400
140300	281700	<b>44</b> 2100
280600	563400	884200
841800	1690200	2652600
Saturn, 871,824,200	Uranus, 1,750,483,800	Neptune, 2,747,209,400

## EXERCISES ON PAGE 73.

1. Convert 5427<sup>m</sup> into kilometers; into millimeters; into centimeters.

 $5427^{m} = 5.427^{km} = 5427000^{mm} = 542700^{cm}$ .

2. 6853<sup>mm</sup> contain how many meters? how many centimeters? what part of a kilometer?

 $6853^{mm} = 6.853^{m} = 685.3^{om} = 0.006853^{km}$ .

3. Write 49.7<sup>m</sup> as centimeters; as millimeters; as part of a kilometer.

$$49.7^{\text{m}} = 4970^{\text{cm}} = 49700^{\text{mm}} = 0.0497^{\text{km}}$$
.

- 4. How many centimeters in  $12.4^{km}$ ? how many millimeters?  $12.4^{km} = 1,240,000^{cm} = 12,400,000^{mm}$ .
- 5. Change 1230 meters into kilometers; into centimeters.  $1230^{m} = 123^{km} = 123,000^{cm}$ .
- 6. Write  $1230^{\text{cm}}$  as meters; as millimeters.  $1230^{\text{cm}} = 12.3^{\text{m}} = 12.300^{\text{mm}}$ .

8.  $0.927^{km} - 6495^{cm}$ ;  $4.37^{cm} - 42.87^{mm}$ .

9.  $8 \times 0.0457$  km;  $3.04 \times 60.93$  cm;  $5.43 \times 67.2$  mm.

		0.0672 <b>-</b>
	0.609 <b>3</b> m	5.43
	3.04	2016
45.7 <sup>m</sup>	24372	2688
8	18279	3360
365.6m	1.852272m	0.364896m

10.  $38,019^{mm} + 0.097$ ;  $0.41^{km} + 25.625$ .

11. At \$1.87 the meter what is the cost of 6.20<sup>m</sup> of cloth?

12. At \$0.75 the meter what is the cost of 60<sup>m</sup> of cloth?

\$0.75 60 \$45.00

13. From a piece of cloth containing 47.60<sup>m</sup> a tailor cuts off three pieces: the first of 3.80<sup>m</sup>, the second of 1.30<sup>m</sup>, and the third of 45<sup>cm</sup>. How much of the cloth is left?

 $3.8^{m}$  1.3 0.45  $\overline{5.55^{m}}$   $47.6^{m}$  5.55  $\overline{42.05^{m}}$ 

14. What is the value of 60cm of cloth, worth \$5.20 a meter?

\$5.20 0.6 \$3.12

15. If \$6.00 are paid for a railroad ticket to travel 440km, what is the fare per kilometer?

$$0.0138 = \$0.014$$

$$440) 6.000$$

$$440$$

$$1600$$

$$1320$$

$$3800$$

$$3520$$

$$280$$

16. If a train run 288km in 9 hours, how many meters does it run in a minute?

60	533.33 <b>=</b>
9	54) 28800.00°
540	270
	180
	162
	180
	162
	180
	162
	180
	162

17. If a man walk at the rate of 6km an hour, what part of an hour will it take to walk 420 meters?

$$6^{\text{km}} = 6000^{\text{m}} \qquad 0.02$$

$$6000)420.00$$

$$42000$$

18. A railroad carried 412 passengers 18 kilometers, and received \$88.992; at the same rate, what will it receive for carrying 350 passengers 35 kilometers?

412	0.012
18	7416) 88.992
3296	7416
412	$\overline{14832}$
7416	14832
350	12250
35	\$0.012
1750	24500
1050	12250
12250	\$147.000

#### Exercises on Pages 75 and 76.

1. Convert 1,854,276qm into hektars; into square kilometers.

 $1,854,276^{qm} = 185.4276^{ha};$ =  $1.854276^{qkm}$ .

- 2. How many hektars in 2.7856 square kilometers?  $2.7856^{qkm} = 278.56^{ha}.$
- 3. Write 1.7431qm as square centimeters; as square millimeters.

 $1.7431^{qm} = 17,431^{qcm}$ ; =  $1,743,100^{qmm}$ .

4. How many square kilometers in 17,467.5 hektars?  $17,467.5^{ha} = 174.675^{qkm}$ .

5. How many square meters in 1.3614qkm?

 $1.3614^{qkm} - 1,361,400^{qm}$ .

6. How many square meters in 2.25 hektars?

 $2.25^{ha} = 22,500^{qm}$ .

7. How many square centimeters in 0.0137 of a square meter?

 $0.0137^{qm} = 137^{qcm}$ .

8. Write 3.571<sup>qcm</sup> as square millimeters.

 $3.571^{\text{qom}} = 357.1^{\text{qmm}}$ .

# Exercises on Page 77.

1. How many cubic centimeters in 2.25<sup>cbm</sup>?

 $2.25^{\text{cbm}} = 2,250,000^{\text{ccm}}$ .

2. How many cubic meters in 2,162,87500m?

 $2,162,875^{\text{com}} = 2.162875^{\text{cbm}}$ .

# Exercises on Page 78.

1. How many liters in 1.7°bm? in 157,854°cm?

 $1.7^{\text{obm}} = 1700^{1};$  $157,854^{\text{com}} = 157.854^{1}.$ 

2. How many cubic centimeters in 9.51? in 0.0151?

 $9.5^1 = 9500^{\text{ocm}}$ ;  $0.015^1 = 15^{\text{ocm}}$ . 3. Change 1.25<sup>hl</sup> to cubic centimeters; to the fraction of a cubic meter.

 $1.25^{\text{hl}} = 125,000^{\text{ocm}}$ ; =  $0.125^{\text{cbm}}$ .

4. Convert 431.881 into hektoliters; into the fraction of a cubic meter.

$$431.88^{1} = 4.3188^{h1}$$
;  
=  $0.43188^{cbm}$ .

5. Write 0.375<sup>cbm</sup> as liters; as cubic centimeters.

$$0.375^{\text{obm}} = 375^{1};$$
  
=  $375,000^{\text{com}}.$ 

6. Write 734,159.651<sup>com</sup> as liters; as hektoliters; as cubic meters.

$$734,159.651^{\text{com}} = 734.159651^{\text{l}};$$
  
=  $7.34159651^{\text{hl}};$   
=  $0.734159651$ 

7. How many meters in 8,573,412.867°° ?

$$8,573,412.867^{\text{com}} = 8.573412867^{\text{cbm}}$$
.

- 8. Change the expression 0.734578912° into cubic centimeters; into liters.
- $0.734578912^{\text{cbm}} = 734,578.912^{\text{ccm}};$ =  $734.578912^{\text{l}}.$
- 9. Change 1731.5 liters into cubic meters; into cubic centimeters.

$$1731.5^{1} = 1.7315^{\text{cbm}};$$
  
= 1,731,500<sup>ccm</sup>.

### Exercises on Page 79.

1. How many kilos in 1.73<sup>t</sup>? in 0.341 of a ton?

$$1.73^{t} = 1730^{kg}$$
;  
 $0.341^{t} = 341^{kg}$ .

- 2. How many kilos will a hektoliter of water weigh?

  100kg.
- 3. Convert 13,756<sup>mg</sup> into grams; into the fraction of a kilo.

$$13,756^{mg} = 13.756^{g}$$
;  
=  $0.013756^{kg}$ .

4. What is the weight in grams of 346.1ccm of water?

5. Give the weight in kilograms of 0.37615<sup>cbm</sup> of water.

376.15<sup>kg</sup>.

- 6. Change 0.6778<sup>kg</sup> into milligrams.
  677,800<sup>mg</sup>.
- 7. How many milligrams in the third part of 17.4 grams?

  5,800<sup>mg</sup>.

#### EXERCISE IV.

1. Add 17.3<sup>m</sup>, 87.41<sup>m</sup>, 271<sup>om</sup>, 380<sup>mm</sup>, and 1.79<sup>m</sup>.

17.3<sup>m</sup>
87.41
2.71
0.38
1.79
109.59<sup>m</sup>

2. What is the sum of \$15.87, \$39.46, \$47.52, \$75.38, \$75.89?

\$15.87 39.46 47.52 75.38 75.89 \$254.12

3. Add 1870m, 49.3m, 317mm, and 6.138m.

1.87<sup>m</sup>
49.3
0.317
6.138
57.625<sup>m</sup>

4. The door-sill being 3<sup>cm</sup> high; the door, 2.34<sup>m</sup>; the finish over it, 13.7<sup>cm</sup>; and the distance from finish to ceiling, 93<sup>cm</sup>: how far from floor to ceiling?

0.03<sup>m</sup>
2.34
0.137
0.93
3.437<sup>m</sup>

5. The distance to the post-office is  $3.31^{km}$ ; thence to the mill,  $1.711^{km}$ ; thence to the store,  $3.718^{km}$ ; thence home,  $2.543^{km}$ . How long is the circuit?

3.31km 1.711 3.718 2.543 11.282km

6. From Portland, Me., to Boston is about 132km; Boston to Albany, 320km; Albany to Buffalo, 480km; Buffalo to Chicago, 800km; Chicago to Omaha, 800km; Omaha to Cheyenne, 780km; how far from Cheyenne to Portland? to Albany? from Boston to Cheyenne?

(1)	(2)
132km	132km
320	320
480	452km
800	
800	3312km
780	452
3312km	2860km
(3)	(4)
320km	3312km
480	132
800	3180km
1600km	

7. If I travel 789.7<sup>km</sup> a day, how far shall I go in 7 days? in 8.5? in 19.6? in 27.8? in 365 days?

789.7km	789.7km	789.7km	789.7km	789.7km
· <b>7</b>	8.5	19.6	27.8	365
5527.9km	39485	47382	63176	39485
	63176	71073	55279	47382
	· 6712.45km	7897	15794	23691
••=	15478.12km	21,953.66km	288,240.5km	

8. How much will 3<sup>m</sup> of cloth cost, at \$1.37 a meter? How much 5.38<sup>m</sup>, at \$2.63 a meter?

9. How much will 13.4 of opium be worth, at \$8.48 a kilo? 28.79 s, at \$7.96 a kilo?

10. A man bought 153 barrels of flour, at \$4.875 a bbl. What did the whole cost him?

11. He gave for it 6 shares of stock, at \$113.50 a share, and the rest in cash. How much money did he pay?

12. He paid \$13.75 for storage; also, 75 cents a barrel for freight. How much do these expenses amount to?

153
<b>\$</b> 0.75
765
1071
\$114.75
13.75
\$128.50

13. It was sold, 49 bbls. at \$6.50 a bbl.; the rest at \$6.25. What were the gross receipts?

<b>\$</b> 6.50	<b>\$</b> 6.25
49	104
5850	2500
<b>2</b> 600	625
\$318.50	\$650.00
153	318.50
49	\$968.50
104	

3.1416

14. He paid for commissions, etc., \$17.50; and counts his loss of interest at \$29.30. What then is his net profit?

15. Find the circumference of a circle having a diameter of 1<sup>m</sup>.

$$\frac{3.1416}{1^{m}}$$
 $\frac{1^{m}}{3.1416^{m}}$ 

3.1416

16. Find the circumferences of circles of which the diameters are respectively 83<sup>m</sup>; 3.71<sup>m</sup>; 32.8<sup>m</sup>; 10.4<sup>cm</sup>; 11.8<sup>cm</sup>; 167.1<sup>mm</sup>; 39.3<sup>mm</sup>. Give each to the nearest tenth of a millimeter.

3.1416

83000m	<b>3710</b>	mm	32800 <sup>mm</sup> •	
94248000	314160		25132800	
<b>2</b> 51328	219912		6 <b>2832</b>	
260752.8mm	94248	94	4248	
	11655.3m		03044.4800 <sup>mm</sup> 03,044.5 <sup>mm</sup> . Ans.	
<b>3.14</b> 16	3.1416	3.1416	3.1416	
104 <sup>mm</sup>	118mm	167.1 <sup>mm</sup>	39.3mm	
125664	251328	31416	91248	
31416	<b>31416</b> ·	219912	282744	
$\overline{326.7264^{\mathbf{mm}}}$	31416	188496	94248	
$= 326.7^{mm}$ . Ans.	370.7088mm	31416	123.46488mm	
	$=370.7^{mm}$ . Ans.	524.96136mm	$= 123.5^{mm}$ . Ans.	
	=	$= 525^{\mathrm{mm}}. Ans.$		

17. What is the length of the earth's orbit, to the nearest meter, if the diameter of the orbit is 294,481,217km?

294481217km

3.1416

1766887302

294481217

1177924868

294481217

883443651

925,142,191.3272km

- 925,142,191,327<sup>m</sup>. Ans.

18. How far round this world, if its diameter is 12,734km?

12734km

3.1416

76404

12734

50936

12734

38202

40,005.1344km. Ans.

19. If a carriage-wheel is 1.31<sup>m</sup> in diameter, what is its circumference? How far will it go, if it roll without slipping, in turning once? 17 times?

(1) 3.1416  $1.31^{m}$  31416 94248 31416  $4.115496^{m}$   $= 4.115^{m}$ . Ans.

(2)  $-4.115^{m}. Ans.$ (3)  $4.115^{m}$  17 28805 4115  $\overline{69.955^{m}}. Ans.$ 

20. How often must that wheel turn in going 69.429<sup>m</sup>? 73.513<sup>m</sup>? 17.27<sup>km</sup>?

21. Find the reciprocal of 3.14159 to the 5th place.

22. What is the diameter of the circle whose circumference is 314.159cm?

314159)31415900 314159

23. What is the diameter of the wheel which revolves 19.5 times in going 107.25<sup>m</sup>?

24. How thick through is a tree which has a girth of 2.97-?

0.31831 2.97<sup>m</sup> 222817 286479 63662 0.9453807<sup>m</sup> = 0.945<sup>m</sup>. Ans.

25. What is the diameter of a circular field two kilometers in circumference?

0.31831 2000 636.62<sup>m</sup>

26. What is the diameter of a rope of which the circumference is 20<sup>cm</sup>?

0.31831 20<sup>cm</sup> 6.3662<sup>cm</sup>

27. In a park is a fountain whose basin is 75<sup>m</sup> in circumference. What is the diameter of the basin?

0.31831 75<sup>m</sup> 159155 222817 23.87325<sup>m</sup> = 23.87<sup>m</sup>. Ans.

## EXERCISE V.

1. Find the area of a rectangle 17 m by 19 m.

19cm 17cm 133 19 323qcm

2. In a rectangular township 16<sup>km</sup> by 7<sup>km</sup>, how many hektars? If there are in it 47.3<sup>km</sup> of highway, averaging 11.7<sup>m</sup> wide, how much land is left for other uses?

47300 <sup>m</sup>	16 <sup>km</sup>
11.7	7km
331100	112qkm
473	100
473	11200ha
553410qm	55.341
$= 55.341^{ha}$	11144.659ha

3. In a rectangular field, 751.3<sup>m</sup> long and 189.3<sup>m</sup> wide, is a straw-berry bed 31.4<sup>m</sup> by 17.8<sup>m</sup>. How many hektars in the field? How many, exclusive of the strawberry bed?

4. If my garden contain 941.65qm, and my neighbor's 748.37qm, what is the area of both in hektars?

5. If a painter can cover 8.786qm in an hour, how much can he cover in 1.78 hours? in 3.86 hours? in 4.57 hours?

8.786qm	8.786 <b>47</b>	8.786qm
1.78	3.86	4.57
70288	52716	61502
61502	70288	<b>43930</b>
8786	<b>2</b> 6358	<b>3</b> 51 <b>44</b>
15.639qm	33.91396qm	40.15202qm
	$= 33.914^{qm}$ . Ans.	=40.152qm. Ans.

6. How many hektars in each of three rectangular fields: one measuring 315.71<sup>m</sup> by 78.91<sup>m</sup>; a second, 293.6<sup>m</sup> by 84.84<sup>m</sup>; the third, 346.8<sup>m</sup> by 71.82<sup>m</sup>. How many in the three?

24912.6761qm = 2.4913ha. Ans.	24909.024qm = $2.4909$ ha, $Ans$ .	24907.176qm = $2.4907$ ha. Ans.	7.4729ha. Ans.
220997	23488	24276	2.4907ha
<b>252568</b>	117 <del>44</del>	3468	2.4909ha
284139	<b>234</b> 88	<b>27744</b>	2.4913ha
31571	11744	6935	
78.91 <b>m</b>	84.84m	71.82 <sup>m</sup>	
315.71 <sup>m</sup>	293.6 <sup>m</sup>	346.8 <sup>m</sup>	

7. Give the price of each field, and of the whole, at \$67.50 a hektar; at \$384 a hektar; and at \$2.375 a square meter.

<b>2.4</b> 913 <b>\$</b> 67.50	2.4909 \$67.50	2.4907 \$67.50		2.4913 \$ 384
1245850	1245450	1245350	<b>\$168.16</b>	99652
174391	174363	174349	168.14	199304
149478	<b>149454</b>	149442	168.12	74739
<b>\$</b> 168.162950	<b>\$</b> 168.135750	\$168.122250	\$504.42	\$956.6592
=\$168.16. Ans. :	=\$168.14. Ans. :	=\$168.12. Ans	, <b>=</b>	=\$956.66 Ans.

8. What is the area of a circle 27cm in diameter? of one which is 1<sup>m</sup> in diameter?

	(1)
27cm	0.7854
27cm	729qcm
189	70686
54	15708
729qcm	54978
•	572.5566qom

(2)  $1^{m} \times 1^{m} \times 0.7854 = 0.7854^{qm}$ 

9. What is the area in hektars of a circular field 784<sup>m</sup> across?

784m	614656qm
784m	0.7854
3136	<b>2458624</b>
6272	3073280
5488	<b>4</b> 917248
614656qm	4302592
	482750.8224qm
	$=48.275^{ha}$ . Ans.

10. Give the area of a circle 31cm in diameter.

31 <b>cm</b>	0.7854
31cm	961 <b>qam</b>
31	<del>7854</del>
93	47124
961 <sup>qcm</sup>	70686
	754 76949cm

11. Find the length of a rectangle 17cm wide, and containing 306cm. What length of carpet 75cm wide is required to make 27cm?

18cm		36 <sup>m</sup>
17)306		75) 2700
17		225
136	•	450
<u>136</u>		<u>450</u>

12. A room is 16<sup>m</sup> long, 8<sup>m</sup> wide, and 8<sup>m</sup> high; another room is 7<sup>m</sup> long, 7<sup>m</sup> wide, and 3<sup>m</sup> high. How many square meters of painting on the walls of both rooms, if no allowance is made for doors and windows? How many more square meters of painting on the walls of the larger room than on those of the smaller?

7 <b>m</b>	. 14 <b>m</b>	16 <sup>m</sup>	24 <sup>m</sup>	384qm	384qm
7	2	8	2	84	84
14m	<del></del>	, 24 <sup>m</sup>	<del></del> 48	468qm. Ans.	300qm. Ans.
	3		8		
	84qm		384qm	•	

13. How many square centimeters of surface on a ball 7cm in diameter?

7 <b>cm</b>	3.1416qcm
7cm	49
499cm	282744
	125664
	153.9384qcm

14. How many square centimeters of surface on a ball 18<sup>cm</sup> in diameter?

18 cm	3.1416
18 <b>cm</b>	324 <b>qcm</b>
144	125664
18	62832
324 qcm	94248
	1017.8784qcm

15. How many square meters of surface on a hemispherical dome 11.27<sup>m</sup> in diameter?

11.27 <sup>m</sup>	$127.0129^{qm}$
11.27	3.1416
7889	7620774
<b>2254</b>	1270129
1127	5080516
1127	1270129
127.0129qm	<b>3</b> 81038 <b>7</b>
	2) 399.02372664
	199.51186332qm
	= 199.5119qm. Ans

16. What is the interior surface of a hemispherical basin 12<sup>cm</sup> in diameter?

17. What is the interior surface of a hemispherical vase 70<sup>cm</sup> in diameter?

18. Find, by this rule, the area of example 9.

	<b>_</b>
2)784	153664qm
392	3.1416
<b>392</b>	921984
784	153664
3528	614656
1176	153664
153664qm	460992
	482750.8224qm
•	$=48.275^{ha}$ . Ans.

19. How many square centimeters are inclosed in a circle struck with a radius of 7<sup>cm</sup>?

3.1416 49qcm 272744 125664 152.9384qcm. Ans. 20. In a sheet of zinc 1.76<sup>m</sup> long and 89<sup>cm</sup> wide are two circular openings, one of which has a radius 10.5<sup>cm</sup>, the other a radius 9.2<sup>cm</sup>. What is the area of the zinc left?

10.5cm	3.1416	9.2cm
10.5cm	110.25qcm	9.2cm
<del></del>	157080	184
105	62832	828
110.25qcm	31416	84.649cm
	31416	32.02
	346.361400qam	
	$-0.03464^{qm}$	
3.1416	$0.02659^{qm}$	1.76m
84.64qcm	0.03464qm	0.89**
125664	0.06123qm	1584
188496		1408
125664		1.5664 <sup>qm</sup>
251328		0.06123qm
$265.905024^{\text{qcm}}$	•	1.50517qm
0.02659 <sup>qm</sup>		$= 1.505^{qm}$ . Ans.

21. What is the area of a circle of which the radius is  $24^{m}$ ?

24 <b>-</b>	3.1416	
24 <b>m</b>	576qm	
<del></del>	188496	
48	219912	
576 <b>9m</b>	157080	
	1809.5616qm	

22. A piece of land in the form of a circle has a radius of  $40^{m}$ ; in the middle of it is a pond forming a circle of  $15^{m}$  radius. What is the total surface? the surface of the pond? the surface of the land to cultivate?

3.1416 1600qm 18849600 31416 5026.56qm, total surface. 706.86qm 4219.7qm, surface of land. 24. How many meters of carpet 56cm wide will be required for a room 8.32m long and 6.6m wide, strips running lengthwise?

$$\begin{array}{r}
11.7 = 12 \text{ strips.} \\
56) 660.0 \\
\underline{56} \\
100 \\
\underline{56} \\
440 \\
\underline{440} \\
392 \\
\underline{48} \\
99.84^{m}
\end{array}$$

25. How many meters of carpet 70cm wide will be required for a room 7m long and 5.4m wide, strips running across the room?

26. How many meters of carpet 80° wide will be required for a room 6<sup>m</sup> long and 5.47<sup>m</sup> wide, strips running across the room?

27. How many meters of carpet 90 wide will be required for

a room 5<sup>m</sup> long and 4.5<sup>m</sup> wide, strips running lengthwise? How much will it cost, at \$1.875 a meter?

28. How many meters of carpet 75<sup>cm</sup> wide will be required for a room 5.25<sup>m</sup> long and 4.75<sup>m</sup> wide, strips running across the room? How much will it cost, at \$2.125 a meter?

29. How many meters of carpet 75<sup>cm</sup> wide will be required for a room 5.6<sup>m</sup> square? How wide a strip will have to be turned

under? How much will the carpet cost, at \$1.25 a meter?

7.4 = 8 strips.	5.6m
75) 560.0	8
525	44.8 <sup>m</sup>
350	<b>\$</b> 1.25
300	2240
	896
75cm	448
35cm	<b>\$</b> 56.00
40cm to turn und	der.

31. How many rolls of paper 45<sup>cm</sup> wide and 8<sup>m</sup> long, allowing 11.19<sup>qm</sup> for doors and windows, will be required to paper a room whose length is 6.12<sup>m</sup>, breadth 5.05<sup>m</sup>, and height 3.5<sup>m</sup>?

$$\begin{array}{r}
 18.6 = 19 \text{ rolls.} \\
 \hline
 36)670.0 \\
 \hline
 36 \\
 \hline
 310 \\
 288 \\
 \hline
 220 \\
 216 \\
 \end{array}$$

32. Find the cost of papering a room 8<sup>m</sup> long, 5.5<sup>m</sup> wide, and 4.5<sup>m</sup> high, with paper 50<sup>cm</sup> wide and 7.5<sup>m</sup> in a roll, at \$1.25 a

roll, put on? There is a base-board 25<sup>cm</sup> wide running round the room, and an allowance of 11<sup>qm</sup> is made for doors and windows.

27 <b>m</b>
$0.25^{m}$
135
<b>54</b>
6.75qm
11
17.75 <sup>qm</sup>
7.5 <sup>m</sup>
.5 <b>m</b>
3.75qm

33. Find the cost of plastering this room, at \$0.50 a square meter.

34. Find the cost of papering a room 5.5<sup>th</sup> long, 4.8<sup>th</sup> wide, and 3.2<sup>th</sup> high, with paper 45<sup>th</sup> wide, 7.5<sup>th</sup> in a roll, at \$0.875 a roll, put on, allowing 12<sup>th</sup> for base-board, doors, etc.

		15.9 - 16	rolls.
6.5m	75**	8375) 539200	\$0.875
4.8m	0.45	3375	16
10.3	375	20170	5250
2	300	16875	875
20.6	3.375	32960	\$14.00
3.2		80375	
412			
618			
65.92			

dastering this room, at \$0.45 a square meter.

26.40 <sup>qm</sup> , ceiling.	80.32
53.92, walls,	\$0.45
80.32	40160
	AS D
ng.	\$36.14

papering a room 6<sup>m</sup> square and 3.5<sup>m</sup> high, 1 7.5<sup>m</sup> in a roll, at \$0.75 a roll, put on; and t 5 cents per running meter.

$$24.8 = 25 \text{ rolls.}$$

21.0 — 20	, tornet	
3375) 84000.0		25
6750		\$0.75
10500		105
16500		125
13500		175
30000	24	\$18.75
27000	\$0.06	1.20
	\$1.20	\$19.95

37. Find the cost of plastering this room, at \$0.36 a square meter.

$6^{\mathbf{m}}$	120 <sup>qm</sup>	
<b>6</b> m	<b>\$</b> 0.36	
36qm, ceiling.	720	
84qm, walls.	360	
120qm	<b>\$43.20</b>	

38. Find the cost of papering a room 13<sup>m</sup> long, 12<sup>m</sup> wide, and 7<sup>m</sup> high, with paper 45<sup>cm</sup> wide and 7.5<sup>m</sup> in a roll, at \$1.50 a roll, put on; and of putting on a border, at \$0.30 a running meter, allowing 15<sup>cm</sup> for base-boards, doors, etc.

13m	7.5 <sup>m</sup>	,		
12 <sup>tm</sup>	0.45 <sup>m</sup>		69.9 = 70	rolls.
25m	375	3	375) 235000.0	
2	300		20230	
50m	3.375qm	L	33700	\$1.50
7 <del>m</del>			30375	70
350qm		<b>\$</b> 0.30	33250	\$105.00
115qm, allow	wance.	50	30375	15.
235qm		<b>\$</b> 15.00		\$120.00

39. Find the cost of plastering this room, at \$0.60 a square meter.

40. How many meters, board measure, in a board 8<sup>m</sup> long and 20<sup>cm</sup> wide?

$$\frac{8^{m}}{0.2^{m}}$$

$$\frac{1.6^{qm}}{1}$$

41. How many meters, board measure, in a joist 5<sup>m</sup> long, 25<sup>cm</sup> wide, and 75<sup>mm</sup> thick?

42. How many meters, board measure, in a stick of timber 15<sup>m</sup> long and 40<sup>cm</sup> square?

	16	
15	25)400	16
0.4	25	6
6.0	150	96
	150	
	-	

43. How many meters, board measure, in 2 joists 5<sup>m</sup> long, 27.5<sup>cm</sup> wide, and 50<sup>mm</sup> thick?

44. How many meters, board measure, in 10 planks, each 4<sup>m</sup> long, 45<sup>cm</sup> wide, and 10<sup>cm</sup> thick? and what is the value of these planks, at \$25 a hundred meters?

45. How many meters, board measure, in 25 box boards, each 4<sup>m</sup> long, 42<sup>cm</sup> wide, and 20<sup>mm</sup> thick? and what is their value, at \$14 a hundred meters?

46. Find the cost of 10 joists 4.5<sup>m</sup> long, 10<sup>cm</sup> wide, and 7.5<sup>cm</sup> thick, at \$11 a hundred meters.

47. Find the cost of 36 planks, each 4<sup>m</sup> long, 27.8<sup>cm</sup> wide, and 75<sup>mm</sup> thick, at \$16 a hundred meters.

48. Find the cost of 3 sticks of timber, each 8<sup>m</sup> long, 22.5<sup>cm</sup> wide, and 20<sup>cm</sup> thick, at \$17.50 a hundred meters.

$0.225^{m}$	8	43.2qm
8 <b>m</b>	25) 200	<b>\$</b> 0.175
1.8qm	200	2160
8		<b>3</b> 02 <b>4</b>
14.4qm		432
3		7.56
43.2qm		

49. Find the cost of a board 8.25<sup>m</sup> long, 28<sup>cm</sup> wide at one end and 35<sup>cm</sup> at the other, and 31.25<sup>mm</sup> thick, at \$0.30 a meter.

$$0.28^{m}$$
 $2.59875^{qm}$  $0.35^{m}$  $1.25$  $2)0.63^{m}$  $1299375$  $0.315^{m}$  $519750$  $8.25$  $259875$  $1575$  $3.2484375$  $630$  $$0.30$  $2520$  $$0.974531250$  $2.59875^{qm}$  $=$ \$0.97.

50. Find the cost of a stick of timber 10<sup>m</sup> long, 25<sup>cm</sup> thick, 30<sup>cm</sup> wide at one end and 25<sup>cm</sup> wide at the other, at \$14 a hundred meters.

0.30=	10	27.5qm
$0.25^{m}$	25)250	<b>\$</b> 0.14
$2)0.55^{m}$	25	1100
$0.275^{m}$	<u> </u>	275
10 <sup>m</sup>		<b>\$</b> 3.85
2.75qm		•
10		
27.5qm		

51. Find the cost of the flooring for a two-story building 16<sup>m</sup> by 10.5<sup>m</sup>; the flooring being 32<sup>mm</sup> thick, and worth \$30 a hundred meters.

52. Find the cost of the flooring timbers for this building, the timbers being 25<sup>cm</sup> by 50<sup>mm</sup>, and placed on edge 30<sup>cm</sup> apart, and worth \$11.50 a hundred meters.

53. Find the cost of the fencing to enclose a field 150<sup>m</sup> long and 75<sup>m</sup> wide; the posts are set 2.5<sup>m</sup> apart, and cost \$0.25 apiece; the fence is 5 boards high; the bottom board is 30<sup>cm</sup>, the top board 25<sup>cm</sup>, and the other three each 22.5<sup>cm</sup> wide, and the boards cost \$13.25 a hundred meters.

<b>30</b>	150 <sup>m</sup>	$122.5^{m}$
25	<b>75</b> m	450 <sup>m</sup>
67.5	225qm	61250
122.5	2	4900
	450qm	551.25qm
		<b>\$</b> 0.1325
		275625
180	180 posts.	110250
<b>\$</b> 0. <b>25</b>	<b>2</b> 5) <b>4</b> 500	165375
900	25	55125
<b>3</b> 60	200	<b>\$</b> 73.04
<b>\$</b> 45.	200	45
•	<u>-</u>	\$118.04

# EXERCISE VI.

1. How many cubic centimeters in a block 9<sup>cm</sup> long by 7<sup>cm</sup> wide, and 6<sup>cm</sup> deep?

9am	63 <b>qcm</b>
70m	6cm
63qcm	378ccm

2. If wood is cut into 120cm lengths, and a pile is 43.7m long and 1.4m high, how many sters of wood are there in it?

43.7m	52.44qm
$1.2^{m}$	1.4 <sup>m</sup>
874	20976
437	<b>5244</b>
52.44qm	73.416s

3. In a grain elevator is a bin 11.2<sup>m</sup> long, 4.34<sup>m</sup> wide, and 2.83<sup>m</sup> deep. How many hektoliters of grain will it hold?

11.2 <sup>m</sup>	48.608qm
4.34m	2.83m
448	145824
<b>336</b>	<b>388864</b>
448	97216
48.608qm	137.56064cbm
	= 1375.6064hl.

4. If a liter of grain weigh 0.81 of the weight of a liter of water, how much will the grain in that bin weigh?

$$1375.6064^{hi}$$

$$= 137560.64^{kg}$$

$$0.81$$

$$\overline{13756064}$$

$$110048512$$

$$\overline{111,424.1184^{kg}}$$

5. A bin measuring 16<sup>m</sup> by 9.7<sup>m</sup>, and 2.8<sup>m</sup> deep, is full of oats, worth \$0.98 a hektoliter. What is the whole worth?

16 <sup>m</sup>	4345.6 <sup>M</sup>
9.7m	<b>\$</b> 0.98
112	347648
144	391104
155.2 <sup>qm</sup>	<b>\$4258.688</b>
2.8m	=\$4258.69. Ans.
12416	
3104	
434.56cbm	
=4345.6 <sup>hl</sup> .	

6. A vat 197cm long, 87cm wide, and 63cm deep, holds how many liters? What would be the weight of water required to fill it?

197cm 87cm	17139qom 63cm
1379	51417
1576	102834
17139qcm	1079757°°m
	$= 1079.757^{1}$
	=1079.757kg.

7. Add 1341<sup>com</sup>, 231<sup>1</sup>, and 2.13<sup>hl</sup>, and give the sum in terms of each of the three units.

$$\begin{array}{r}
 1341^{\text{com}} \\
 231^{\text{l}} = 231000^{\text{com}} \\
 2.13^{\text{hl}} = 213000^{\text{com}} \\
 \hline
 445341^{\text{com}} \\
 = 4.45341^{\text{hl}}.
 \end{array}$$

8. If a spring pours out 467.81 each minute, how many hektoliters will it deliver in 60 minutes? in 37 minutes? in 78 minutes?

9. If 67.31 of oil in a vat with perpendicular sides fill it to a depth of 173mm, how deep will 13.7 times that quantity fill it? and how many hektoliters will there be?

$$\begin{array}{rcl}
173^{\text{mm}} & 67.3^{1} \\
13.7 & = 0.673^{\text{hl}} \\
\hline
1211 & \frac{13.7}{4711} \\
519 & 4711 \\
\underline{173} & 2019 \\
\underline{2370.1^{\text{mm}}} & 673 \\
\underline{= 2.3701^{\text{m}}} & 9.2201^{\text{hl}}
\end{array}$$

10. Into a round cup 10cm across, with perpendicular sides, pour oil until it is 1cm deep; then there are 78.54ccm of oil in the cup. How many cubic centimeters will there be when the oil is 38mm deep?

38mm	78.54 ···
<b>= 3.8</b> cm	3.8cm
	62832
	23562
	298.452°°

11. What is the capacity of a

tin cup 95 <sup>mm</sup> ac	cross and 11.08cm
deep?	
$95^{min} - 9.5^{ma}$	0.7854
9.5cm	90.25qcm
475	39270
855	15708
90.25qcm	70686
	70.88235qcm
	11.08cm
	56705880
	7088235
	7088235
	785.3764380ccm
=	$= 0.785^{1}$ . Ans.

12. What are the capacities of two cylindrical vessels, one being 16.24 across and 19.95 deep, the other 75.4 across and 87.9 deep?

16.24cm	4132.433com	75.4mm
16.24cm	$=4.132^{1}$	75.4 <sup>mm</sup>
6496		3016
3248		3770
.9744		5278
1624		5685.16qmm
263.7376qcm		0.7854
0.7854		2274064
10549504		2842580
13186880		<b>4</b> 5481 <b>28</b>
21099008		3979612
18461632		4465.124664qmm
207.1395	-	= 4465.125qmm
19.95cm		87.9mm
10356975		40196125
18642555	•	31255875
18642555	3	5721000
2071395	39	92485.4875cmm
4132.433025°CC		.392 <sup>1</sup> .

13. How many cubic centimeters in a ball 10cm in diameter? How much less if you take the more exact multiplier?

10cm	0.5236
10cm	1000000
100 qcm	523.6cm
10cm	
1000ccm	
6)	3.1415927
-	0.5235988
	1000
	523.5988 <sup>00m</sup>
	523.600m
	523.5988°CM
	0.0012°cm

14. Into a cubical box 20cm on a side, and full of water, an iron ball 20cm in diameter is gently lowered until it touches bottom. How much water is left in the box? Answer in liters and in cubic centimeters.

20cm 20cm	0.5236 <b>8000ccm</b>
400qcm	4188.8cm
20	
8000ccm	
4188.8ccm	
3811.2ccm	
3.8112 <sup>1</sup> .	

15. One cask contains 171.41

73:81; while a square vat, 137cm each way, is filled to a depth of 69om. How much oil in all the vessels? in liters and in hektoliters.

137cm 137cm	18769qcm 69cm
959	168921
411	112614
137	1295061 ccm
18769qcm	$= 1295.061^{1}$ .

171.4 209.31 73.81 1295.061<sup>1</sup> 1749.5611 -17.49561<sup>hl</sup>.

16. How many liters of air in a room 7.8m long, 6.23m wide, and 3<sup>m</sup> high?

17. If a person's breathing spoils the air at the rate of 0.2175cbm a minute, how long of oil; another, 209.31; a third, | will it take 3 persons sitting

in the room, closed, to spoil the air?  0.2175  3	18. How lon rate, would the s long, 16 <sup>m</sup> wide, a an audience of 2	and 7= high, last
0.6525 6525)1457820.00 13050	22= 16= 132 22	2175 280 174000 4350
15282 13050 22320 19575	3524= 7= 2464*=	60.9000
27450 26100	40.5 609) 24640.0 2436	

19. How many cubic meters of wood in a round stick of equal size throughout, 37cm in diameter and 8.4m long?

370	0.7854	0.10752126
37 <b>0</b>	1369 <del>***</del>	8.4=
259	70686	43008504
111	47124	86017008
1369***	23562 7854	0.903178584*** - 0.9032***.
	1075.2126	
	<b>- 0.10752126•■</b> .	

### EXERCISE VII.

at is the weight, in kalograms, of a hektoliter of water? of a cubic meter of water? of a cubic centimeter?

$$1^{ht} = 100^{kg}$$
 $73.8^1 = 73.8^{kg}$ 
 $1^{obst} = 1000^{kg}$ 
 $1^{cost} = 0.001^{kg}$ 

2. If a man buys half a ton of potatoes for \$20, and retails them all, without waste, at 5 cents a kilogram, what profit does he make on the whole?

3. What is the weight of water required to fill a vat 98cm long, 71cm wide, and 38cm deep?

98cm	6958 <b>qcm</b>
71cm	38
98	<b>5</b> 566 <b>4</b>
686	20874
6958qcm	264.404ccm
	=264.404kg.

4. If the vat of the last example were filled with brine weighing 1.04ks to the liter, what would be the weight of the brine?

5. If the vat of Example 3 were filled with wine weighing 0.981 to the liter, what would be its weight?

6. What is the total weight of 13 men averaging 73.48 each?

7. How many kilograms, and how many tons, would 3.6175 observed of brick weigh, at 2 tons to a cubic meter? at 2.34 tons?

3.6175	3.6175
2 <sup>t</sup>	2.34
7.235	144700
=7235ks	108525
	72350
	8.46495
	=8464.95kg

8. From a barrel containing 67ks of granulated sugar were taken three parcels of 2.75ks each, and four parcels of 7.50ks each. How much is left in the barrel?

30.0%s	24
8.25	325)7800
38.25×s	650
Otto	1300
67ks	1300
38.25	1
09.75he	10. A mass of 21 8

9. Into how many pills of 325=s each can a mass of 78s be divided?

10. A mass of 21 8s is divided into 60 pills. What is the weight of each pill?

6) 2180.000ms 363.333ms

#### EXERCISE VIII.

1. If a stone weighs 1.3<sup>kg</sup> in air and 0.68<sup>kg</sup> in water, and the stone and a block of wood together weigh 1.55<sup>kg</sup> in air and 0.63<sup>kg</sup> in water, what is the specific gravity of the block of wood?

 $1.55^{kg} - 1.3^{kg} = 0.25^{kg}$ , the weight of the wood in the air

 $1.55^{kg} - 0.63^{kg} = 0.92^{kg}$ , the weight of water displaced by the stone and the wood.

 $1.3^{kg} = 0.68^{kg} = 0.62^{kg}$ , the weight of water displaced by the stone alone.

Therefore  $0.92^{kg} = 0.62^{kg} = 0.3^{kg}$ , the weight of water displaced by the wood.

And  $0.25 \pm 0.3 = 0.833$ , the specific gravity of the wood.

What is the weight of 8.17<sup>hl</sup> of alcohol, specific gravity 0.83?

ist will 97 alcohol weigh, of specific gravity 0.817? of specify 0.819? of specific gravity 0.823? 0.838? 0.847?

0.819	0.823	0.838	0.847
974	9754	97**	97**
<del>57</del> 33	5761	5866	5929
7371	7407	7542	7623
79 443**	79.831ks	81.286ks	82.159ks

4. A bar of aluminum 113<sup>mm</sup> long, 17<sup>mm</sup> wide, and 13<sup>mm</sup> thick, is said to be of specific gravity 2.57. What does it weigh? If it really is of specific gravity 2.67, what does it weigh?

113 <sup>mm</sup>	1921qmm	24.973	24.973
17mm	13 <sup>mm</sup>	2.57	2.67
791	<del>5763</del>	174811	174811
113	1921	124865	149838
1921qmm	24973cmm	49946	49946
	=24.973 ccm	64.18	66.67791
	= 24.973		<b>-</b> 66.68€

5. What would be the specific gravity of the bar of the last example if it weighed 65.1375?

6. What is the weight of a bar of aluminum 371<sup>mm</sup> by 63<sup>mm</sup> by 84<sup>mm</sup>, specific gravity being 2.63?

371 <sup>mm</sup>	1963332cmm
63 <sup>mm</sup>	weigh
1113	$1.963332^{\mathrm{kg}}$
2226	2.63
23373qmm	5889996
84	11779992
93492	3926664
186984	5.16356316ks
1963332cmm	=5.1636kg

7. An irregular mass of copper, gently lowered into a pail brimful of water, caused 1.3741 to run over. What did it weigh if of specific gravity 8.91? if 8.89?

1.374**	1.374 kg
8.91	8.89
1374	12366
12366	10992
10992	10992
12.242kg	12.21486 kg
	-12.215ks

8. What was the specific gravity of that copper if the mass weighed 12.3016 ?

9. A plate of iron 137 long, 64.3 wide, and 4.31 thick, weighs 277.54 What is its specific gravity? What would the same mass weigh at specific gravity 7.47? at 7.79?

8809.1 ee
4.31
88091
264273
352364
37967,221 **** - 37.97 <sup>1</sup> .

.967221<sup>1</sup>≈ 7.79 704989 70547 10547 1465159<sup>3</sup>≈ 10. What is the specific gravity of sea-water when a hektoliter weighs 102.5845? what when 31 weigh 30775?

11. What is the specific gravity of a substance of which 7.3 weighs 31.5 ?

12. If a cubic meter of sand weighs 1723\*s, what is its specific gravity? If 3.400m of gravel weigh 7.134 tons, what is the specific gravity?

13. If a cubic centimeter of metal weighs 7.3s, what is its specific gravity?

$$1)7.3$$
 $7.3$ 

14. What is the specific gravity of a fluid weighing 2.317<sup>kg</sup> to a liter?

15. If a body weigh 3.71kg in air and 2.38kg in water, what is its specific gravity?

16. A piece of ore weighing 3.77<sup>kg</sup> weighs in water only 2.53<sup>kg</sup>. What is its specific gravity?

$$\begin{array}{r}
3 77 \\
2.53 \\
\hline
1.24 \\
\hline
3.04 \\
\hline
124)377.00 \\
372 \\
\hline
500 \\
496
\end{array}$$

17. How many cubic centimeters in a stone which loses

17.8s of its weight when weighed in water? What is its specific gravity if weighed in air it weighs 33.7s?

18. In a wrought-iron bottle I find 2.63¹ of quicksilver, weighing 35.81½; in another 2.59¹, weighing 35.193½; in a third, 2.617¹, weighing 35.571½. What is the specific gravity of each? What would be the specific gravity if the three were emptied into one vessel and mixed?

$$\begin{array}{r}
 13.616 \\
 263 \overline{\smash)3581.000} \\
 \underline{263} \\
 951 \\
 789 \\
 \overline{1620} \\
 \underline{1578} \\
 \underline{420} \\
 \underline{263} \\
 \overline{1570} \\
 1578
\end{array}$$

13.588 259)3519 300 259 329 3)40.796 13.59867 -13.59867 -13.599, Ane.  19. A plate of iron 89em by 17em by 7em weighs 79.43es. What is its specific gravity?  13.592 2817)35571 000 2617 9401 7851 15500 13085 24150 23553 5970 5234		
259  929  777  1520  1295  2250  2054,  1960  19. A plate of iron 89cm by 17cm weighs 79.43ks. What is its specific gravity?  13.592  2617)35571 000  2617  9401  7851  15500  13085  24150  23553  5970  5924	13.588	
3)40.796 777 1520 1295 2250 2054, 1960 2064 17° by 7° weighs 79.43° What is its specific gravity?  13.592 2617 9401 7851 15500 13085 24150 23553 5970 5970 5924	259)3519.300	
13.59867  1520  1295  2250  2054,  19. A plate of iron 89° by 17° weighs 79.43° what is its specific gravity?  13.592  2617)35671 000  2617  9401  7851  15500  13085  24150  23553  5970  5970  5970  74137	259	13 592
1520 1295  2250 2054, 1980 17° by 7° weighs 79.43° What is its specific gravity?  13.592 2617  9401 7851 15500 13085 24150 23553 5970 5970  10591)79430.0 74137	929	3)40.796
1295 2250 2054, 1960 17° by 7° weighs 79.43%. What is its specific gravity?  13.592 2817)35571 000 2817 9401 7851 15500 13085 24150 23553 5970 5970 74137	777	13.59867
2250 2054, 1960 1960 2064 13.592 13.592 2817)35571 000 2817 9401 7851 15500 13085 24150 23553 5970 5924	•	- 13.599, Ane.
2054, 1960 170m by 70m weighs 79.43%. What is its specific gravity?  13.592 2817)35571 000 2817 9401 7851 15500 13085 24150 23553 5970 5924	1295	}
1960 2064  170m by 7cm weighs 79.43 s. What is its specific gravity?  13.592 2817)35571 000 2617  9401 7851 15500 13085  24150 23553 5970 5970 5924	2250	
1960 2064  13.592  2817)35571 000  2817  9401 7851 15500 13085  24150 23553 5970 5970 5924	2054 、	19. A plate of iron 89cm by
2054  13.592  2817)35571 000  2817  9401  7851  15500  13085  24150  23553  5970  5970  5934	1960	
13.592 2817)35571 000 2817  9401 7851 15500 13085  24150 23553 5970 5970 5924		, ,
13.592 2817)35571 000 2817  9401 7851 15500 13085  24150 23553 5970 5970 5924	_	89em
2617)35571 000  2617  9401  7851  15500  13085  24150  23553  5970  5970  5924	13.592	
2617 9401 7851 15500 13085  24150 23553 5970 5924	2617)35571 000	
9401 7851 700 15500 13085  24150 23553 5970 74137	*	
7851 15500 13085 24150 23553 5970 5924	0403	89
15500 13085 24150 23553 5970 5970 74187		1513qcm
13085 24150 23553 5970 5934 10591 7.5 10591 7.5 7.5 74137	7801	7cm
13085 24150 23553 5970 5934 7.5 10591)79430.0 74187	15500	10591***
23553 5970 5934 10591)79430.0 74187	13085	10001
23553 5970 5934 10591)79430.0 74137	24150	7.5
5970 74137	23553	
E934	5970	-
52930		
		1 52930

# EXERCISE IX.

se men eat 8ts a week, how much would one man eat at te? How much would seven men? At the same rate, lo the three men eat in one day? and how much each he same rate, how much would seven men eat each day? in five weeks?

2.67	7)8.00	3 <u>)1.14</u>	0.38	2.67	18.67
7	1.14 <sup>kg</sup>	0.38	8	7	5
1.67ks			2.67**	18.67₺	93,33**

2. At the same rate, how much would 17 men eat in 3 weeks and 4 days?

3. If one hektoliter of oats is enough for 5 horses 1 week, how much is enough for 1 horse 1 weeks? for 1 horses 17 weeks?

$$5)1.0 201 7$$

$$1401$$

$$17 187$$

$$11 201$$

$$17 37401$$

$$17$$

4. If two hektoliters of grain are enough for 3 horses 5 days,

how much is enough for 3 horses 1 day? for 1 horse 1 day? for 7 horses 6 days?

$$\begin{array}{r}
3 & 5)2.0 \\
5 & 0.4^{\text{hi}} = 40^{\text{h}} \\
3)15 \\
5 & & & \\
3)40 \\
\hline
13.33 \\
42 \\
\hline
2666 \\
5332 \\
\hline
559.86^{\text{l}} = 560^{\text{l}}
\end{array}$$

5. Mix 17 liters of vinegar, costing 6 cents a liter, with 39<sup>1</sup> at 5 cents, 21<sup>1</sup> at 7 cents, and 13<sup>1</sup> of water costing nothing. Find the amount of the mixture, and its cost.

6. For how much a liter must I sell that mixture, in order to gain 96 cents? for how much to clear \$1.41?

\$4.44	\$0.06
0,96	90)\$5.40
\$5.40	<u>540</u>
\$4.44	\$0.065
1.41	90)5.850
\$5.85	540
•	450
	450

7. A grocer sold 421 kegs of butter for \$4995.25; 56 kegs brought \$12.50 a keg, 91 brought \$11.75 a keg; and 100 kegs brought \$12.25 a keg. For how much a keg were the other kegs sold?

4995.25

2994.25

 If 3 tons of coal cost \$15.75, how many tons will \$36.75 buy?

9. If 5= of cloth cost \$18.75, what should 7= cost?

10. If a tap running 3.5 a minute fills a tub in 16 minutes, how long should a tap delivering 5 a minute be in filling the same tub?

11. If both taps of the last example be opened at once, how soon will they fill the tub?

12. If 3 men can dig 378<sup>m</sup> of ditch in 2 days, how long will it take 5 men, at the same rate, to dig 787<sup>m</sup>?

13. Into a tub which will hold 481, one tap is delivering water at the rate of 3.71 a minute; while out of it, by another tap, the water is running at 2.51 a minute. How long will it take to fill the tub, beginning with it empty?

14. A tap discharges into a tub 4.21 a minute; from the tub water is also running, by a second tap; the water in the tub

gains 301 in 18 minutes. How fast is the second tap discharging?

15. If a wheel is 1.2<sup>m</sup> across, how often will it turn in going one kilometer?

$$3.1416$$
  $265$ 
 $1.2^{m}$   $377)100000$ 
 $62832$   $754$ 
 $31416$   $2460$ 
 $3.76992^{m}$   $2262$ 
 $= 3.77^{m}$   $1980$ 
 $= 0.00377^{km}$   $1885$ 

16. How many times in a minute does the wheel of the last example turn, when the carriage is driven 14km an hour?

$$\begin{array}{r}
 265 \\
 \hline
 0.23 \\
 \hline
 795 \\
 \hline
 530 \\
 \hline
 60.95 \\
 \hline
 -61 \text{ times.}
 \end{array}$$

17. What is the weight of the water in a tank if it would take a flow of 8.71 a minute 1 hour and 38 minutes to empty it?

18. Replace the bulk of water with oil worth \$18.75 a hektoliter, and what will the contents of the tank be worth?

## EXERCISE X.

1. A train leaves Paris at 11 o'clock A.M., and reaches Lyons at 10 o'clock P.M. How many meters does it travel in a hour, the distance from Paris to Lyons being 512.7km?

There are 11 hours between 11 A.M. and 10 P.M. Therefore the train runs  $512.7^{km} + 11 = 46.609^{km} = 46,609^{m}$ .

2. A railroad has a single track 11.450km long. How many rails 4.569m in length did it require to lay the track?

There are two lines of rails. Therefore length of rails is  $2 \times 11.450^{\text{km}} = 22.900^{\text{km}} = 22.900^{\text{m}}$ . Therefore the number of rails is  $22.900 \div 4.569$ .

.. number of rails required was 5013. Ans.

3. A book is 2.1cm in thickness; each leaf is 0.05mm thick. Find the number of pages in the book.

The number of leaves is 21 + 0.05 = 420. The number of pages is  $2 \times 420 = 840$ .

4. The cost of opening a canal amounts to \$25,400 a kilometer. How much would a canal cost which was 113.253km long?

If it cost \$25,400 to open  $1^{km}$ , to open 113.253 it will cost  $113.253 \times $25,400$ .

113.253 \$ 25400 45301200 566265 226506 \$ 2,876,626.200

5. The expense of laying out a paved road is \$12,500 a kilometer. How much would a road cost which was 72.053km long?

If it cost \$12,500 to lay out  $1^{km}$ , to lay out  $72.053^{km}$  it will cost  $72.053 \times $12,500$ .

 $72.053 \\ \$ 12500 \\ \hline 36026500 \\ 144106 \\ 72053 \\ \hline \$ 900,662.50$ 

6. The cost of building a railroad is about \$78,000 a kilometer in France, and only \$25,000 in the United States. How much would it cost in each country to make a road 295.671 ln long?

If it cost \$78,000 to build  $1^{km}$ , to build  $295.671^{km}$  it will cost  $295.671 \times $78,000 = $23,062,338$ . If it cost \$25,000 to build  $1^{km}$ , to build  $295.671^{km}$  it will cost  $295.671 \times $25,000 = $7,391,775$ .

295.671 \$78000 2365368000 2069697 \$23,062,338.000 4)29567100 \$7,391,775 7. If you must go up 211 steps to reach the top of a tower, and each step is 195<sup>mm</sup> high, what is the height of the tower?

$$195^{mm} - 0.195^{m}$$
.

If one step is  $0.195^m$  high, 211 steps are  $211 \times 0.195^m$  high.

8. A house has 5 stories, each story has 19 stairs, each stair is 16cm in height. Calculate how high the floor of the fifth story is from the ground.

$$16^{\text{cm}} = 0.16^{\text{m}}$$
.

If one step is  $0.16^m$  high, 19 steps are  $19 \times 0.16^m = 3.04^m$ , and 4 flights of 19 steps are  $4 \times 3.04^m = 12.16^m$ .

9. A ream of paper contains 20 quires, each quire has 24 sheets, the ream is 13.5cm in thickness. Find the thickness of each sheet.

In one ream there are  $20 \times 24 = 480$  sheets. If 480 sheets are  $13.5^{\text{cm}}$  thick,  $13.5^{\text{cm}} + 480 = 0.028^{\text{cm}}$ , thickness of one sheet.

10. The equator on a terrestrial globe measures  $0.80^{m}$  in circumference. By the aid of a tape-measure we find that the distance between two cities on this globe is  $0.046^{m}$ . What is really the distance in kilometers between the two cities? (The earth's equator is  $40,075.45^{km}$ .)

The ratio of distance on globe between the two cities to the equator is  $0.046^{m} + 0.80^{m} = 0.0575$ . Therefore the actual distance between the two cities is  $0.0575 \times 40,075.45^{km} = 2304.338^{km}$ .

8)0.4600	40075.45km
0.0575	0.0575
	$\overline{20037725}$
	28052815
	20037725
	2304.338km

11. Upon a military map we find that the distance from Paris to St. Denis is 78<sup>mm</sup>. What is the distance in kilometers from Paris to St. Denis? The map is made on the scale of 1 to 80,000<sup>m</sup>; that is, 1<sup>m</sup> on the map represents 80,000<sup>m</sup> of actual measurement upon the ground.

The actual distance is 80,000 times the distance on the map; that is,  $80,000 \times 78^{mm} = 6,240,000^{mm} = 6.24^{km}$ .

12. Give the number of revolutions made by the wheels of a carriage in travelling 82km. The wheels are 1354mm in diameter.

 $82^{km} = 82,000,000^{mm}$ .

The circumference of the wheels is  $3.1416 \times 1354^{mm} = 4253.7264^{mm}$ . The number of revolutions is the total distance divided by the circumference of the wheel, or  $82,000,000^{mm} + 4253.7264^{mm} = 19,277$  times.

3.1416	19277
. 1354mm	42537264)820000000000
125664	42537264
157080	394627360
94248	<b>3</b> 82835376
31416	117919840
	85074528
4253.7264 <sup>mm</sup>	328453120
	297760848
	306922720
	297760848
	<del></del>

13. How many hektars in a square kilometer? how many are? how many square meters?

1 show = 100ha, = 10000a, = 1000000am.

14. France has about 542,000. Hew many hektars does # measure?

$$1^{\text{qkm}} = 100^{\text{he}}.$$

$$\therefore 542000^{\text{qkm}} = 542000 \times 100^{\text{he}}.$$

$$= 54200000^{\text{he}}.$$

15. A piece of land 1224.5<sup>m</sup> square is sold at \$140 a boktar. How much does the land bring?

1224.5	149.94
1224.5	<b>\$140</b>
61225	599760
48980	14994
24490	\$20,991.60
24490	φ20,001.00
12245	
1499400.25qm	
- 149.94ha.	

16. The total surface measurement of the glass in the windows of a house is  $182^{qm}$ . How many panes of  $53^{qm}$  by  $48^{qm}$  will it take to supply the windows?

 $182^{qm} = 1,820,000^{qcm}$ .

53cm	715.4	
48em	2544) 1820000.0 17808	
424		
212	3920	
2544 quan, area of one pane.	2544	
, and on one parts	13760	
	12720	
	10400	
•	10176	
5. 169 . 9 had		

: it will take 716 panes.

17. How many square slabs of marble 150qom on the surface will it require to pave a court whose area is 25.35qm?

 $25.35^{qm} = 253,500^{qcm}$ .

The number of slabs required is  $253,500^{\text{cm}} + 150^{\text{cm}} = 1690$ .

18. A speculator bought 31.0728ha of land for \$1296 a hektar. For how much a square meter must be sell it to realize a profit of \$1937?

31.0728		\$0.136
<b>\$</b> 1296		<b>\$10728)</b> \$42207.349
1864368		<b>3</b> 10728
2796552		1113454
621456		932184
310728		1812709
<b>\$40,270.34</b> 88	cost.	1012/00
1937	profit.	
<b>\$42,207.3488</b>	selling price.	

19. A man is offered \$6000 for 2.5 ars of land. He declines to sell; and soon after, the town gives him \$25.20 a square meter. How much did he make by refusing the first offer?

$$2.5^{\circ} = 250^{\circ}$$
  
\$25.20  
 $250$   
 $126000$   
 $5040$   
\$6300.00  
 $6000$   
\$300

20. A man surveys a piece of land and finds that it measures 14.0715<sup>ha</sup>. He afterwards discovers that his chain was too short by 0.03<sup>m</sup>. How can he calculate the real superficial measurement of his land without surveying it again? (A surveyor's chain is 10<sup>m</sup> long.)

$$\begin{array}{r}
 10.00 - 0.03 = 9.97. \\
 9.97 + 10 = 0.997. \\
 \hline
 0.997 & 14.0715^{\text{ha}} \\
 \hline
 0.994009 & \\
 \hline
 6979 & 1266435 \\
 \hline
 8973 & 562860 \\
 \hline
 8973 & 1266435 \\
 \hline
 \hline
 0.994009 & 1266435 \\
 \hline
 \hline
 13.987^{\text{ha}}
 \end{array}$$

21. The railroad from Paris to Orleans has a double track; each rail is 4<sup>m</sup> long, and the distance from Paris to Orleans is 121<sup>km</sup>. What is the number of rails used in laying the track? The width of the road is 15<sup>m</sup>; how many hektars of land does the road include?

There are four lines of rails.  $4 \times 121^{km} = 484^{km} = 484,000^m$  of rails. If one rail is  $4^m$  long, in  $484,000^m$  there are  $484,000 \div 4 = 121,000$  rails.  $15^m = 0.015^{km}$ . The area of road is

$$121^{km} \times 0.015^{km} = 1.815^{qkm} = 181.5^{kn}$$
. Ans.

121km	4) 484000	121km
4	121000 rails.	0.015
484km		605
		121
		1.815qkm

22. Calculate the number of ars in a surface which a ream of paper (480 sheets) will cover. The sheets are 30.3cm long and 195mm wide.

 $195^{mm} = 19.5^{om}$ .

The area of one sheet is  $30.3^{\text{cm}} \times 19.5^{\text{cm}} = 590.85^{\text{qcm}}$ .

The area of 480 sheets is  $480 \times 590.85^{\text{qom}} = 283,608^{\text{qom}} = 0.283608^{\text{a}}$ .

19.5	590.85
30.3	480
585	4726800
585	<b>2</b> 363 <b>4</b> 0
590.85qcm	283608.00qcm

23. A pile of wood is 4.25<sup>m</sup> long, 1.33<sup>m</sup> thick, and 2.60<sup>m</sup> high. How many sters are there in it?

1" = 1cbm. In the pile of wood there are

$$4.25 \times 1.33 \times 2.60 = 14.6965^{\text{obm}} = 14.696^{\text{s}}$$
. Ans.  
 $4.25$   $5.6525$   $2.6$   $339150$   $1275$   $13050$   $14.69650^{\text{obm}}$   $14.69650^{\text{obm}}$ 

24. A beam is 7.070<sup>m</sup> long; its two other dimensions are 0.258<sup>m</sup> and 87<sup>mm</sup>. Find its volume.

 $87^{mm} = 0.087^{m}$ . Its volume is  $0.258^{m} \times 0.087^{m} \times 7.070^{m} = 0.15869^{obm}$ .

$$egin{array}{cccc} 0.258 & 0.022446 \\ \underline{0.087} & \underline{7.07} \\ 1806 & \underline{157122} \\ \underline{2064} & \underline{157122} \\ 0.022446 & 0.15869322^{\mathrm{obsm}} \end{array}$$

25. A bar of iron 3<sup>m</sup> long measures 45<sup>mm</sup> square on the end where it has been evenly cut. The bar is heated and drawn out to a greater length by being passed through an orifice 24<sup>mm</sup> square. What is the length of the bar after the operation?

$$45^{mm} = 0.045^{m}$$
.  $24^{mm} = 0.024^{m}$ .

The volume of the bar is  $0.045^{m} \times 0.045^{m} \times 3^{m} = 0.006075^{obm}$ . The area of the end, after the bar has been heated is

$$0.024^{m} \times 0.024^{m} = 0.000576^{qm}$$
.

Therefore the length of the bar is  $0.006075 + 0.000576 = 10.547^{m}$ .

0.045 <sup>m</sup>	0.024m	10.547
0.045	0.024	576)6075.000
225	96	576
180	48	3150
0.002025qm	0.000576qm	2880
3		2700
0.006075°bm		2304
		3960
		3892
		<del></del>

26. A reservoir is 1.50<sup>m</sup> wide, 2.80<sup>m</sup> long, and 1.25<sup>m</sup> deep. Find how many liters it contains when full, and to what height it would be necessary to raise it that it might contain 10<sup>obm</sup>.

The volume of the reservoir is  $1.5 \times 2.8 \times 1.25 = 5.25^{\text{elem}} = 5250^{\text{l}}$ . The area of the bottom is  $1.5 \times 2.8 = 4.2^{\text{qm}}$ ; therefore, in order to contain  $10^{\text{obm}}$ , the height must be  $10^{\text{obm}} + 4.2^{\text{qm}} = 2.38^{\text{m}}$ .

1.5 <sup>m</sup>	2.38m
2.8	42)100.00
120	84
30	160
4.20qm	126
1.25	340
2100	<b>3</b> 36
840	-
420	
5,2500	

27. Suppose a box to be 3.75<sup>m</sup> long, 3.50<sup>m</sup> wide, and 0.50<sup>m</sup> high. How much lime would it take to fill it with mortar, reckoning that 1<sup>cbm</sup> of lime after being slaked becomes 1.80<sup>cbm</sup> of mortar?

Volume of the box is  $3.75 \times 3.50 \times 0.50 = 6.5625^{\text{chem}}$ . Since 1 of mortar when slaked becomes  $1.8^{\text{nbm}}$ , the box will hold  $6.5625^{\text{chem}}$  of slaked mortar, which is the same as  $6.5625^{\text{chem}} + 1.8 = 3.646^{\text{chem}}$  of dry mortar.

3.75	3.646cbm
3.5	18)65.625cbm
1875	54
1125	116
13.125	108
0.5	82
6.5625°bm	72
0.0020	105

28. A chest has the following dimensions: 1.17<sup>m</sup>, 90<sup>m</sup>, 1.04<sup>m</sup>. How many cakes of soap 13<sup>cm</sup> square on the bottom and 29<sup>cm</sup> thick could be put in it? 0.12 of the volume of the chest must be deducted for packing.

The volume of a cake of soap is  $13 \times 13 \times 29 = 4901^{\text{com}}$ . The volume of the chest, deducting waste of room in packing, is

 $1.17 \times 0.90 \times 1.04 \times 0.88 = 0.9637056^{\text{cbm}} = 963705.6^{\text{com}}$ . Therefore the chest will hold (963,705.6 + 4901) cakes of soap.

13	1.17	196
13	1.04	4901)963705.6
<del></del> 39	468	4901
13	$\frac{117}{12168}$	47360 44109
169 . 29	$\frac{0.9}{1.09512}$	32515
1521	0.88	29406
338	876096	<del></del>
4901 ocm	876096 0.9637056ebm	·

29. A cubic meter of dry plaster makes 1.18cbm when tempered; tempered plaster increases 1 in every 100, twenty-four hours after it is mixed. What volume of tempered plaster would be obtained from 55 sacks of 251 each of dry plaster?

 $25^{1} = 0.025^{\text{cbm}}$ . The volume of the plaster is  $55 \times 0.025^{\text{cbm}} = 1.375^{\text{cbm}}$ . As  $1^{\text{cbm}}$  makes  $1.18^{\text{cbm}}$  when tempered,  $1.375^{\text{cbm}}$  will make  $1.375 \times 1.18^{\text{cbm}} = 1.6225^{\text{cbm}}$ . In twenty-four hours its volume will be  $1.01 \times 1.6225^{\text{cbm}} = 1.6387^{\text{cbm}}$ .

0.025cbm 55 125 125 1.375cbm	1.375cbm	1.6225
	1.18	1.01
	11000	16225
	1375	16225
	1375	1 000 Tahm
	1,62250 cbm	1.6387°bm

30. A reservoir is 2.80<sup>m</sup> long, 1.50<sup>m</sup> wide, and 1.25<sup>m</sup> deep. How many liters will be required to fill 0.80 of it?

1.5m	4.20qm	<b>5250</b> <sup>1</sup>
<b>2</b> .8	1.25	0.8
120 30	2100	4200.0
	840	2200.0
<del></del>	420	
4.20qm	5.2500 <sup>cbm</sup>	
	$=5250^{\circ}$ , volume.	

31. A man buys 1415<sup>hl</sup> of wheat for \$3.50 a hektoliter; but the measure used proves too small, the mistake amounting to 3<sup>l</sup> in every hektoliter. What was the quantity of wheat delivered to the purchaser, the cost, and the reduction which ought to be made to him on account of the error?

The mistake was  $3^1$  in  $100^1$ , or he received only 0.97 of  $1415^{h1}$  =  $1372.55^{h1}$ . If  $1^{h1}$  of wheat cost \$3.50,  $1415^{h1}$  cost  $1415 \times $3.50$  = \$4952.50. A reduction of 0.03 of \$4952.50 = \$148.58 ought to be made.

1415hl	1415	· \$4952.50
0.97	<b>\$</b> 3.50	0.03
9905	70750	<b>\$148.5750</b>
12735	4245	-
1372.55 <sup>hl</sup>	<b>\$</b> 4952.50	

32. The dimensions of a tile are as follows: length 22° m, width 11° m, thickness 55 mm. Find the volume of the tile, and the number of tiles in a pile of 25° m.

 $55^{\text{mm}} = 5.5^{\text{cm}}$ . The volume of a tile is  $22 \times 11 \times 5.5 = 1331^{\text{com}}$ .  $25^{\text{cbm}} = 25,000,000^{\text{com}}$ . In the pile there will be 25,000,000 + 1331 = 18,732 tiles.

22cm
11
<u></u> 22
22
242
5.5
1210
1210
1331.00cm

33. The measurement of a pile of wood shows that a ster could be filled from it 25.68 times. Give the volume of the pile in cubic meters, reckoning the length of the logs to be 1.15<sup>m</sup>.

The volume of a pile is  $1 \times 1 \times 1.15 \times 25.68 = 29.532^{\text{chan}}$ . Ans.

25.68 1.15<sup>cbm</sup> 12840 2568 2568 29.5320<sup>cbm</sup>

34. A liter of air weighs 1.273s. How much does a cubic meter of air weigh?

 $1^{\text{cbm}} = 1000^{\text{l}}$ . Therefore  $1^{\text{cbm}}$  of air weighs  $1000 \times 1.273^{\text{s}} = 1273^{\text{s}} = 1.273^{\text{ks}}$ . Ans.

35. A package of candles which weighs 465s is sold at 28 cents. What is the price of a kilogram of candles?

1s of candles costs \$0.28 + 465 = \$0.000602. Therefore  $1^{leg}$  costs  $1000 \times $0.000602 = $0.602$ .

36. How many times would 3.243 of water fill a liter?

As 1° of water will fill a cubic meter, 3.243° will fill 3.243° meter, 3.243

- 37. Give the weight in kilograms of 43.4578ccm of pure water.
- $43.4578^{\text{com}}$  of water weigh  $43.4578^{\text{g}} = 0.0434578^{\text{kg}}$ .
- 38. The volume of an engine's axletree is 0.245chm. Find its weight, the specific gravity of the iron being 7.8.
  - $0.245^{\text{cbm}}$  of water weigh  $0.245^{\text{t}}$ , and  $0.245^{\text{cbm}}$  of iron weigh  $7.8 \times 0.245_{\text{t}} = 1.911^{\text{t}}$ .

39. Calculate the volume of a gram of the following substances: proof spirit, specific gravity 0.865; tin, specific gravity 7.291; lead, specific gravity 11.35; copper, specific gravity 8.85; silver, specific gravity 10.47; cork, specific gravity 0.240.

The volume equals 1 which, filled with water, weighs 14 divided by the specific gravity.

(i.)	(iii.)	(v.)
1.16 cam	0.088°	0.095
865)1000.00	1135) 100.000	1047) 100.000
865	9080	9423
1350	9200	5770
865	9080	<b>5235</b>
4850		(vi.)
	(iv.)	4.1670cm
(ii.)	0.1130cm	24) 100.000
0.14cm	885) 100.000	96
7291) 1000.00	885	40
7291	1150	24
<b>27</b> 090	885	160
	2650	144
		160

40. Olive oil costs 60 cents a kilogram. What is the price of a liter? The specific gravity of olive oil is 0.914.

11 of olive oil weighs  $0.914^{kg}$ . As  $1^{kg}$  costs \$0.60, 11 costs 0.914  $\times$  \$0.60 = \$0.548.

41. Pure alcohol costs \$1.87 a kilogram. What is the price of a liter? The specific gravity of alcohol is 0.792.

11 of alcohol weighs 0.792 kg.

As  $1^{kg}$  costs \$1.87,  $1^{1}$  costs 0.792  $\times$  \$1.87 = \$1.48.

42. A man wants to build a shed large enough to hold 135<sup>st</sup> of wood; if the shed is to be 3<sup>m</sup> high and 5<sup>m</sup> wide, how long must it be?

 $135^{\text{et}} = 135^{\text{obm}}$ . The ground area is  $3 \times 5 = 15^{\text{qm}}$ . Therefore the height must be  $135 + 15 = 7^{\text{m}}$ .

43. In a country where firewood is cut 1.16<sup>m</sup> long what height must the sides of the ster be to hold a cubic meter?

The height must be  $1^{\text{chm}} \div 1.16^{\text{qm}} = 0.86207^{\text{m}}$ .

44. If a ster of cork cost \$20.00, how much would 100kg cost, the cork weighing one quarter as much as water?

1st of cork weighs  $250^{kg}$ , and costs \$20.00.  $100^{kg}$  will cost  $\frac{199}{250}$  of \$20.00 =  $\frac{2}{5}$  of \$20.00 = \$8.00.

45. A liter of powder weighs 825s. What would be the volume of a charge for a gun if the charge weighed 5s? Calculate the volume in cubic centimeters.

The specific gravity of powder is 0.825. It takes  $(1 \div 0.825)^{\text{com}}$  of powder to weigh  $1^g$ ; therefore to weigh  $5^g$  it takes  $5^{\text{com}} + 0.825 = 6.06^{\text{com}}$ .

46. Out of gold which weighs 19.362 times as much as water, sheets of gold foil are made which are 0.010<sup>mm</sup> in thickness. What surface would 3<sup>g</sup> of gold cover?

 $0.010^{\text{mm}} = 0.001^{\text{cm}}$ . The volume of the gold is  $3^{\text{com}} + 19.362 = 0.154943^{\text{ccm}}$ . Therefore, the surface is  $0.154943^{\text{ccm}} + 0.001^{\text{cm}} = 154.943^{\text{ccm}}$ .

47. Find the weight of an oak board 3.25<sup>m</sup> long, 0.31<sup>m</sup> wide, and 0.04<sup>m</sup> thick; the specific gravity of the oak being 0.808.

The volume of the board is  $3.25 \times 0.31 \times 0.04 = 0.0403^{\text{obm}}$ .  $1^{\text{obm}}$  of oak weighs  $0.808^{\text{t}}$ ; therefore  $0.0403^{\text{obm}}$  weigh  $00.403 \times 0.808^{\text{t}} = 0.0325624^{\text{t}} = 32.5624^{\text{kg}}$ .

48. Find the weight of a bar of iron having the following dimensions: length 3.6<sup>m</sup>, width 6<sup>cm</sup>, thickness 2<sup>cm</sup>; the specific gravity of the iron being 7.8.

3.6m = 
$$360^{\circ m}$$
.

360

 $\frac{6}{2160}$ 
 $\frac{2}{4320^{\circ \circ m}}$ , volume.

4320

 $\frac{7.8}{34560}$ 
 $\frac{3024}{33696.06}$ 

=33.696ks

49. How many lead balls each weighing 27s could be obtained by melting a mass of lead, cubic in form, the edge measuring 0.356m, the specific gravity of the lead being 11.35?

 $0.356^{m} = 35.6^{cm}$ .

35.6°	<b>4</b> 5118.01 <b>6</b>	18966
35.6	11.35	27)512089
2136 1780 1068 1267.36	225590080 135354048 45118016 45118016	27 242 216 260
35.6	512089.4816 <b>0</b>	243
760416		178
633680		162
380208		169
45118.016 <sup>com</sup> , volume	<b>).</b>	162

50. Marble costs \$30.95 a cubic meter, and the specific gravity of marble is 2.73. If a block of marble weighs 1260kg, what is its volume, and what is it worth?

1° of marble weighs  $2.73^{t}$ .  $1260^{kg} = 1.26^{t}$ .

0.4515cbm	0.4615
273)126.0000	<b>\$</b> 30.95
1092	23075
1680	41535
1638	13845
420	<b>\$14.28</b>
$\frac{273}{1470}$	
1365	

51. Sea-water contains 28 parts, by weight, of salt in 1000. A liter of sea-water weighs 1.025<sup>kg</sup>. How many kilograms of salt could be obtained from 126.276842<sup>cbm</sup> of sea-water?

1 1 of sea-water contains 0.028 of salt.

126.276842	129433.753
1.025kg	0.028 kg
631384210	1035470024
<b>252553684</b>	258867506
126276842	3624.145084kg
129.433753050kg	

52. An empty cask weighs 17.06kg; when filled with water it weighs 275.8kg. How many liters does it hold? How many casks of this size would it require to receive the wine from a vat containing 3.008cbm?

The cask will hold  $275.8^{kg} - 17.06^{kg} = 258.74^{kg}$  of water. It takes  $258.74^{kg}$  of water to weigh  $258.74^{kg}$ . Therefore the cask will hold  $258.74^{kg}$ .

 $3.008^{\text{obsn}} = 3008^{\text{l}}$ . If one barrel holds  $258.74^{\text{l}}$ , to hold  $3008^{\text{l}}$ , it will take 3008 + 258.74 = 12 barrels.

53. It takes about 204.81 of wheat to sow a hektar. How many cubic meters would it take to sow a square kilometer?

 $1^{\text{qkm}} = 100^{\text{hs}}$ .  $1^{\text{hs}}$  will require  $100 \times 204.8^{\text{l}} = 20.480^{\text{l}} = 20.48^{\text{chm}}$ . Ans.

54. A piece of road 1km long and 7m wide is to be macadamized; the macadamizing is to be 33cm deep; it costs 43 cents a cubic meter to prepare the stones. What will enough for the road cost?

 $1^{km} = 1000^{m}$ ;  $33^{cm} = 0.33^{m}$ .

0.33	2310
7	\$0.43
2.31	6930
1000	9240
2310.00	\$993.30

55. A gasometer holds 28,000cbm of gas. How many jets would this gasometer feed, when each jet burns 1251 an hour, and is used 4 hours every evening?

Each jet will burn  $4 \times 125^1 = 500^1$  each evening.  $28,000^{\text{obm}} = 28,000,000^1$ . The gasometer will feed 28,000,000 + 500 = 56,000 jets.

56. The city of Venice is situated in the midst of a great lake of salt water, communicating with the sea, and all the rain-water is caught for the cisterns. Ordinary years the fall of rain in Venice is 82<sup>cm</sup>; the surface of the city, after the canals have been deducted, is 520<sup>ha</sup>; reckoning the population at 115,330, how many liters a day of rain-water could each inhabitant have?

 $520^{\text{hs}} = 5,200,000^{\text{qm}}; 82^{\text{cm}} = 0.82^{\text{m}}.$ 

The average amount of rain-water is  $5,200,000 \times 0.82 = 4,264,000^{\text{obss}} = 4,264,000,000^{\text{l}}$ . Each person can use per year 4,264,000,000 + 115,530, or, per day,  $4,264,000,000 + (115,530 \times 365) = 101.118^{\text{l}}$ .

0.82	115,530	101.1181
5200000	365	4216845)426400000.000
16400000	577650	4216845
410	693180	4715500
4264000.00	346590	<b>4216845</b>
	42168450	4986550
		4216845
		7697050
		4216845
		34802050
		33734760

57. Find the weight of a bar of iron 5.35<sup>m</sup> long, 4.56<sup>cm</sup> thick, and 3.54<sup>cm</sup> wide. Find, also, the width of an oak beam 4.30<sup>m</sup> long, 9.12<sup>cm</sup> thick, which has the same weight. The specific gravity of the oak to be reckoned at 1.026, that of the iron 7.788.

 $5.35^{m} = 535^{om}$ .  $4.30^{m} = 430^{cm}$ . The volume of the oak beam is  $67,258.596992^{g} + 1.026^{g} = 65,554.188^{com}$ . The area of one side of the oak beam is  $430 \times 9.12 = 3921.6^{qcm}$ ; therefore thickness is  $65,554.188^{com} + 3921.6^{qcm} = 16.72^{cm}$ .

4.56 cm		16.14 <b>24</b>		8636.184
3.54		535		7.788
1824		807120		69089472
2280		484272		69089472
1368		807120		60453288
6.1424qcm		8636.1840°cm,	volume.	60453288
	65554.188	·		67258.596992
1026)672	258596.992		•	=67.259kg.
618				$16.72^{cm}$
56	398		39216	655541.88
	130			39216
	5685			263381
<u> </u>	5130			<b>2</b> 35296
	5559			
	5130			280858
	4296			274512
	$\frac{4104}{1929}$			63468
	1026			
	9039			
	8208			
	8212			

58. Give the specific gravity and volume of a body weighing 35kg in air and 30kg in water.

The weight of water displaced by the body is 5kg.

The weight of body in air is 35kg.

Therefore specific gravity is 35 + 5 = 7.  $35^1$  of water weigh  $35^{kg}$ ;  $35 + 7 = 5^1$ , volume.

59. A ster of piled oak wood weighs 425kg; the specific gravity of the wood is 0.74. What is the volume occupied by the spaces between the logs? For how much must 100kg of separate sticks be sold in order to bring the same amount as when sold by the ster; a ster selling for \$2.20?

If there were no spaces between the logs, the ster of wood would weigh  $740^{kg}$ . Therefore the spaces, if filled with wood, would weigh  $740^{kg} - 425^{kg} = 315^{kg}$ . Therefore volume of spaces is  $315 \div 740 = 0.42568^{obm}$ .  $100^{kg}$  ought to be sold for  $\frac{199}{425}$  of \$2.20 = \$220 + 425 = \$0.518.

0.42568°bm	<b>\$</b> 0.518	
74)31.50000	425) \$ 220.000	
_296_	2125	
190	750	
148	425	
420	3250	
$\frac{370}{500}$	3200	
444		
560		

60. Wrought iron sells for \$7.00 per 100ks. A bar of iron 4.5cm wide, 3.3cm thick costs \$5.08; what is its length, reckoning the specific gravity of the iron at 7.4?

\$7.00 per  $100^{kg}$  is the same as \$0.07 per kilogram. An iron bar that costs \$5.08 must weigh  $5.08 + 0.07 = 72.57143^{kg}$ , and its volume is  $72.57143 + 7.4 = 9.8066^{l} = 9806.5^{ccm}$ . The area of an end of the bar is  $4.5^{ccm} \times 3.3^{ccm} = 14.85^{ccm}$ . Therefore the length is  $9806.6 + 14.85 = 660.4^{ccm} = 6.604^{ccm}$ .

9.8066 <sup>1</sup>	660.4°
74) 725.7143	1485) 980650.0
666	8910
597	8965
<u>592</u>	8910
514	<del></del>
444_	5500
703	
<u>666</u>	

61. Experiment shows that water weighs 770 times as much as air; and the specific gravity of mercury, in comparison with water, is 13.6. How many liters of air will it take to weigh as much as a liter of mercury?

Water is 770 times as heavy as air, and mercury is 13.6 times as heavy as water. Therefore mercury is 13.6 × 770 times as heavy as air.

62. A mass of lead weighing 753ks is made into sheets 0.1mm thick. Calculate, in square me-

ters, the surface which can be covered by the sheets thus obtained. The specific gravity of the lead is 11.3.

The volume of the lead is  $753 + 11.3 = 66.637^1 = 0.066637^{\text{obs}}$ .

 $0.1^{mm} = 0.0001^{m}$ . The surface of the lead is

 $0.066637^{\text{nbm}} + 0.0001^{\text{m}} = 666.379^{\text{m}}$ .

63. A rectangular sheet of tin of uniform thickness is 85cm wide, 1.35m long; it weighs 268s. What is its thickness, reckoning the specific gravity of tin at 7.3?

The volume of the tin is  $268 + 7.3 = 36.7109^{\text{com}}$ ;  $1.35^{\text{m}} = 135^{\text{cm}}$ . The area of the tin is  $135^{\text{cm}} \times 85^{\text{cm}} = 11,475^{\text{qom}}$ ; therefore its thickness is  $36.7109^{\text{com}} + 11,475^{\text{qom}} = 0.0032^{\text{cm}}$ .

64. The fine coal which collects about the shafts of the mines and in the coal-yards, was for a long time wasted, because it could not be burned in stoves and grates. Now, this dust is mixed with tar in proportion of 92kg of dust and 8kg of tar; the mixture is heated, and afterwards pressed in rectangular moulds of 14.75cm, 18.5cm, and 29cm; each one of these blocks weighs 10kg; they are sold at \$3.00 \text{ a ton, and make excellent fuel for heating steam boilers. Give the specific gravity of this fuel; also, the sum which would be realized in thus utilizing 800,000t of coal dust, the cost of tar, mixing, etc., being \$0.50 a ton.

Volume of a block is  $14.75 \times 18.5 \times 29 = 7913.305^{\text{com}} = 7.913305^{\text{l}}$ . Specific gravity is 10 + 7.913305 = 1.264.  $800,000^{\text{t}}$  of coal dust will make  $800,000^{\text{t}} + 0.92 = 869,565.217^{\text{t}}$  of the mixture.  $869,565.217^{\text{t}}$  at \$2.50 per ton =  $869,565.217 \times \$2.50 = \$2,173,913.04$ .

Per ton occionative and	¥ =,=, 0, 0 = 0 0 = 0
14.75cm	869565.217
18.5	92)80000000.00
7375	736
11800	640
1475	<u>552</u>
272.875	880
29	<u>828</u> 520
2455805	460
<b>54</b> 5750	600
7913.305ccm	<u>552</u> 480
1.264 79133)100000.000 79133 208670 158266 504040 474798	460 200 184 160 92 680 644 869565.217
292420	\$2.50
	43478260850 1739130434
	\$2,173,913.04

65. A bar of iron a millimeter square on the end will break under a tension of 30kg. Find the length at which a suspended bar of iron will break from its own weight, the specific gravity of the iron being 7.8.

 $30^{kg} = 0.03^{t}$ .

The volume of the iron bar is  $0.03 + 7.8 = 0.00384615^{\text{obm}}$ . The area of an end of the bar is  $1^{\text{mm}} \times 1^{\text{mm}} = 1^{\text{qmm}} = 0.000001^{\text{qm}}$ . Therefore the length of the bar is  $0.00384615^{\text{obm}} + 0.000001^{\text{qm}} = 3846.15^{\text{m}}$ .

66. Fifty-three kilograms of starch are obtained from 100kg of wheat. A hektar of land produces 1363 of wheat; a hektoliter of wheat weighs 78kg. If the wheat harvested from a field measuring 2kg and 33qm is taken

to a starch factory, how much starch will be made from it?

 $0.53^{kg}$  of starch are obtained from  $1^{kg}$  of wheat.  $1^{l}$  of wheat weighs  $0.78^{kg}$ .  $1^{ha}$  produces  $1363 \times 0.78^{kg}$  of wheat  $= 1063.14^{kg}$ ,  $2^{ha}$   $33^{qm}$   $= 2.0033^{ha}$ .  $2.0033^{ha}$  produce  $2.0033 \times 1063.14^{kg}$   $= 2129.788362^{kg}$  of wheat. The amount of starch is  $1128.7878^{kg}$ .

1363 0.78\*s 10904 9541 1063.14\*s 2.0033 318942 318942 212628 2129.788362\*s 2129.788 0.53 6389364 10648940 1128.78764\*s

67. A gardener wishes to provide glass for his hot-beds. The beds cover 2.65°; the panes will cover 0.75 of the whole surface, the rest being taken up by the frames and alleys. First, find how many panes measuring 45°m by 37°m it will take to cover the beds; then find the price of the glass, at a cost of 95 cents a square meter.

 $45^{\text{cm}} = 0.45^{\text{m}}$ ;  $37^{\text{cm}} = 0.37^{\text{m}}$ ;  $2.65^{\text{a}} = 265^{\text{cm}}$ .

Total area of the glass is 0.75 of  $265^{qm} = 198.75^{qm}$ . The area of one pane is  $0.45 \times 0.37 = 0.1665^{qm}$ . Therefore the number of panes needed is 198.75 + 0.1665 = 1194. At \$0.95 per square mater,  $198.75^{qm}$  will cost  $198.75 \times \$0.95 = \$188.81$ .

0.45m	1:194	198:75
0.37	1665)1987500	<b>:\$.0.95</b>
315	1665	99375
135	8225	178875
0.1665qm	1665	\$188.81
	15600	
	14985	
	6150	

68. A jar full of water weighs 1.325\*s; filled with mercury it weighs 12.540\*s. What is the capacity of the jar, and its weight? The specific gravity of the mercury is 13.59.

The weight of the jar and the jar full of mercury is  $12.540^{kg}$ . Therefore the difference in weight between the mercury and the water is  $12.540^{kg} - 1.325^{kg} = 11.215^{kg}$ . 13.59 - 1 = 12.59, the specific gravity of a liquid of which the jar full without the jar weighs  $11.215^{kg}$ . Hence the capacity of the jar is  $11.215 + 12.59 = 0.89079^k$ .  $0.89079^k$  of water weigh  $0.89079^k$ . Therefore weight of jar is  $1.325 - 0.89079^k$  =  $0.43421^{kg} = 434.21^{kg}$ .

12.540 <b>/</b> 1.325	$0.89079^{1}$ $1259)1121.50000$	1.32500 <b>►</b> 0.89079
11.215ks	10072	0.43421
	11430	
	11331	
	9900	
•	-8813	
	10870	
	10072	

69. A helitoliter of rape-seed weighs 63ks, and 32% of oil can be extracted from it. How many kilograms of the seed will it take to make a helitoliter of oil?

'1<sup>h1</sup> = 100<sup>1</sup>. If  $32^{1}$  of oil can be extracted from  $68^{kg}$  of seed,  $1^{1}$  of oil can be extracted from  $63 \div 32 = 1.96875^{kg}$  of seed, and  $100^{1}$  of oil can be extracted from  $100 \times 1.96875^{kg} = 196.875^{kg}$  of seed.

70. Common burning gas is 0.97 of the weight of air, and a liter of air weighs 1.293s. In a shop there are 65 jets, each one of which burns 1231 an hour, and is used 5 hours in the winter evenings. Calculate the weight of the gas used in a month, and the expense of lighting the shop, when gas costs 6 cents a cubic meter.

11 of gas weighs  $0.97 \times 1.2934 = 1.254214$ . 65 jets, each burning 1234 am hour, and used 5 hours an evening for 30 days, will use  $65 \times 5 \times 30 \times 123^1 = 1,199,250^1$ , the weight of which is  $1,199,250 \times 1.254214 = 1,504,111.344 = 1504.1113444$ .  $1,199,250^1 = 1199.254214$ . The expense at \$0.06 per cubic meter is  $1199.25 \times $0.06 = $71.96$ .

1.293	123 <sup>1</sup>	1199250	1199.25
0.97	65	1.254218	\$0.06
9051	615	1199250	<b>\$71.9550</b>
11637	738	<b>239850</b> °	•
	79951	479700	<b>- \$</b> 71.96
1.25421	5	<b>599625</b>	
	399751	<b>2</b> 398 <b>5</b> 0	
	30	119925	
	1199250	1504111.34250	

71. A merchant buys one kind of wine at 30 cents a liter, another kind at 21 cents a liter; he mixes the two kinds by putting 51 of the first with 81 of the second. For how much a liter must he sell the mixture in order to gain \$3.75 a hektoliter?

51 at \$0.30 per liter cost \$1.50.

81 at \$0.21 per liter cost \$1.68.

Therefore  $13^1$  of the mixture cost \$1.50 + \$1.68 = \$3.18, and  $1^1$  costs \$3.18 + 13 = \$0.2446. Again, if \$3.75 per hektoliter is equivalent to a gain of \$0.0375 per liter, to make \$3.75 per hektoliter the merchant must sell the wine for \$0.0375 + \$0.2446 = \$0.2821 per liter.

<b>\$</b> 0.30	<b>\$</b> 0.21	0.2446
5	8	13)3.1800
\$1.50	<b>\$</b> 1.68	26
•	1.50	58
	<b>\$</b> 3.18	52
	•	60
		52
		80
		78

72. If it requires 360 tiles to drain an ar of land, what will it cost to drain 17.784ha, when the tiles cost \$20 a thousand, and the expense of laying is the same as the cost of the tiles?

The expense of laying the tiles and their cost is \$40 per thousand.  $17.784^{ha} = 1778.4^{a}$ . To drain  $1778.4^{a}$  of land  $1778.4 \times 360$  tiles = 640.224 tiles = 640.224 thousand are needed. 640.224 thousand at \$40 per thousand cost  $640.224 \times $40 = $25,608.96$ . Ans.

1778.4	640.224
360	<b>\$40</b>
1067040	\$ 25608.960
53352	
640224.0	

73. It is found in building that hewn stone of medium durability ought not to support, as a permanent weight, more than 0.07 of the

weight that it would require to crush it. A certain kind of stone used for building will be crushed under a weight of 250kg a square centimeter. What is the greatest height to which a wall constructed of this material can be safely carried, the specific gravity of the stone being 2.1?

250kg per square centimeter is equivalent to 250,000g per square centimeter. 0.07 of 250,000g = 17,500g ought to be the pressure on a square centimeter. Therefore volume of imaginary prism ought to be 17,500 + 2.1 = 8333.33cm, or the height ought to be 8333.33cm = 83.333m.

74. Several kinds of wines are mixed as follows: 2451 at 20 cents a liter, 5471 at 15 cents a liter, 3441 at 25 cents a liter. How much does the mixture cost a liter?

245<sup>1</sup> at \$0.20 per liter cost \$49.00 547<sup>1</sup> at \$0.15 per liter cost \$82.05 344<sup>1</sup> at \$0.25 per liter cost \$86.00 1136<sup>1</sup> of the mixture cost \$217.05

Therefore  $1^1$  costs \$217.05 + 1136 = \$0.191. Ans.

	•	-	
245	547	344	\$0.191
\$0.20	<b>\$</b> 0.15	\$0.25	1136) 217.050
<b>\$49.00</b>	2735	1720	1136 .
•	<b>547</b>	688	10345
	\$82.05	\$86.00	10224
	•	*	1210
			1136

75. A farmer wishes to drain a field of 8.75hs. Each hektar requires 750m of ditches. The opening of these ditches costs 10 cents a running meter; the tiles are 30cm long, and cost \$15 a thousand. He pays 2 cents a meter for laying the tiles, and 4 cents a meter for filling the ditches. What is the cost of draining the field?

There are required  $8.75 \times 750^{m} = 6562.5^{m}$  of ditches. The expense of opening the ditches, laying the tiles, and filling the ditches is \$0.10 + \$0.02 + \$0.04 = \$0.16 per meter.  $6562.5^{m}$  will cost 6562.5  $\times \$0.16 = \$1050.00$ .  $30^{cm} = 0.3^{m}$ . For  $6562.5^{m}$ , 6562.5 + 0.3 = 21.875 tiles are necessary. The tiles cost \$15 per thousand. Therefore 21.875 thousand cost  $21.875 \times \$15 = \$328.13$ . Hence cost of draining the field is \$1050.00 + \$328.13 = \$1378.13.

8.75	<b>65</b> 6 <b>2</b> .5	21.875	\$1050.00
75 <b>0</b>	<b>\$</b> 0.16	· <b>\$</b> 1'5`	328.13
43750	393750	109375	\$1378.13
6125	65625	21875	-
6562.50m	\$1050.000	<b>\$</b> 328.125 <b>- \$</b> 3	28.13.

### EXERCISE XI.

1. Find the prime factors of 148; 264; 178; 183; 173; 187; 346; 343.

2. Find the prime factors of 210; 353; 5280; 231; 31,476; 1369; 1368.

 $2^{8} \times 3 \times 7 \times 11 \times 17$ . Ans.

```
3. Find the prime factors of 247; 327; 179; 85; 2125; 2553; 2333.
                       3 \times 109. Ans.
   13 \times 19. Ans.
                                            1 \times 179. Ans.
                                                                 1 \times 83. Ans.
                                                               1 | 2333
                                     13 | 2353
                                                                 2333
                                 13 × 181. Ans.
                                                           1 \times 2333. Ans.
  4. Find the prime factors of 165; 168; 2148; 16,662; 321; 1551;
38.
       3 | 165
                                                                   2 | 16662
 3\times5\times11. Ans. 2^8\times3\times7. Ans. 2^2\times3\times179. Ans. 2\times3\times2777. Ans.
          3 321
              107
     3 \times 107. Ans.
                                                             2 \times 19. Ans.
                              3 \times 11 \times 47. Ans.
  5. Find the prime factors of 82; 129; 72; 66; 68; 65; 76; 86;
88; 142.
     2|82
                                 2^{3} \times 3^{2}. Ans.
                                                   2 \times 3 \times 11. Ans.
5\times13. And. 2^2\times19. And. 2\times43. And. 2^6\times11. Ans. 2\times71. Ans.
  6. Find the prime factors of 326; 368; 464; 292; 362; 365; 730;
42.
      2|326
                      24 × 23. Ans.
                                           2^4 \times 29. Ans.
                                                               2^n \times 73. Ans.
  2 \times 163. Ant.
                                               2 730
      2|362
         Ť81
 2 \times 181. Ans.
                       5 \times 73. Ans.
                                        2 \times 5 \times 73. Ans.
                                                              2 \times 3 \times 7. Ans.
```

7. Find the prime factors of 868; 999; 822; 1346; 7641; 6234; 234. 2º | 868 2 | 822 2|1346 3 411 217  $3^3 \times 37$ . Ans. 31 137  $2 \times 673$ . Ans.  $2^2 \times 7 \times 31$ . Ans.  $2 \times 3 \times 137$ . Ans. 2|6234 38 | 7641 3 3117 283 1039  $3^{3} \times 283$ . Ans.  $2 \times 3 \times 1039$ . Ans.  $2 \times 3^2 \times 13$ . Ans. 8. Find the prime factors of 579; 577; 212; 126; 128; 8192; **8190**. 3 579 193  $1 \times 577$ . Ans.  $2^2 \times 53$ . Ans.  $3 \times 193$ . Ans.  $2 \times 3^2 \times 7$ . Ans. 2 | 8190 32 4095 27. Ans. 218. Ans. 455 5 13  $2\times3^2\times5\times7\times13$ . Ans. 9. Find the prime factors of 8197; 3125; 2401; 1331; 78,309; **25,**179. 7 | 8197 1171 74. Ans. 118. Ans.  $7 \times 1171$ . Ans. 55. Ans. 32 | 78309 3 | 25179 8393 8701 7

11

1199

 $3\times7\times11\times109$ . Ans.

109

11

1243

 $3^2 \times 7 \times 11 \times 113$ . Ans.

113

### EXERCISE XII.

1. Find the prime factors of 8.4; 7.6; 1.08; 0.144; 0.036; 0.037; 21.45.

$$8.4 = 84 \times 0.1$$
.  $7.6 = 76 \times 0.1$ .  $1.08 = 108 \times 0.01$ .  $0.144 = 144 \times 0.001$ .

$$\begin{array}{c|c}
 2^2 & 108 \\
 3^2 & 27 \\
 \end{array}$$

 $2^{2}\times3\times7\times0.1$ . Ans.  $2^{2}\times19\times0.1$ . Ans.  $2^{2}\times3^{2}\times0.01$ . Ans.  $2^{4}\times3^{2}\times0.001$ . Ans.

$$0.036 = 36 \times 0.001$$
.

$$0.037 = 37 \times 0.001$$
.

$$21.45 = 2145 \times 0.01$$
.

$$\begin{array}{c|c}
 2^2 & 36 \\
 3^2 & 9 \\
 \hline
 1
 \end{array}$$

$$37$$
 $1 \times 37 \times 0.001$ . Ans.

 $2^2 \times 3^2 \times 0.001$ . Ans.

$$3 \times 5 \times 11 \times 13 \times 0.01$$
. Ans.

2. Find the prime factors of 14.6; 2.61; 21.2; 78.54; 0.5236; 0.00052.

$$14.6 = 146 \times 0.1$$

$$2.61 = 261 \times 0.01$$
.  $21.2 = 212 \times 0.1$ .

$$21.2 = 212 \times 0.1$$

$$2 \times 73 \times 0.1$$
. Ans.

$$3^2 \times 29 \times 0.01$$
. Ans.

$$2^2 \times 53 \times 0.1$$
. Ans.

$$78.54 = 7854 \times 0.01$$
.

$$0.5236 = 5236 \times 0.0001$$
.

 $2^2 \times 7 \times 11 \times 17 \times 0.0001$ . Ans.

 $2\times3\times7\times11\times17\times0.01$ . Ans.

$$0.00052 = 52 \times 0.00001$$

 $2^2 \times 13 \times 0.00001$ . Ans.

3. Find the prime factors of 86.7; 48.3; 99.99; 5.04; 1.485; 0.216.

$$86.7 - 867 \times 0.1$$
.

$$48.3 = 483 \times 0.1$$
.

$$99.99 = 9999 \times 0.01$$
.

 $3\times17^{2}\times0.1$ . Ans.  $3\times7\times29\times0.1$ . Ans.  $3^{2}\times11\times101\times0.01$ . Ans.

$$5.04 = 504 \times 0.01$$
.

$$1.485 = 1485 \times 0.001.$$

$$0.216 = 216 \times 0.001$$
.

 $2^{8} \times 3^{2} \times 7 \times 0.01$ . Ans.  $3^{8} \times 5 \times 11 \times 0.001$ . Ans.  $2^{8} \times 3^{8} \times 0.001$ . Ans.

4. Find the prime factors of 34.87; 32.4; 5.115; 71.2; 2.993.

$$34.87 - 3487 \times 0.01$$
.

$$32.4 = 324 \times 0.1$$
.  $5.115 = 5115 \times 0.001$ .

$$15 \triangleq 5115 \times 0.001$$

$$11 | 3487 \over 317$$
  
 $11 \times 317 \times 0.01$ . Ans.

$$2^2 \times 3^4 \times 0.1$$
. Ans.

 $3 \times 5 \times 11 \times 31 \times 0.001$ . Ans.

$$71.2 = 712 \times 0.1$$
.

$$2^{8} \times 89 \times 0.1$$
, Ans.

$$2.993 - 2993 \times 0.001$$
.

$$41 \times 73 \times 0.001$$
. Ans.

# EXERCISE XIII.

1. Find the G.C.M. of 27 and 33. | 3. Find the G.C.M. of 8 and 28.

3. Ans.

2. Find the G. C. M. of 13 and 39.

13. Ans.

4. Find the G.C.M. of 27 and 45.

$$3^2 - 9$$
. Ans.

5. Find the G.C. M. of 81 and 108.

$$3^{8}$$
  $\boxed{81 \quad 108}$   $\boxed{3}$   $\boxed{4}$   $\boxed{3^{8}} = 27$ . Ans.

6. Find the G.C.M. of 4, 10, 12.

7. Find the G.C.M. of 4, 6, 10.

8. Find the G. C. M. of 9, 12, 21.

9. Find the G.C.M. of 10, 15, 25.

10. Find the G.C.M. of 14, 98, 42.

11. Find the G.C.M. of 30, 18, 54.

12. Find the G. C. M. of 14, 56, 42.

**13.** Find the : G. C. M. of 96, 36, 48.

14. Find the G.C.M. of 84, 105, 63.

15. Find the G.C.M. of 24, 60, 84, 128.

16. Find the G.C.M. of 45, 81, 27, 90.

$$\frac{3^{2}}{5}$$
  $\frac{45}{5}$   $\frac{81}{9}$   $\frac{27}{3}$   $\frac{90}{10}$   $3^{2} = 9$ . Ans.

17. Find the G.C.M. of 78, 18, 54, 42.

18. Find the G.C.M. of 98, 28, 70, 42.

19. Find the G.C.M. of 96, 112, 80, 32.

20. Find the G.C.M. of 24, 96, 48, 120.

21. Find the G.C.M. of 84, 252, 168, 210.

22. Find the G. C. M. of 33, 88, 77, 55.

23. Find the G.C.M. of 252, 315, 420, 504.

24. Find the G. C. M. of 128, 192, 320, 368, 432.

$$2^{4}$$
  $128$   $192$   $320$   $368$   $432$   $8$   $12$   $20$   $23$   $27$   $2^{4}$  = 16. Ans.

25. Find the G. C. M. of 136, 204, 357, 459.

26. Find the G.C.M. of 909, 1414, 2323, 4242.

# EXERCISE XIV.

1. Find the G.C.M. of 2479 and 3589.

$$2479)3589(1)$$
 $2479$ 
 $10 1110$ 
 $3 111$ 
 $37)2479(67)$ 
 $222$ 
 $259$ 
 $37. Ans. 259$ 

2. Find the G.C.M. of 3045 and 6195.

3. Find the G.C.M. of 568 and 712.

$$\begin{array}{c|c}
8 & 568 & 712 \\
\hline
71 & 89 & 71 \\
& 71 \\
2 & 18 \\
3^2 & 9 \\
8. Ans. & 1
\end{array}$$

4. Find the G.C.M. of 11,023 and 6493.

5. Find the G.C.M. of 1485 and 2160.

6. Find the G.C.M. of 7040 and 7392.

7. Find the G.C.M. of 2760 and 4485.

8. Find the G.C.M. of 1177 and 2675.

$$\begin{array}{r}
 11 | 1177 \\
 \hline
 107) 2675 (25 \\
 \underline{214} \\
 \hline
 535 \\
 \underline{535}
 \end{array}$$

107. Ans.

9. Find the G.C.M. of 78,473 and 94,653.

809. Ans.

10. Find the G.C.M. of \$5,143 and 10,283.

11. Find the G. C. M. of 44,323 and 61,087.

12. Find the G. C. M. of 232,353 and 39,699.

13. Find the G.C.M. of 33,853 and 35,017.

14. Find the G.C.M. of 5115 and 7254.

15. Find the G.C.M. of 2268 and 3348.

16. Find the G. C. M. of 1003 and 2419.

17. Find the G.C.M. of 419 and 52,301.

18. Find the G. C. M. of 30,072 and 133,784.

19. Find the G.C.M. of 4527 and 10,836.

$$9 \begin{vmatrix} 4527 & 10836 \\ 11 & 473 & 7 \end{vmatrix} 1204$$

$$43 ) 172(4)$$

$$172$$

$$9 \times 43 = 387. Ans.$$

20. Find the G.C.M. of 17,104 and 27,794.

#### EXERCISE XV.

1. Find the G.C.M. of 855, 1197, 1596.

3	855	1197	_]	596
3	285	399		<b>532</b>
5	95	7/133	7	133
,	19	19		19
3	× 19 •	= 57. Ans.		

2. Find the G. C. M. of 3864, 3404, 3657.

23. Ans.

Find the G. C. M. of 15,561,
 11.115. 13.585.

,,	-,		
13	11115	13585	15561
9	855	5 1045	7 1197
5	95	11 209	9 171
	19	19	19
	v 19	- 947 A+	14

nd the G.C.M. of 2943, 578,

109 = 327. Ans.

Find the G. C. M. of 1177, 1391, 1819.

107. Ans.

Find the G. C. M. of 4939, 1347, 3143.

449) 3143 (7 3143

449. Ans.

 Find the G. C. M. of 740, 333, 296.

8. Find the G. C. M. of 833, 1785, 1309.

119. Ans.

9. Find the G.C.M. of 7326, 8547, 9768, 22,755.

$$\begin{array}{c|c}
8 & 9768 \\
11 & 1221 \\
\hline
111
\end{array}$$

111. Ans.

10. Find the G.C.M. of 4994, 7491, 9988, 12,485, 16,571.

$$\begin{array}{c|c}
5 & 12485 \\
11 & 2497 \\
\hline
& 227
\end{array}$$

$$\begin{array}{r}
 73 \\
 227)16571 \\
 \underline{1589} \\
 681 \\
 681
 \end{array}$$

227. Ans.

## EXERCISE XVI.

1. Find the L.C.M. of 6, 14, 21.

$$2 \underbrace{ \begin{bmatrix} 6 & 14 & 21 \\ 3 & 7 & 21 \end{bmatrix}}_{2 \times 3 \times 7 = 42. Ans.}$$

2. Find the L. C. M. of 8, 12, 3, 24.

3. Find the L.C.M. of 6, 10, 15.

4. Find the L. C. M. of 9, 12, 18, 4.

5. Find the L. C. M. of 15, 21, 35.

$$3 \underbrace{15}_{5} \underbrace{21}_{7} \underbrace{35}_{35}$$
 $3 \times 5 \times 7 = 105$ . Ans.

6. Find the L.C.M. of 12, 20, 24.

$$2^{3} \times 3 \times 5 = 120$$
. Ans.

7. Find the L.C.M. of 14, 24, 28.

$$2^{2} | 14 \quad 24 \quad 28 \\ \hline 6 \quad 7$$
$$2^{3} \times 3 \times 7 = 168. \ Ans.$$

8. Find the L.C.M. of 12, 15, 20.

9. Find the L. C. M. of 16, 24, 32.

Find the L. C. M. of 21, 33,
 77.

$$3[21 \quad 33 \quad 77]$$
 $7 \quad II \quad 77$ 
 $3 \times 7 \times 11 = 231$ . Ans.

11. Find the L. C. M. of 27, 33, 99.

$$3^{3} \underbrace{127 \quad \text{$98} \quad 99}_{3}$$

$$3^{9} \times 11 = 297. \quad Ans.$$

13. Find the L.C.M. of 7, 11, 13.

 $7 \times 11 \times 13 = 1001$ . Ans.

13. Find the L.C.M. of 77, 55, 35.

. Find the L.C.M. of 16, 18, 2.

Find the L. C. M. of 10, 12,
 33, 60.

 $2^4 \times 3 \times 5 \times 11 = 660$ . Ans.

16. Find the L. C. M. of 15, 16, 18, 20, 22, 24.

2	15 15 15 15	16	18	20	22	24
2	15	8	9	10	11	12
2	15	4	9	_ \$	11	6
3	15	2	9		11	#
	5	2	3		11	

 $2^{4} \times 3^{3} \times 5 \times 11 = 7920$ . Ans.

17. Find the L. C. M. of 56, 64, 70, 84, 112.

,	,				
2	34	64	70	84	112
2	54	32	35	42	56
$2^{z}$		16	35	21	28
7		4	35	21	
		4	K	-	

 $2^{\circ} \times 3 \times 5 \times 7 = 6720$ , Ans.

18. Find the L.C.M. of 48, 54, 81, 144, 162.

19. Find the L.C.M. of 75, 100, 120, 150, 180.

10	75	100	120	150	180
2		10	12	15	18
3		#	6	15	9
			2	5	3

 $2^{0} \times 3^{2} \times 5^{3} = 1800$ , Ans.

20. Find the L.C.M. of 112, 168, 196, 224.

21. Find the L.C.M. of 7, 14, 15, 21, 45.

22. Find the L.C.M. of 16, 25, 81.

23. Find the L.C.M. of 26, 39, 52, 65.

24. Find the L. C. M. of 80, 72, 225, 48.

25. Find the L.C.M. of 10, 20, 30, 40, 50, 60.

26. Find the L.C.M. of 30, 42, 105, 70.

27. Find the L.C.M. of 36, 24, 35, 20.

 $2^{8} \times 3^{2} \times 5 \times 7 = 2520$ . Ans.

28. Find the L.C.M. of 7, 11, 14, 15.

$$\frac{|7| 11}{2 \times 7 \times 11 \times 3 \times 5} = 2310$$
. Ans.

29. Find the L. C. M. of 12, 18, 27, 63, 28.

30. Find the L.C. M. of 34, 26, 65, 85, 51, 39.

 $2\times3\times5\times13\times17=6630$ . Ans.

31. Find the L.C.M. of 12, 18, 96, 144.

 $2^6 \times 3^2 = 288$ . Ans.

82. Find the L. C. M. of 84, 156, 63, 99.

 $2^{n} \times 3^{n} \times 7 \times 11 \times 13 = 36,036$ . Ans.

33. Find the L. C. M. of 17, 51, 119, 210.

**84.** Find the L. C. M. of 16, 30, 48, 56, 72.

 $2^4 \times 3^2 \times 5 \times 7 = 5040$ . Ans.

35. Find the L.C.M. of 27, 33, 54, 69, 132.

 $2^a \times 3^a \times 11 \times 33 = 27,324$ . Ans.

d the L.C.M. of 15, 180.

37. Find the L.C.M. of 44, 128, 198, 280, 330.

44	126	198	280	330
22	63	99	140	165
11	63	99	70	165
	21	33	70	55
	3	33	10	55
		33	2	11

 $2^4 \times 3^2 \times 5 \times 7 \times 11 = 27,720$ . Ans.

38. Find the L.C.M. of 50, 338, 675, 975.

 $2 \times 3^{0} \times 5^{1} \times 13^{2} = 228,150$ . Ans.

39. Find the L.C.M. of 552, 575, 920.

 $2^3 \times 3 \times 5^2 \times 23 = 13,800$ . Ans.

40. Find the L.C. M. of 228, 304, 342.

 $2^4 \times 3^3 \times 19 = 2736$ . Ans.

41. Find the L.C.M. of 1080 and 1260.

 $2^{8} \times 3^{8} \times 5 \times 7 = 7560$ . Ans.

42. Find the L.C.M. of 600 and 480.

43. Find the L.C.M. of 1564 and 1932.

 $2^{2} \times 17 \times 3 \times 7 \times 23 = 32,844$ . Ans.

44. Find the L.C.M. of 2530 and 1760.

$$\begin{array}{c|cccc}
2 & 2530 & 1760 \\
5 & 1265 & 880 \\
11 & 253 & 176 \\
\hline
& 23 & 16
\end{array}$$

 $2^{5} \times 5 \times 11 \times 23 = 40,480$ . Ans.

45. Find the L.C.M. of 936 and 2925.

 $2^{3} \times 3^{2} \times 5^{2} \times 13 = 23,400$ . Ans.

46. Find the L.C.M. of 3432 and 4032.

 $2^4 \times 3^5 \times 11 \times 13 = 576,576$ . Ans.

47. Find the L.C. M. of 1875 and 2425.

$$5^{2} \underbrace{1875 \quad 2425}_{75}$$

$$3 \times 5^{4} \times 97 = 181,875. \text{ Ans.}$$

48. Find the L.C.M. of 1632 and 2976.

 $2^5 \times 3 \times 17 \times 31 = 50,592$ . Ans.

49. Find the L.C.M. of 1001 and 2233.

$$\begin{array}{c|ccccc}
11 & 1001 & 2233 \\
7 & 91 & 203 \\
\hline
& 13 & 29
\end{array}$$

 $7 \times 11 \times 13 \times 29 = 29,029$ . Ans.

50. Find the L. C. M. of 539 and 1463.

 $7^2 \times 11 \times 19 = 10,241$ . Ans.

### EXERCISE XVII.

1. Find the L.C.M. of 424 and 583.

G. C. M. = 53.

L. C. M. - 11 × 424 - 4664. Ans.

2. Find the L.C.M. of 319 and 407.

G. C. M. - 11.

L. C. M. - 29 ×407 - 11,803. And.

Find the L.C.M. of 1679
 and 1932.

G. C. M. = 23, 69

L. C. M.=73×1932=141,036. Ans.

4. Find the L.C.M. of 1003 and 2419.

 $=17\times2419=41,123$ . Ans.

Find the L. C. M. of 1003 and 1357. ١

L. C. M. = 17×1357 = 23,069, Ans.

 Find the L. C. M. of 899 and 961.

L. C. M.  $= 29 \times 961 = 27,869$ . Ans.

7. Find the L.C.M. of 407, 703, 444.

L. C. M. = 11 × 19 × 444 = 92,796.

Ans.

8. Find the L.C.M. of 411, 959, 2055.

L. C. M. =  $7 \times 2055 = 14,385$ . Ans.

9. Find the L.C.M. of 221 and 351.

L. C. M. =  $17 \times 351 = 5967$ . Ans.

10. Find the L.C.M. of 1426 and 989.

L.C.M.= $2\times31\times989=61,318$ . Ans.

11. Find the L.C.M. of 3864, 3404, 3657.

 $2^{3} \times 3 \times 7 \times 23 \times 37 \times 53$ = 7,577,304. Ans.

12. Find the L.C.M. of 539 and 253.

$$\begin{array}{c|cc}
11 & 253 & 539 \\
\hline
23 & 49
\end{array}$$

L. C. M.  $= 23 \times 539 = 12,397$ . Ans.

13. Find the L.C.M. of 2943, 2616, 4578.

 $2\times4\times7\times9\times327=164,808$ . Ans.

14. Find the L.C.M. of 2863 and 1151.

L. C. M. = 
$$1151 \times 2863$$
  
=  $3,295,313$ . Ans.

15. Find the L.C.M. of 1177, 1391, 1819.

L. C. M. =13×17×1177=260,117. Ans.

16. Find the L.C.M. of 5317 and 2863.

L. C. M. -13×2863-37,219. Ans.

17. Find the L.C.M. of 12,703 and 12,879.

 Find the L.C M. of 23,309 and 10,753.

L. C. M. = 
$$10,753 \times 23,309$$
  
=  $240,631,677$ . Ans.

19. Find the L.C.M. of 4939 and 3143.

L.C.M.=11×3143-34,573. Ans.

20. Find the L.C.M. of 4199 and 6137.

L.C. M. = 19×4199=79,891. Ans.

### EXERCISE XVIII.

1. Reduce to whole or mixed

- 19. Ans.

to whole or mixed

= 24. Ans.

to whole or mixed

= 61. Ans.

4. Reduce to whole or mixed numbers 197.

5. Reduce to whole or mixed numbers \$12.

6. Reduce to whole or mixed numbers 34.

7. Reduce to whole or mixed numbers  $\frac{374}{25}$ .

$$\frac{3.74}{25} = 14\frac{24}{25}$$
. Ans.

8. Reduce to whole or mixed numbers  $\frac{481}{3}$ .

$$\frac{481}{13} = 37$$
. Ans.

9. Reduce to whole or mixed numbers \*\frac{3}{2}\frac{3}{2}\frac{3}{2}.

$$\frac{3828}{75} = 50\frac{78}{75}$$
. Ans.

10. Reduce to whole or mixed numbers 4684.

$$\frac{4684}{1777} = 26\frac{82}{1777}$$
. Ans.

11. Reduce to whole or mixed numbers  $\frac{2.8 \cdot 2.9}{7.5 \cdot 3}$ .

$$\frac{2829}{753} = 3\frac{570}{753}$$
. Ans.

12. Reduce to whole or mixed numbers  $\frac{299}{23}$ .

$$\frac{299}{28} = 13$$
. Ans.

13. Reduce to whole or mixed numbers 529.

$$\frac{529}{29} = 18\frac{7}{29}$$
. Ans.

14. Reduce to whole or mixed numbers  $\frac{7.8}{4.2}$ .

$$\frac{786}{42} = 1839$$
. Ans.

15. Reduce to whole or mixed numbers \$275.

$$\frac{8975}{25} = 359$$
. Ans.

# EXERCISE XIX.

1. Reduce to improper fractions 34.

$$3\frac{4}{9} = \frac{81}{9}$$
. Ans.

2. Reduce to improper fractions  $5\frac{9}{10}$ .

$$5\frac{9}{10} = \frac{59}{10}$$
. Ans.

3. Reduce to improper fractions  $12\frac{4}{11}$ .

$$12\frac{4}{11} = \frac{136}{11}$$
. Ans.

4. Reduce to improper fractions  $10_{1}^{7}$ .

$$10\frac{7}{19} = \frac{197}{19}$$
. Ans.

5. Reduce to improper fractions 8\$.

$$83 = 59$$
. Ans.

6. Reduce to improper fractions 12+3.

$$12\frac{18}{15} = \frac{198}{15}$$
. Ans.

7. Reduce to improper fractions  $84\frac{1}{2}$ .

$$84\frac{17}{20} = \frac{1697}{20}$$
. Ans.

8. Reduce to improper fractions 864 13.

$$864\frac{13}{97} = \frac{83821}{97}$$
. Ans.

9. Reduce to improper fractions  $41_{788}$ .

Reduce to improper fractions 41, 10 and 10.

11. Reduce to improper fractions 400133.

$$400\frac{127}{400} = \frac{1601117}{400}$$
, Ans.

Reduce to improper fractions 5000 white.

$$5000_{388} = \frac{15000088}{2008}$$
. Ans.

14. Reduce to improper fractions 3001 A.E.

15. Reduce to improper fractions 7373.

16. Express 8, 7, 3, 5, 12, 13, 18, 29, 25 in the form of fractions, each having 5 for a denominator.

17. Express 21 in the form of fractions, having for denominators 3, 5, 7, 8, 12, 13, 20, 25, 30, 37.

Express 12, 15, 23 in the form of fractions, each having for sators 12, 15, 23, respectively.

### EXERCISE XX.

- 1. Reduce to lowest terms  $\frac{120}{192}$ .  $\frac{120}{120} = \frac{15}{24} = \frac{5}{8}$ . Ans.
- 2. Reduce to lowest terms  $\frac{105}{185}$ .  $\frac{105}{185} = \frac{21}{27} = \frac{7}{2}$ . Ans.
- 3. Reduce to lowest terms  $\frac{928}{1820}$ .  $\frac{928}{1820} = \frac{116}{165}$ . Ans.
- 4. Reduce to lowest terms  $\frac{1728}{2448}$ .  $\frac{1728}{2448} = \frac{216}{806} = \frac{108}{158} = \frac{12}{17}$ . Ans.
- 5. Reduce to lowest terms  $\frac{1396}{6561}$ .  $\frac{1396}{8561} = \frac{144}{25} = \frac{16}{81}$ . Ans.
- 6. Reduce to lowest terms  $\frac{2310}{3080}$ .  $\frac{2310}{3080} = \frac{231}{308} = \frac{21}{28} = \frac{3}{4}$ . Ans.
- 7. Reduce to lowest terms  $\frac{1848}{2352}$ .  $\frac{1848}{2352} = \frac{281}{294} = \frac{77}{88} = \frac{7}{8}$ . Ans.
- 8. Reduce to lowest terms  $\frac{3960}{12672}$ .  $\frac{3960}{12672} = \frac{495}{1584} = \frac{55}{176} = \frac{5}{16}$ . Ans.
- 9. Reduce to lowest terms  $\frac{1848}{8003}$ .  $\frac{1848}{8003} = \frac{616}{1001} = \frac{88}{143} = \frac{8}{13}$ . Ans.
- 10. Reduce to lowest terms  $\frac{924}{1092}$ .  $\frac{924}{1092} = \frac{281}{278} = \frac{77}{91} = \frac{11}{18}$ . Ans.
- 11. Reduce to lowest terms  $\frac{2540}{2570} = \frac{88}{99} = \frac{8}{9}$ . Ans.
- 12. Reduce to lowest terms  $\frac{824}{1092}$ .  $\frac{824}{1092} = \frac{81}{278} = \frac{27}{91}$ . Ans.

- 13 Reduce to lowest terms  $\frac{6783}{9703}$ .  $\frac{6782}{9703} = \frac{1683}{2277} = \frac{153}{207} = \frac{17}{23}$ . Ans.
- 14. Reduce to lowest terms  $\frac{6840}{27360}$ .  $\frac{6840}{27360} = \frac{171}{684} = \frac{19}{76} = \frac{1}{4}$ . Ans.
- 15. Reduce to lowest terms  $\frac{5760}{760}$ .  $\frac{5760}{760} = \frac{576}{760} = \frac{144}{145}$ . Ans.
- 16. Reduce to lowest terms  $\frac{875}{10000}$ .  $\frac{875}{10000} = \frac{7}{80}$ . Ans.
- 17. Reduce to lowest terms  $\frac{2308}{4140}$ .  $\frac{552}{1085} = \frac{184}{845} = \frac{8}{15}$ . Ans.
- 18. Reduce to lowest terms  $\frac{181}{186}$ .  $\frac{1915}{186} = \frac{85}{54}$ . Ans.
- 19. Reduce to lowest terms  $\frac{516}{2107}$ .  $\frac{516}{2107} = \frac{12}{45}$ . Ans.
- 20. Reduce to lowest terms  $\frac{3872}{92807}$ .  $\frac{8872}{92807} = \frac{352}{8437} = \frac{32}{767}$ .
- 21. Reduce to lowest terms 33473.

G. C. M. = 809.  $\frac{78478}{94658} = \frac{97}{117}$ . Ans.

22. Reduce to lowest terms \( \frac{175}{26145} \).

G. C. M. = 83.  $\frac{15325}{15325} = \frac{113}{113}$ . Ans.

23. Reduce to lowest terms #4827.

G. C. M. = 127. \$1839 - \$17. Ans.

luce to lowest terms 1241.

$$3 \ | 339$$
 $113)1243(11$ 
 $1243$ 
 $= 113.$ 
 $\frac{349}{1243} = \frac{4}{12}.$  Ans.

25. Reduce to lowest terms 1177.

$$11 \underbrace{1177}_{107} \underbrace{2675}_{2675} \underbrace{(25)}_{214}$$
G. C. M. = 107.  $\underbrace{535}_{1177} = \underbrace{11}_{25}$ . Ans.

26. Reduce to lowest terms 11448.

27. Reduce to lowest terms 14141.

$$14141)16289(1)$$

$$14141$$

$$12\sqrt{2148}$$

$$179)14141(79)$$

$$\frac{1253}{1611}$$

$$1611$$

$$\frac{14141}{1611} = \frac{1611}{1611}$$

$$Ans.$$

- 28. Reduce to lowest terms  $\frac{481488}{104488}$ .  $\frac{881488}{104488} = \frac{882884}{31987}$ . Ans.
- 29. Reduce to lowest terms  $\frac{65065}{999999} = \frac{65}{999}$ . Ans. Divide both terms by 1001.

# Exercise XXI.

1. Find the product of  $\frac{2}{3} \times 2$ .

$$\frac{3}{4} \times \frac{2}{1} = \frac{3}{2} - 1\frac{1}{2}$$
. Ans.

2. Find the product of  $\frac{1}{2} \times 9$ .

$$\frac{3}{4} \times \frac{9}{1} = \frac{27}{4} = 6\frac{3}{4}$$
. Ans.

3. Find the product of  $10 \times \frac{3}{4}$ .

$$\frac{2}{19} \times \frac{2}{5} = 4$$
. Ans.

4. Find the product of  $15 \times \frac{3}{4}$ .

$$\frac{15}{1} \times \frac{3}{3} = 15$$
. Ans.

5. Find the product of  $\frac{9}{21} \times 7$ .

$$\frac{3}{21} \times \frac{7}{1} = 3$$
. Ans.

6. Find the product of  $16 \times \frac{4}{5}$ .

$$\frac{2}{16} \times \frac{5}{8} = 10$$
. Ans.

7. Find the product of  $\frac{2}{3} \times 2$ .

$$\frac{5}{8} \times \frac{2}{1} = \frac{5}{4} = 1\frac{1}{4}$$
. Ans.

8. Find the product of  $\frac{2}{15} \times 5$ .

$$\frac{2}{15} \times \frac{5}{1} - \frac{2}{3}$$
. Ans.

9. Find the product of  $27 \times \$$ .

$$\frac{\frac{3}{27}}{1} \times \frac{5}{9} = 15$$
. Ans.

10. Find the product of  $\frac{18}{18} \times 2$ .

$$\frac{13}{20} \times \frac{2}{1} = \frac{13}{10} = 1_{10}^{3}. Ans.$$

11. Find the product of  $\frac{18}{18} \times 3$ .

$$\frac{13}{20} \times \frac{3}{1} = \frac{39}{20} = 1\frac{19}{20}$$
. Ans.

12. Find the product of  $\frac{18}{25} \times 4$ .

$$\frac{13}{20} \times \frac{4}{1} = \frac{13}{5} = 2\frac{3}{5}. Ans.$$

13. Find the product of  $5 \times \frac{1}{2}$ .

$$\frac{5}{1} \times \frac{13}{20} = \frac{13}{4} = 3\frac{1}{4}$$
. Ans.

14. Find the product of  $6 \times \frac{1}{2}$ .

$$\frac{3}{1} \times \frac{13}{20} = \frac{39}{10} = 3\frac{9}{10}. Ans.$$

15. Find the product of  $7 \times \frac{18}{20}$ .

$$\frac{7}{1} \times \frac{13}{20} = \frac{91}{20} = 4\frac{11}{20}$$
. Ans.

16. Find the product of  $8 \times \frac{18}{26}$ .

$$\frac{2}{1} \times \frac{13}{20} = \frac{26}{5} = 5\frac{1}{8}. Ans.$$

17. Find the product of  $\frac{13}{25} \times 10$ .

$$\frac{13}{20} \times \frac{10}{1} = \frac{13}{2} = 6\frac{1}{2}. Ans.$$

18. Find the product of  $\frac{1}{28} \times 12$ 

$$\frac{13}{29} \times \frac{12}{1} = \frac{39}{5} = 7\frac{4}{5}. Ans.$$

19. Find the product of  $\frac{18}{20} \times 15$ .

$$\frac{13}{20} \times \frac{\cancel{15}}{\cancel{1}} = \frac{39}{4} = 9\frac{3}{4}. Ans.$$

20. Find the product of  $\frac{1}{4}$   $\times$  20.

$$\frac{13}{20} \times \frac{20}{1} = 13$$
. Ans.

### EXERCISE XXII.

1. Simplify  $\frac{2}{3}$  of  $\frac{7}{11}$ .

$$\frac{2}{3} \times \frac{7}{11} = \frac{14}{33}$$
. Ans.

2. Simplify  $\frac{3}{7}$  of  $2\frac{1}{10}$ .

$$\frac{3}{7} \times 2_{\frac{1}{10}} = \frac{3}{7} \times \frac{21}{10} = \frac{9}{10}$$
. Ans.

3. Simplify \$ of \$.

$$\frac{3}{7} \times \frac{5}{9} = \frac{5}{21}$$
. Ans.

4. Simplify 
$$2\frac{2}{5} \times 2\frac{1}{2}$$
.  
 $2\frac{2}{5} \times 2\frac{1}{2} = \frac{12}{5} \times \frac{5}{2} = 6$ . Ans.

5. Simplify  $44 \times 21$ .

$$4\frac{4}{5} \times 2\frac{1}{7} = \frac{24}{5} \times \frac{\cancel{15}}{7} = \frac{72}{7} = 10\frac{2}{7}$$
. Ans.

6. Simplify  $45 \times 91$ .

$$4\frac{5}{6} \times 9\frac{1}{8} = \frac{29}{\cancel{6}} \times \frac{\cancel{28}}{3} = \frac{406}{9} = 45\frac{1}{9}. \text{ Ans.}$$

7. Simplify  $\frac{1}{2}$  of  $\frac{3}{2}$  of 10.

$$\frac{1}{3} \times \frac{3}{5} \times \frac{\cancel{10}}{1} = 2. \text{ Ans.}$$

8. Simplify 3 of 3 of 3.

$$\frac{2}{3} \times \frac{3}{4} \times \frac{2}{3} = \frac{1}{3}$$
. Ans.

9. Simplify  $\frac{4}{5} \times \frac{3}{5} \times \frac{3}{5}$  of  $4\frac{1}{5}$ .

$$\frac{4}{5} \times \frac{5}{6} \times \frac{3}{7} \times 4\frac{1}{5} = \frac{2}{\cancel{5}} \times \frac{\cancel{5}}{\cancel{5}} \times \frac{\cancel{5}}{\cancel{5}} \times \frac{\cancel{3}}{\cancel{5}} \times \frac{\cancel{21}}{5} = \frac{6}{5} = 1\frac{1}{5}. \text{ Ans.}$$

10. Simplify # of 41.

$$\frac{5}{6} \times 4\frac{1}{3} = \frac{5}{6} \times \frac{9}{2} = \frac{15}{4} = 3\frac{3}{4}. Ans.$$

11. Simplify # of # of # of # of # of 15#.

$$\frac{8}{9} \times \frac{9}{10} \times \frac{5}{7} \times \frac{3}{4} \times \frac{1}{5} \times 15 = \frac{\cancel{3}}{\cancel{9}} \times \frac{\cancel{9}}{\cancel{19}} \times \frac{\cancel{5}}{\cancel{7}} \times \frac{\cancel{3}}{\cancel{4}} \times \frac{1}{\cancel{5}} \times \frac{\cancel{93}}{\cancel{4}} = \frac{27}{20} = 1 \frac{\cancel{7}}{\cancel{20}}. \quad Ans.$$

12. Simplify  $5\frac{3}{4} \times 8\frac{3}{4}$ .

$$5\frac{3}{4} \times 8\frac{3}{5} = \frac{23}{4} \times \frac{42}{5} = \frac{483}{10} = 48\frac{3}{10}$$
. Ans.

13. Simplify  $\frac{1}{4} \times \frac{1}{4} \times \frac{7}{15} \times 7\frac{1}{2}$ .

$$\frac{2}{3} \times \frac{4}{7} \times \frac{7}{15} \times 7\frac{1}{2} - \frac{2}{3} \times \frac{4}{7} \times \frac{7}{15} \times \frac{15}{2} - \frac{4}{3} - 1\frac{1}{3}$$
. Ans.

14. Simplify \( \frac{2}{3} \) of \( \frac{2}{20} \) of 8\( \frac{1}{3} \).

$$\frac{3}{5} \times \frac{10}{27} \times \frac{9}{20} \times 8\frac{1}{3} - \frac{3}{5} \times \frac{10}{27} \times \frac{9}{20} \times \frac{25}{3} - \frac{5}{6}. \text{ Ans.}$$

15. Simplify  $\frac{1}{11} \times \frac{2}{2} \frac{1}{1} \times \frac{2}{4} \frac{1}{8} \times 2\frac{1}{1} \frac{1}{8}$ .

$$\frac{8}{11} \times \frac{20}{21} \times \frac{35}{48} \times 2\frac{10}{10} - \frac{8}{11} \times \frac{20}{21} \times \frac{35}{48} \times \frac{48}{19} - \frac{800}{627} - 1\frac{178}{627}. Ans.$$

16. Simplify 
$$\frac{43}{43} \times \frac{18}{105} \times 1_{808}$$
. 9
$$\frac{21}{21} \times \frac{3}{105} \times 1_{808} = \frac{21}{43} \times \frac{13}{105} \times \frac{315}{308} = \frac{117}{946}$$
. Ans.

17. Simplify  $\frac{5}{8} \times \frac{120}{121} \times \frac{55}{85} \times 17$ .

$$\frac{5}{5} \times \frac{120}{121} \times \frac{66}{85} \times \frac{17}{1} = \frac{90}{11} = 8\frac{2}{11}. Ans.$$

**18.** Simplify  $\frac{28}{58} \times \frac{29}{59} \times \frac{29}{58} \times 1\frac{29}{29}$ .

$$\frac{38}{39} \times \frac{52}{57} \times \frac{69}{86} \times 1_{\frac{20}{23}} = \frac{\cancel{38}}{\cancel{39}} \times \frac{\cancel{52}}{\cancel{57}} \times \frac{\cancel{69}}{\cancel{59}} \times \frac{\cancel{43}}{\cancel{23}} = \frac{4}{3} - 1_{\frac{1}{2}}. \text{ Ans.}$$

19. Simplify  $\frac{1}{2}$  of  $\frac{3}{8}$  of  $\frac{3}{4}$  of  $\frac{3}{8}$  of  $\frac{3}{8}$  of  $\frac{3}{8}$  of  $\frac{3}{10}$  of 10.  $\frac{1}{2} \times \frac{2}{3} \times \frac{3}{4} \times \frac{4}{5} \times \frac{5}{6} \times \frac{6}{7} \times \frac{7}{8} \times \frac{8}{9} \times \frac{9}{19} \times \frac{10}{1} = 1. \text{ Ans.}$ 

20. Simplify  $\frac{7}{25}$  of  $\frac{8}{11}$  of 30.

$$\frac{7}{25} \times \frac{8}{11} \times \frac{30}{1} = \frac{336}{55} = 6\frac{6}{55}. Ans.$$

21. Simplify  $\frac{118}{868} \times \frac{85}{226} \times \frac{13}{85} \times 1\frac{3}{4}$ .

$$\frac{113}{355} \times \frac{85}{226} \times \frac{12}{35} \times 1\frac{2}{4} = \frac{113}{355} \times \frac{17}{355} \times \frac{17}{22} \times \frac{17}{35} \times \frac{17}{4} = \frac{51}{710}. \text{ Ans.}$$

22. Simplify  $\frac{7}{8} \times \frac{3}{4} \times \frac{3}{21} \times \frac{4}{5}$  of  $\frac{5}{8}$  of  $\frac{3}{4}$  of 8.  $\frac{7}{8} \times \frac{3}{4} \times \frac{8}{21} \times \frac{4}{5} \times \frac{5}{8} \times \frac{3}{4} \times \frac{8}{1} = \frac{3}{4}. \text{ Ans.}$ 

**23.** Simplify  $\frac{2}{18}$  of  $\frac{89}{40}$  of  $\frac{52}{117}$ .

$$\frac{\cancel{2}}{\cancel{13}} \times \frac{\cancel{39}}{\cancel{49}} \times \frac{\cancel{52}}{\cancel{117}} = \frac{1}{15}. Ans.$$

24. Simplify  $\frac{7}{11} \times \frac{7}{12} \times \frac{33}{63} \times 48$ .

$$\frac{g}{11} \times \frac{7}{12} \times \frac{27}{63} \times \frac{28}{1} = 8. \text{ Ans.}$$

25. Simplify \(\frac{2}{4}\) of \(\frac{7}{6}\) of \(\frac{2}{2}\) of 12.

$$\frac{\cancel{5}\cancel{5}\cancel{5}}{\cancel{4}\cancel{5}} \times \frac{\cancel{7}\cancel{5}\cancel{5}}{\cancel{5}\cancel{5}} \times \frac{\cancel{5}\cancel{5}\cancel{5}}{\cancel{4}\cancel{2}} \times \frac{\cancel{1}\cancel{2}}{\cancel{1}} - \frac{3}{\cancel{4}}. Ans.$$

26. Simplify 13 of 41 of 8.

$$1\frac{3}{8} \times 4\frac{1}{2} \times \frac{3}{8} = \frac{5}{8} \times \frac{9}{2} \times \frac{3}{8} = \frac{45}{16} = 2\frac{14}{16}$$
. Ans.

27. Simplify  $2\frac{4}{5} \times 1\frac{3}{7} \times 1\frac{1}{12} \times 8$ .

$$24 \times 14 \times 114 \times 8 = \frac{22}{9} \times \frac{\cancel{10}}{\cancel{7}} \times \frac{\cancel{28}}{\cancel{15}} \times \frac{8}{1} = \frac{1408}{27} = 52\cancel{4}$$
. Ans.

**28.** Simplify  $3\frac{1}{7}$  of  $2\frac{1}{3}$  of  $1\frac{4}{13}$  of  $1\frac{4}{11}$ .

$$3\frac{5}{7} \times 2\frac{1}{2} \times 1\frac{5}{15} \times 1\frac{4}{15} = \frac{\frac{2}{2}}{7} \times \frac{5}{2} \times \frac{\frac{21}{2}}{7} \times \frac{15}{11} = \frac{225}{11} = 20\frac{5}{11}$$
. Ans

29. Simplify  $\frac{11}{12} \times 5\frac{1}{12} \times 4\frac{1}{12} \times \frac{7}{12} \times 5$ .

$$\frac{11}{12} \times 5\frac{1}{8} \times 4\frac{1}{8} \times \frac{7}{22} \times 5 = \frac{11}{12} \times \frac{\cancel{16}}{\cancel{3}} \times \frac{\cancel{33}}{\cancel{3}} \times \frac{7}{\cancel{22}} \times \frac{5}{1} = \frac{385}{12} = 32\frac{1}{12}. \text{ Ans.}$$

**30.** Simplify  $\frac{2}{5}$  of  $\frac{7}{15} \times 8\frac{2}{7} \times \frac{6}{29}$  of  $1\frac{1}{15}$ .

$$\frac{2}{5} \times \frac{7}{15} \times 83 \times \frac{6}{29} \times 117 = \frac{2}{5} \times \frac{7}{15} \times \frac{2}{5} \times \frac{2}{7} \times \frac{2}{5} \times \frac{7}{15} = \frac{28}{45}. Ans.$$

Simplify \( \frac{1}{4} \times \frac{1}{44} \).

$$\frac{17}{82} \times \frac{9}{27} \times \frac{123}{183} = \frac{9}{76}. Ans.$$

$$\frac{17}{2} \times \frac{9}{38} \times \frac{123}{183} = \frac{9}{76}.$$

82. Simplify ##× ##× ##

$$\frac{292}{468} \times \frac{191}{657} \times \frac{8}{1719} - \frac{32}{406}. Ans.$$
155 9 9

88. Simplify 1988 of 1888.

$$\frac{\frac{5}{1295}}{\frac{2763}{9}} \times \frac{\frac{2}{112}}{\frac{2169}{9}} \times \frac{\frac{5}{1555}}{\frac{1968}{1968}} = \frac{50}{243}. Ans.$$

#### EXERCISE XXIII.

Divide ## by 6.

$$\frac{24}{35} + 6 = \frac{1}{6} \times \frac{24}{35} = \frac{4}{35}$$
. Ans.

$$\frac{10}{11} + 5 = \frac{\frac{2}{19}}{11} \times \frac{1}{\beta} = \frac{2}{11}. Ans.$$

le 
$$\frac{3}{8}$$
 by 8.  
 $\frac{1}{8} \times \frac{3}{7} = \frac{3}{56}$ . Ans.

$$18\frac{1}{4} + 7 = \frac{1}{7} \times \frac{\frac{8}{39}}{3} = 2\frac{1}{4}$$
. And

$$\frac{5}{8} + \frac{3}{4} = \frac{4}{3} \times \frac{5}{8} = \frac{5}{6}.$$
 Ans

1. Divide 
$$\frac{14}{15}$$
 by 6.

$$\frac{24}{35} + 6 = \frac{1}{5} \times \frac{24}{35} = \frac{4}{35}. \text{ Ans.}$$
2. Divide  $\frac{14}{17}$  by 5.
$$\frac{10}{11} + 5 = \frac{19}{11} \times \frac{1}{5} = \frac{2}{11}. \text{ Ans.}$$
3. Divide  $\frac{1}{17}$  by 5.
$$\frac{1}{8} + \frac{3}{4} = \frac{4}{3} \times \frac{5}{3} = \frac{5}{6}. \text{ Ans.}$$
4. Divide  $18\frac{3}{5}$  by 7.

$$\frac{1}{8} + 7 = \frac{1}{7} \times \frac{35}{3} = 2\frac{3}{5}. \text{ Ans.}$$
5. Divide  $\frac{3}{5}$  by  $\frac{3}{5}$ .
$$\frac{5}{8} + \frac{3}{4} = \frac{4}{3} \times \frac{5}{3} = \frac{5}{6}. \text{ Ans.}$$
6. Divide  $\frac{1}{12}$  by  $\frac{3}{5}$ .
$$\frac{12}{16} + \frac{3}{8} = \frac{5}{3} \times \frac{12}{16} = 2. \text{ Ans.}$$

$$\frac{12}{16} + \frac{3}{8} = \frac{5}{3} \times \frac{12}{16} = 2. \text{ Ans.}$$

$$1\frac{1}{4} + 3\frac{1}{4} = \frac{7}{4} + \frac{10}{3} = \frac{3}{10} \times \frac{7}{4} = \frac{21}{40}$$
. Ans.

8. Divide 51 by 43.

$$5\frac{1}{5} + 4\frac{2}{5} = \frac{26}{5} + \frac{14}{3} = \frac{3}{14} \times \frac{26}{5} = \frac{39}{35} = 1\frac{4}{55}$$
. Ans.

9. Divide 83 by 41.

$$8\frac{2}{9} + 4\frac{1}{9} = \frac{74}{9} + \frac{37}{9} = \frac{9}{37} \times \frac{74}{9} = 2$$
. Ans.

10. Divide 71 by 41.

$$7\frac{1}{5} + 4\frac{3}{7} = \frac{36}{5} + \frac{30}{7} = \frac{7}{39} \times \frac{39}{5} = \frac{42}{25} = 1\frac{17}{25}$$
. Ans.

11. Divide 
$$6\frac{3}{4}$$
 by  $9\frac{1}{2}$ .
$$6\frac{3}{4} + 9\frac{1}{2} = \frac{27}{4} + \frac{19}{2} = \frac{2}{19} \times \frac{27}{4} = \frac{27}{38}. \text{ Ans.}$$

12. Divide 84 by 44.

$$8\frac{2}{3} + 4\frac{2}{3} = \frac{26}{3} + \frac{14}{3} = \frac{3}{14} \times \frac{23}{3} = \frac{13}{7} = 1\frac{2}{7}$$
. Ans.

13. Divide 3 by 14.

$$3\frac{3}{9} + \frac{14}{27} = \frac{35}{9} + \frac{14}{27} = \frac{27}{14} \times \frac{35}{9} = \frac{15}{2} = 7\frac{1}{4}$$
. Ans.

14. Divide 
$$4\frac{9}{7}$$
 by  $6\frac{9}{7}$ .  
 $4\frac{9}{7} + 6\frac{9}{7} = \frac{31}{7} + \frac{62}{9} = \frac{9}{62} \times \frac{31}{7} = \frac{9}{14}$ . Ans.

15. Divide 5 by 43.  

$$5 + 43 = 5 + \frac{30}{7} - \frac{7}{39} \times \frac{5}{1} = \frac{7}{6} = 1\frac{1}{6}$$
. Ans.

16. Divide 34 of 21 by 11 of 21.

$$3\frac{1}{8}$$
 of  $2\frac{1}{4} + 1\frac{1}{4}$  of  $2\frac{1}{6} = \frac{19}{5}$  of  $\frac{5}{2} + \frac{3}{2}$  of  $\frac{19}{9} = \frac{19}{5} \times \frac{5}{2} \times \frac{2}{5} \times \frac{2}{19} = 3$ . Ans.

17. Divide 23 by 31 of 115.

$$2\frac{3}{7} + 3\frac{1}{8} \text{ of } 1\frac{1}{15} = \frac{16}{7} + \frac{10}{3} \text{ of } \frac{16}{15} = \frac{16}{7} \times \frac{3}{16} \times \frac{3}{16} = \frac{9}{14}.$$
 Ans.

18. Divide 24 of 51 by 74.

$$2\frac{9}{11} \text{ of } 5\frac{1}{2} + 7\frac{9}{4} = \frac{31}{11} \text{ of } \frac{11}{2} + \frac{31}{4} = \frac{81}{11} \times \frac{11}{2} \times \frac{2}{4} = 2. \text{ Ans.}$$

19. Divide 5% of 8% of 1% by 2% of 5%.

5) of 8) of 1) + 2\frac{1}{10} of 5) = 
$$\frac{28}{5}$$
 of  $\frac{25}{3}$  of  $\frac{11}{7}$  +  $\frac{21}{10}$  of  $\frac{50}{9}$ 

$$-\frac{28}{5} \times \frac{25}{5} \times \frac{11}{7} \times \frac{19}{21} \times \frac{9}{59} = \frac{44}{7} = 6$$
). Ans.

#### EXERCISE XXIV.

Express with least common denominator 1, 3, 4.

L. C. D. = 
$$2 \times 3 \times 5 = 30$$
.

$$\frac{1}{2}$$
,  $\frac{2}{5}$ ,  $\frac{5}{6} = \frac{15}{30} = \frac{25}{30}$ . Ans.

2. Express with least common denominator \$, \$, \$, \$,

L. C. D. 
$$= 2^8 \times 3^8 \times 5 = 360$$
.

$$\frac{2}{3}$$
,  $\frac{5}{9}$ ,  $\frac{7}{8}$ ,  $\frac{9}{10} = \frac{240 + 200 + 315 + 324}{360}$ . Ans.

s with least common denominator §, ‡, ‡, ‡.

**L.** C. D. 
$$-2^{6} \times 3 \times 5 \times 7 - 840$$
.

$$\frac{1}{8}$$
,  $\frac{5}{21}$ ,  $\frac{19}{35} = \frac{700 \quad 105 \quad 200 \quad 456}{840}$ . Ans.

s with least common denominator 💤, 💤, 🔩, 🔩.

**L.** C. D. = 
$$2^a \times 3^a \times 5^a = 800$$
.

, 
$$\frac{7}{20}$$
,  $\frac{3}{25}$ ,  $\frac{8}{45} = \frac{120 - 315 - 108 - 160}{800}$ . Ans.

5. Express with least common denominator  $\frac{12}{25}$ ,  $\frac{17}{40}$ ,  $\frac{13}{85}$ ,  $\frac{19}{45}$ .

L. C. D. = 
$$2^3 \times 3 \times 5^2 = 600$$
.

$$\frac{12}{25}$$
,  $\frac{17}{40}$ ,  $\frac{13}{60}$ ,  $\frac{19}{75} = \frac{288}{600} = \frac{255}{600} = \frac{130}{600}$ . Ans.

6. Express with least common denominator \$, \frac{7}{80}, \frac{4}{85}, \frac{28}{28}, \frac{12}{22}.

L. C. D. = 
$$2^8 \times 3 \times 5 \times 7 = 840$$
.

$$\frac{3}{8}$$
,  $\frac{7}{30}$ ,  $\frac{4}{35}$ ,  $\frac{3}{28}$ ,  $\frac{19}{24} = \frac{315}{840}$   $\frac{196}{840}$   $\frac{96}{840}$ . Ans.

7. Express with least common denominator  $\frac{1}{16}$ ,  $\frac{7}{18}$ ,  $\frac{28}{26}$ ,  $\frac{28}{57}$ .

L. C. D. = 
$$2^4 \times 3^3 \times 5 = 2160$$
.

$$\frac{11}{16}$$
,  $\frac{7}{18}$ ,  $\frac{13}{20}$ ,  $\frac{23}{30}$ ,  $\frac{17}{54} = \frac{1485}{2160}$  840 1404 1656 680. Ans.

8. Which is the greater,  $\frac{13}{20}$  or  $\frac{17}{25}$ ?  $\frac{5}{6}$  or  $\frac{7}{3}$ ?  $\frac{3}{5}$  or  $\frac{7}{12}$ ?

L. C. D. =  $2^2 \times 5^2 = 100$ . L. C. D. =  $2 \times 3^2 = 18$ . L. C. D. =  $5 \times 12 = 60$ .

$$\frac{13}{20} = \frac{65}{100}$$

$$\frac{17}{28} = \frac{68}{100}.$$

$$\frac{5}{6} = \frac{15}{18},$$
  $\frac{3}{5} = \frac{36}{60},$ 

$$\frac{7}{9} = \frac{14}{18}$$

$$\frac{3}{5} = \frac{36}{60}$$

$$\frac{7}{9} = \frac{14}{18}. \qquad \qquad \frac{7}{12} = \frac{35}{60}.$$

.. \frac{17}{6} is the greater. .. \frac{5}{6} is the greater. .. \frac{5}{6} is the greater.

9. Arrange the fractions  $\frac{7}{12}$ ,  $\frac{1}{18}$ ,  $\frac{1}{24}$  in order of magnitude.

L. C. D. 
$$= 2^3 \times 3^2 = 72$$
.

$$\frac{7}{12} = \frac{42}{72}$$

$$\frac{11}{18} = \frac{44}{72}$$

$$\frac{13}{24} = \frac{39}{72}$$

$$\frac{7}{12} = \frac{42}{72}$$
,  $\frac{11}{18} = \frac{44}{72}$ ,  $\frac{13}{24} = \frac{39}{72}$ .  $\frac{13}{24}$ ,  $\frac{7}{12}$ ,  $\frac{11}{18}$ . Ans.

10. Arrange the fractions  $\frac{5}{12}$ ,  $\frac{8}{15}$ ,  $\frac{4}{11}$ ,  $\frac{7}{18}$  in order of magnitude.

L. C. D. = 
$$2^2 \times 3^2 \times 5 \times 11 = 1980$$
.

$$\frac{5}{12}$$
,  $\frac{8}{15}$ ,  $\frac{4}{11}$ ,  $\frac{7}{18} = \frac{825}{1980}$ 

$$\frac{4}{11}$$
,  $\frac{7}{18}$ ,  $\frac{5}{12}$ ,  $\frac{8}{15}$ . Ans.

#### EXERCISE XXV.

$$\frac{1}{2} + \frac{3}{2} - \frac{4}{2} = 2$$
. Ans.

2. Find the sum of 
$$\frac{1}{4} + \frac{3}{8} + \frac{1}{4}$$
.

$$\frac{1}{3} + \frac{2}{3} + \frac{1}{3} - \frac{4}{3} - 1\frac{1}{4}$$
. Ans.

$$\frac{1}{4} + \frac{1}{4} + \frac{3}{4} = \frac{5}{4} = 1\frac{1}{4}$$
. Ans.

$$1\frac{1}{2} + 2\frac{1}{2} = 3\frac{1+1}{2} = 4$$
. Ans.

5. Find the sum of 
$$1\frac{1}{4} + 2\frac{1}{4}$$
.  $1\frac{1}{4} + 2\frac{1}{4} = 3\frac{1+2}{4} = 4$ . Ans.

$$2\frac{1}{6} + 3\frac{1}{6} = 5\frac{3+4}{6} = 6\frac{1}{6}$$
. Ans.

$$1\frac{7}{4} + \frac{4}{3} = 1\frac{7+2}{3} = 2\frac{1}{4}$$
. Ans.

$$\frac{9}{17} + \frac{3}{17} + \frac{14}{17} + \frac{11}{17} - \frac{37}{17} = 2\frac{1}{17}$$
. Ans.

sum of 
$$84 + 64 + 54 + 14$$
.

$$5\frac{1}{4} + 6\frac{1}{4} + 5\frac{1}{4} + \frac{1}{4} = 19\frac{1}{4} = 21\frac{1}{4}$$
. Ans.

sum of 
$$\frac{1}{4} + \frac{1}{4}$$
.

$$\frac{+25}{10} = 113$$
. Ans.

$$\frac{+7}{8} = 1\frac{8}{4}$$
. Ans.

$$\frac{+1}{6} = \frac{2}{3}$$
. Ans.

L. C. D. 
$$-2^{4} \times 3 \times 5 = 60$$
.

$$\frac{16+33}{60} = \frac{49}{60}. \quad Ans.$$

15. Find the sum of 
$$\frac{4}{18} + \frac{11}{14}$$
.

L. C. D. 
$$= 2^4 \times 3 = 48$$
.

$$\frac{15+22}{48}=\frac{37}{48}. \ Ans.$$

16. Find the sum of 
$$12\frac{n}{4} + 7\frac{n}{4}$$
.  $12\frac{n}{4} + 7\frac{n}{4} = 19\frac{1}{16} = 19\frac{1}{16}$ . Ans

Find the sum of  $85 \frac{1}{12} \times 27 \frac{11}{12}$ .

$$85\frac{7}{12} \times 27\frac{11}{12} = 112\frac{11+22}{26} = 113\frac{7}{16}$$
. Ans.

18. Find the sum of 
$$\frac{1}{2} + \frac{1}{4} + \frac{1}{4} + \frac{1}{4}$$
.

L. C. D. = 
$$2^3 \times 3 \times 5 = 60$$
.  

$$\frac{30 + 20 + 15 + 12}{60} = \frac{77}{60} = 1\frac{17}{60}$$
. Ans.

19. Find the sum of 
$$\frac{1}{4} + \frac{3}{4} + \frac{3}{4} + \frac{4}{5}$$
.

L.C. D. = 
$$2^2 \times 3 \times 5 = 60$$
.  
 $\frac{30 + 40 + 45 + 48}{60} = \frac{163}{60} = 2\frac{13}{60}$ . Ans.

20. Find the sum of 
$$\frac{5}{8} + \frac{11}{12} + \frac{3}{18} + \frac{7}{20} + \frac{18}{18}$$
.

L. C. D. 
$$= 2^2 \times 3 \times 5 = 60$$
.

$$\frac{50+55+32+21+26}{60} = \frac{184}{60} = 3\frac{1}{16}$$
. Ans.

21. Find the sum of 
$$5\frac{1}{27} + 11\frac{1}{28} + 24\frac{21}{20} + \frac{9}{50} + 17\frac{8}{15} + 14 + 11\frac{5}{12}$$
.  
L. C. D. =  $2^8 \times 3 \times 5^2 = 600$ .  
 $82\frac{1588}{500} = 85\frac{83}{500}$ . Ans.

$$9\frac{1}{7} + 15\frac{1}{2}\frac{1}{8} + 163\frac{1}{6}\frac{7}{8} + 1\frac{1}{2}\frac{1}{2} + 10\frac{1}{2}$$
.  
L. C. D.  $= 2^2 \times 3^2 \times 7 = 252$ .

198449 - 19947. Ans.

23. Find the sum of 
$$3\frac{2}{5} + 4\frac{2}{5} + 1\frac{5}{5} + 2.$$
L. C. D. = 2 + 3 + 5 = 30.
$$12\frac{2}{10} = 12\frac{1}{10}.$$

$$1\frac{3}{30} + 2\frac{3}{35} + 5\frac{7}{30} + \frac{4}{15}.$$
L. C. D. =  $2^2 \times 3 \times 5^2 = 300$ .
$$8\frac{319}{300} = 8\frac{78}{100}.$$

$$\frac{3}{7} + \frac{14}{14} + \frac{2}{14} + \frac{34}{14} + \frac{4}{14}$$

L. C. D. = 
$$2^8 \times 3^8 \times 7 = 504$$
.

$$10\frac{787}{584} - 11\frac{282}{584}$$
. Ans.

$$44 + 34 + 24 + 14 + 24$$

L. C. D. = 
$$2^8 \times 3^2 \times 7 = 504$$
.

$$10\frac{1}{6}\frac{1}{6}\frac{1}{4} = 11\frac{1}{6}\frac{1}{6}\frac{1}{4}$$
. Ans.

$$\frac{11}{10} + \frac{7}{40} + 10 + \frac{28}{10}$$

L. C. D. 
$$= 2^8 \times 3 \times 5 \times 7 = 840$$
.  
 $10733$ . Ans.

$$\frac{27}{50} + \frac{29}{60} + \frac{31}{80} + \frac{35}{100} + \frac{37}{240}$$
.

L. C. D. 
$$= 2^4 \times 3^2 \times 5^2 = 3600$$
.

$$\frac{6822}{1600} = 1\frac{179}{200}$$
. Ans.

$$2 + \frac{3}{4} + 1\frac{3}{5} + 4\frac{5}{5} + 5\frac{13}{5}$$
.

L. C. D. 
$$= 2^8 \times 3^2 = 72$$
.

$$12395 = 1451$$
. Ans.

30. Find the sum of  $3\frac{1}{8} + 6 + \frac{4}{11} + 2\frac{8}{16} + 5\frac{6}{16} + \frac{9}{26}$ . L. C. D.  $-2^4 \times 5 \times 11 = 880$ .  $16\frac{16}{16} = 18\frac{9}{16}$ . Ans.

81. Find the sum of  $\frac{A_0}{16} + \frac{1}{16} + \frac{3}{16} + \frac{3}{16} + \frac{1}{16} + \frac{3}{16} + \frac{3}{16} + \frac{3}{16} + \frac{3}{16} + \frac{3}{16} = 360.$  6188 = 811. Ans.

82. Find the sum of  $\frac{5}{14} + \frac{4}{11} + \frac{91}{2}.$ L. C. D. =  $2 \times 7 \times 11 = 154$ .  $\frac{9314}{2} = 1031$ . Ans.

33. Find the sum of  $20\frac{6}{13} + 11\frac{7}{20} + 5\frac{1}{2} + 305.$ L. C. D. =  $2^6 \times 3 \times 5 = 120$ .  $341\frac{1}{2}\frac{7}{2}$ . Ans.

36. Find the sum of  $\frac{11}{11} + \frac{1}{14} + \frac{1}{14}.$  L. C. D. =  $2^2 \times 3 \times 19 = 228$ ,  $\frac{111}{14}. \quad Ans.$ 

35. Find the sum of  $\frac{4}{17} + \frac{11}{14} + \frac{14}{14} + \frac{14}{14}.$   $7 \quad 7 \quad 7 \quad 204.$  = 1.45c.

36. Find the sum of  $317\frac{2}{3} + 17\frac{2}{31} + 4\frac{2}{10} + \frac{7}{10} + 6\frac{2}{3} + \frac{2}{17}$ . L. C. D. =  $2 \times 3 \times 5 \times 17 = 510$ .  $344\frac{1421}{310} = 346\frac{491}{310}$ . Ans.

87. Find the sum of  $4\frac{7}{15} + 8\frac{5}{11} + 4\frac{7}{11} + 5\frac{3}{7} + 5\frac{4}{7} + \frac{3}{7}.$ L.C. D. =  $3 \times 5 \times 7 \times 11 = 1155$ .  $26\frac{3}{7}\frac{7}{15}\frac{7}{15} = 29\frac{7}{15}\frac{7}{15}$ . Ans.

38. Find the sum of  $3\frac{1}{4} + 5\frac{4}{45} + 8\frac{7}{16} + \frac{1}{2}\frac{2}{4} + 1\frac{1}{2}\frac{2}{4}\frac{2}{4}.$ L. C. D. = 2880.  $17\frac{1}{2}\frac{1}{2}\frac{1}{4} = 18\frac{1}{2}\frac{1}{2}\frac{1}{6}$ . Ans.

89. Find the sum of  $4\frac{5}{18} + 7\frac{5}{18} + 5\frac{7}{18} + 275\frac{47}{188} + 2\frac{7}{18}$ . L. C. D. =  $2^4 \times 3 \times 7 \times 13 = 1092$ .  $293\frac{21}{18}\frac{1}{18} = 294\frac{1}{18}\frac{1}{18}$ . Ans.

40. Find the sum of  $\frac{17}{13} + 7_{12} + 6_{12} + 400_{12} + 51_{12}^{23}.$ L. C D. =  $2^{3} \times 7 \times 3 \times 11 = 1848$ .  $464_{12}^{23} = 465_{11}^{21}. Ans.$ 

#### Exercise XXVI.

alue of 52¼ - 46. = 6¼. Ans.

alue of  $\frac{4}{9} - \frac{3}{9}$ .  $\frac{3}{9} - \frac{1}{3}$ . Ans. 3. Find the value of  $\frac{3}{4} - \frac{3}{4}$ .  $\frac{3}{4} - \frac{2}{3} = \frac{9-8}{12} = \frac{1}{12}$ . Ans.

4. Find the value of  $\frac{8}{15} - \frac{5}{12} = \frac{32 - 25}{60} - \frac{7}{60}$ . Ans.

5. Find the value of 
$$\frac{11}{18} - \frac{3}{14}$$
.

$$\frac{11}{18} - \frac{3}{14} = \frac{77 - 27}{126} = \frac{50}{126} = \frac{25}{63}$$
Ans.

6. Find the value of 
$$4 - \frac{1}{2}$$
.  
 $4 - \frac{1}{2} = 3\frac{1}{2}$ . Ans.

7. Find the value of 
$$7 - \frac{2}{3}$$
.  
 $7 - \frac{2}{3} = 6\frac{1}{3}$ . Ans.

8. Find the value of 
$$3 - \frac{5}{6}$$
.  $3 - \frac{5}{6} = 2\frac{1}{6}$ . Ans.

9. Find the product of 
$$8 - \frac{3}{7}$$
.  $8 - \frac{3}{7} = 7\frac{4}{7}$ . Ans.

10. Find the product of 
$$5 - \frac{4}{5}$$
.  $5 - \frac{4}{5} = 4\frac{1}{5}$ . Ans.

11. Find the value of 
$$5 - \frac{7}{9}$$
.  $5 - \frac{7}{9} = 4\frac{2}{9}$ . Ans.

12. Find the value of 
$$6\frac{1}{3} - 5\frac{1}{6}$$
.  
 $6\frac{1}{3} - 5\frac{1}{6} = 1^{\frac{2-1}{6}} = 1\frac{1}{6}$ . Ans.

13. Find the value of 
$$4\frac{2}{3} - 3\frac{3}{7}$$
.

$$4\frac{2}{5} - 3\frac{3}{7} = 1\frac{14-15}{35} = \frac{34}{35}$$
. Ans.

14. Find the value of 
$$7\frac{1}{4} - 2\frac{8}{10}$$
.

$$7\frac{1}{8} - 2\frac{8}{10} = 5\frac{10-9}{80} = 5\frac{1}{80}$$
. Ans.

15. Find the value of 
$$7\frac{2}{3} - 4\frac{3}{3}$$
.

$$7\frac{2}{5} - 4\frac{3}{6} = 3\frac{18 - 40}{45} = 2\frac{23}{45}$$
. Ans.

16. Find the value of 
$$6\frac{3}{4} - 2\frac{3}{4}$$
.

$$6\frac{2}{8} - 2\frac{3}{4} = 4\frac{8-9}{12} = 3\frac{11}{12}$$
. Ans.

17. Find the value of 
$$9\frac{4}{5} - 4\frac{5}{5}$$
.

$$9\frac{4}{5} - 4\frac{5}{6} = 5\frac{24 - 25}{80} = 4\frac{29}{80}$$
. Ans.

18. Find the value of 
$$4\frac{2}{3} - \frac{1}{2}$$
.

$$4\frac{2}{8} - \frac{1}{2} = 4\frac{4-8}{6} = 4\frac{1}{6}$$
. Ans.

19. Find the value of 
$$6\frac{3}{4}-4\frac{3}{3}$$
.

$$6\frac{3}{4} - 4\frac{2}{8} = 2\frac{9-8}{12} = 2\frac{1}{12}$$
.

20. Find the value of 
$$7\frac{1}{4} - 2\frac{3}{4}$$
.

$$7\frac{1}{4} - 2\frac{3}{4} = 5\frac{2-8}{4} = 4\frac{3}{4}$$
. Ans.

21. Find the value of  $8\frac{1}{8}-4\frac{4}{7}$ .

$$8\frac{1}{5} - 4\frac{4}{7} = 4\frac{7-20}{85} = 3\frac{22}{85}$$

**22.** Find the value of 
$$85\frac{7}{22} - 27\frac{1}{18}$$
.

$$85\frac{7}{22} - 27\frac{1}{18} = 58\frac{68 - 121}{198} = 57\frac{149}{198} = 57\frac{79}{99}$$
. Ans.

23. Find the value of 
$$8\frac{7}{10} - 2\frac{11}{16}$$
. | 24. Find the value of  $10 - 3\frac{5}{8}$ .

$$8\frac{7}{10} - 2\frac{11}{16} = 6\frac{56 - 55}{80} = 6\frac{1}{80}$$
. Ans.

24. Find the value of 
$$10 - 3\frac{2}{3}$$
.  $10 - 3\frac{2}{3} = 6\frac{2}{3}$ . Ans.

25. Find the value of 
$$120\frac{21}{32} - 110\frac{1}{22}$$
.

$$120\frac{21}{32} - 110\frac{13}{22} = 10\frac{68 - 52}{96} = 10\frac{11}{96}. Ans.$$

**26.** Find the value of 
$$5\frac{17}{18} - \frac{27}{35}$$
.

$$5\frac{17}{28} - \frac{27}{88} = 5\frac{85 - 108}{146} = 4\frac{117}{40}$$
. Ans.

- 27. Find the value of  $13\frac{3}{40} 2\frac{15}{40}$ .  $13\frac{3}{40} 2\frac{15}{40} = 11\frac{33}{40} 10\frac{23}{40}$ . Ans.
- 28. Find the value of  $2\frac{1}{2}\frac{5}{4}$   $1\frac{1}{2}\frac{5}{4}$ .  $2\frac{1}{2}\frac{1}{4}$  —  $1\frac{1}{2}\frac{5}{4}$  =  $1\frac{604}{8}\frac{15}{8}$  =  $\frac{748}{16}$ . Ans.
- 29. Find the value of  $4 1\frac{2817}{4866}$ .  $4 - 1\frac{2817}{4866} = 2\frac{4000 - 2817}{4000} = 2\frac{1688}{4000}$ . Ans.
- 30. Find the value of  $1473 279\frac{1}{12}$ .  $1473 - 279\frac{1}{12} = 1193\frac{1}{12}$ . Ans.
- 31. Find the value of  $1473\frac{5}{18} 279\frac{1}{12}$ .  $1473\frac{5}{18} - 279\frac{1}{12} = 1194\frac{60-148}{156} = 1193\frac{78}{156}$ . Ans.
- 32. Find the value of  $1473\frac{7}{18} 279\frac{1}{12}$ .  $1473\frac{7}{18} - 279\frac{1}{12} = 1194\frac{14-88}{36} = 1193\frac{17}{16}$ . Ans.
- 33. Find the value of  $278\frac{15}{16} 30\frac{5}{12}$ .  $278\frac{15}{12} - 30\frac{5}{12} = 248\frac{45-20}{48} = 248\frac{25}{12}$ . Ans.
- 34. Find the value of  $125\frac{5}{23} 10\frac{17}{33}$ .  $125\frac{5}{23} = 10\frac{17}{33} - 115\frac{15-34}{55} = 114\frac{47}{35}$ . Ans.
- 35. Find the value of  $118\frac{5}{11} 17\frac{2}{14}$ .  $118\frac{5}{11} - 17\frac{2}{14} = 101\frac{70 - 38}{154} = 101\frac{27}{154}$ . Ans.
- 36. Find the value of  $94\frac{5}{11} 91\frac{13}{12}$ .  $94\frac{5}{11} - 91\frac{13}{12} = 3\frac{70 - 148}{154} = 2\frac{81}{154}$ . Ans.
- 37. Find the value of  $7\frac{5}{21} 2\frac{1}{2}$ .  $7\frac{5}{21} - 2\frac{1}{12} = 5\frac{10-88}{42} = 4\frac{19}{2}$ . Ans.
- 38. Find the value of  $\frac{385}{357} \frac{13}{51}$ .  $\frac{235}{357} \frac{13}{51} = \frac{235 91}{357} = \frac{48}{119}$ . Ans.

39. Find the value of  $\frac{17}{68} - \frac{29}{108}$ .

$$\frac{17}{63} - \frac{29}{108} = \frac{204 - 203}{756} = \frac{1}{756}$$
. Ans.

40. Find the value of  $\frac{9}{38} - \frac{48}{209}$ .

$$\frac{9}{38} - \frac{43}{209} = \frac{99 - 86}{418} = \frac{13}{418}$$
. Ans.

41. Find the value of 148 - 289.

$$\frac{146}{273} - \frac{268}{637} = \frac{1032 - 804}{1911} = \frac{218}{1911}.$$
 Ans.

**42.** Find the value of  $\frac{350}{350} - \frac{190}{200}$ .

$$\frac{359}{360} - \frac{199}{200} = \frac{1795 - 1791}{1800} = \frac{1}{450}$$
. Ans.

## EXERCISE XXVII.

1. Simplify  $3\frac{2}{3} - 2\frac{5}{3} + 4\frac{3}{10} + 1\frac{7}{3} - 5\frac{3}{10}$ .

Sum of plus terms = 948

Sum of minus terms =  $8\frac{19}{120}$ Difference =  $1\frac{3}{7}$ . Ans.

2. Simplify 
$$\frac{1}{11} - \frac{1}{12} + 7\frac{3}{5} - 2\frac{1}{5} - 1\frac{11}{15}$$
.

Sum of plus terms =  $8\frac{78}{88}$ 

Sum of minus terms =  $4\frac{15}{16}$ 

Difference = 3157. Ans.

3. Simplify  $12 - 3\frac{2}{7} - 1\frac{8}{10} - 4\frac{5}{28} + 2\frac{18}{20} - 4\frac{8}{5}$ .

Sum of plus terms =  $14\frac{18}{20}$ 

Sum of minus terms =  $13\frac{51}{140}$ 

Difference = 13. Ans.

4. Simplify  $43\frac{7}{15} - 1\frac{1}{8} - 1\frac{1}{48} - 1\frac{1}{48} - 2\frac{1}{48} - 2\frac{7}{12} - 2\frac{48}{48} - 3\frac{1}{12}$ .

Sum of plus terms =  $43\frac{7}{15}$ 

Sum of minus terms =  $16\frac{5}{48}$ 

Difference =  $27\frac{29}{80}$ . Ans.

5. Simplify 
$$\frac{1}{2} + \frac{4}{18} + 7\frac{9}{20} + 8\frac{14}{19} + 7\frac{1}{2} + 8\frac{1}{10} + 4\frac{1}{12} - 36\frac{1}{20}$$
.  
Sum of plus terms =  $36\frac{1}{20}$   
Sum of minus terms =  $36\frac{1}{20}$   
Difference =  $0$ . Ans.

6. Simplify 
$$(8\frac{5}{18} + 1\frac{1}{29} + 17\frac{1}{16} + 40) - (30\frac{1}{16} + 11\frac{1}{16})$$
.  
Sum of plus terms =  $66\frac{1}{108}$   
Sum of minus terms =  $41\frac{7}{8}$   
Difference =  $25\frac{17}{216}$ . Ans.

7. Simplify 
$$(172\frac{1}{18} + 93\frac{1}{117}) + 172\frac{1}{18} - 93\frac{1}{117}$$
.  
 $(172\frac{1}{18} + 93\frac{1}{117}) + (172\frac{1}{18} - 93\frac{1}{117})$   
 $= 172\frac{1}{18} + 93\frac{1}{117} + 172\frac{1}{18} - 93\frac{1}{117}$   
 $= 172\frac{1}{18} + 172\frac{1}{18} = 344\frac{1}{12}\frac{1}{12} = 344\frac{1}{18}$ . Ans.

8. Simplify 
$$(172\frac{1}{18} + 93\frac{1}{14}) - (172\frac{1}{18} - 93\frac{1}{14})$$
.  
 $(172\frac{1}{18} + 93\frac{1}{14}) - (172\frac{1}{18} - 93\frac{1}{14})$   
 $= 172\frac{1}{18} + 93\frac{1}{14} - 172\frac{1}{18} + 93\frac{1}{14}$   
 $= 93\frac{1}{14} + 93\frac{1}{14} = 186\frac{1}{14}$ . Ans.

9. Simplify 
$$(\frac{3}{13} - \frac{2}{89}) + (\frac{5}{78} + \frac{7}{156})$$
.  

$$\left(\frac{3}{13} - \frac{2}{39}\right) + \left(\frac{5}{78} + \frac{7}{156}\right) = \frac{3}{13} - \frac{2}{39} + \frac{5}{78} + \frac{7}{156}$$

$$= \frac{36 - 8 + 10 + 7}{156} = \frac{15}{52}. \text{ Ans.}$$

10. Simplify 
$$\frac{1}{9} - \frac{8}{11} - 2\frac{3}{4} + 3\frac{3}{8} + 7\frac{7}{12} - 1\frac{3}{5} - \frac{3}{22}$$
.  
Sum of plus terms =  $11\frac{25}{38}$   
Sum of minus terms =  $4\frac{167}{220}$   
Difference =  $6\frac{465}{38}$ . Ans.

11. Simplify 
$$\frac{3}{10} - \frac{7}{1000} - \frac{9}{10000} - \frac{5}{10000}$$
.

 $\frac{3}{10} - \frac{7}{100} = \frac{9}{1000} - \frac{5}{10000} = \frac{3000 - 700 - 90 - 5}{10000} = \frac{441}{2000}$ . Ans.

12. Simplify 
$$9\frac{1}{5} - 7 - \frac{3}{4} - \frac{3}{5}$$
.  $9\frac{1}{5} - 7 - \frac{3}{4} - \frac{3}{5} - 2\frac{15 - \frac{1}{2}\frac{3}{4} - 20}{2\frac{1}{4}} = 1\frac{1}{2\frac{1}{4}}$ . Ans.

13. Simplify  $5\frac{3}{8} + 8\frac{3}{4} - 1\frac{3}{8} - 4\frac{7}{8}$ .

Sum of plus terms =  $14\frac{5}{12}$ .

Sum of minus terms =  $\frac{6\frac{17}{2}}{8\frac{7}{180}}$ . Ans.

14. Simplify  $6\frac{3}{4} - 5\frac{3}{8} + 4\frac{3}{8} - 4\frac{5}{12}$ .

Sum of plus terms =  $11\frac{3}{20}$ .

Sum of minus terms =  $10\frac{1}{12}$ .

Difference =  $1\frac{1}{15}$ . Ans.

15. Simplify  $14\frac{7}{18} + 9\frac{8}{5} - 6\frac{4}{4} - 12\frac{4}{5} - 3\frac{8}{5}$ . Sum of plus terms =  $23\frac{89}{90}$ . Sum of minus terms =  $23\frac{8}{20}$ . Difference =  $\frac{151}{180}$ . Ans.

16. Simplify  $20\frac{2}{3} - 2\frac{5}{3} - 9\frac{5}{5} + 10\frac{8}{10} - 14\frac{7}{12}$ . Sum of plus terms =  $30\frac{29}{50}$ Sum of minus terms =  $26\frac{5}{72}$ Difference =  $\frac{78}{360}$ . Ans.

17. Simplify  $95\frac{2}{8} - 9\frac{7}{20} - 8\frac{2}{7} - 14\frac{6}{15} + 74\frac{2}{5}$ . Sum of plus terms =  $169\frac{2}{5}$ Sum of minus terms =  $32\frac{5}{25}$ Difference =  $137\frac{179}{25\frac{2}{3}}$ . Ans.

18. Simplify  $12\frac{3}{4} + 23\frac{3}{8} - (4\frac{3}{10} + 12\frac{3}{6} + 7\frac{14}{18})$ . Sum of plus terms =  $36\frac{1}{8}$ Sum of minus terms =  $24\frac{19}{80}$ Difference =  $11\frac{59}{120}$ . Ans.

19. Simplify  $16\frac{2}{15} + 18\frac{5}{24} - (5\frac{2}{5} + 9\frac{9}{40} + 14\frac{5}{24})$ .

Terms outside parenthesis =  $34\frac{41}{120}$ Terms inside parenthesis =  $28\frac{129}{120}$ Difference =  $5\frac{61}{120}$ . Ans.

20. Simplify 
$$97\frac{8}{9} - (20 + 9\frac{8}{4} + 18\frac{2}{25} + 24\frac{49}{80})$$
.

Terms outside parenthesis =  $97\frac{8}{9}$ .

Terms inside parenthesis =  $72\frac{81}{100}$ .

Difference =  $25\frac{71}{900}$ . Ans.

21. Simplify 
$$2\frac{12}{16} + 3\frac{15}{85} - (1\frac{58}{10} + 1\frac{31}{82} + \frac{49}{85})$$
.

Terms outside parenthesis =  $6\frac{5}{28}$ 

Terms inside parenthesis =  $4\frac{678}{1120}$ 

Difference =  $1\frac{647}{1120}$ . Ans.

22. Simplify 
$$\frac{148}{100} + \frac{2471}{1000} - \frac{82643}{100000}$$
.
$$\frac{143}{100} + \frac{2471}{1000} - \frac{82643}{100000} = \frac{143000 + 247100 - 82643}{100000}$$

$$= \frac{307457}{100000} = 3\frac{7457}{100000}$$
. Ans.

## EXERCISE XXVIII.

- 1. Simplify  $\frac{2\frac{8}{11}}{3\frac{3}{4}}$ .

  Multiply by 44.  $\frac{100}{165} = \frac{20}{33}$ . Ans.
- 2. Simplify  $\frac{3}{7\frac{1}{8}}$ .

  Multiply by 8.  $\frac{24}{57} = \frac{8}{19}$ . Ans.
- 3. Simplify  $\frac{17\frac{1}{7}}{13\frac{1}{3}}$ .

  Multiply by 21.  $\frac{360}{280} = 1\frac{2}{7}$ . Ans.

- 4. Simplify  $\frac{\frac{5}{8}}{\frac{1}{8}}$ .

  Multiply by 27.  $\frac{15}{225} = \frac{1}{15}$ . Ans.
- 5. Simplify  $\frac{5\frac{1}{8}}{8\frac{4}{11}}$ .

  Multiply by 99.  $\frac{253}{414} = \frac{11}{18}$ . Ans.
- 6. Simplify  $\frac{1\frac{4}{8} \text{ of } 3\frac{1}{7}}{4\frac{1}{8} \text{ of } \frac{9}{10}}$ .  $\frac{g}{g} \times \frac{\frac{22}{7}}{7} \times \frac{8}{33} \times \frac{\frac{16}{9}}{9} = \frac{32}{21} = 1\frac{11}{11}.$ Ana.

- 7. Simplify  $\frac{2\frac{1}{2}-1\frac{5}{6}}{1\frac{5}{6}-1\frac{5}{8}}$ .

  Multiply by 72.  $\frac{180-112}{132-117}=\frac{68}{15}=\frac{4^{3}}{15}$ . Ans.
- 8. Simplify  $\frac{10\frac{2}{5} 1\frac{5}{7}}{7\frac{1}{5} 3\frac{3}{40}}$ .

  Multiply by 280.  $\frac{2912 480}{1995 861} = \frac{2432}{1134} = 2\frac{32}{564}$ . Ans.
- 9. Simplify  $\frac{3}{1}$  of  $2\frac{1}{17}$ .  $\frac{3}{7} \times \frac{35}{17} \times \frac{17}{7} \times \frac{3}{5} = 1$ ?. Ans.
- 10. Simplify  $\frac{6\frac{2}{4} 1\frac{1}{14}}{2\frac{1}{6} + 1\frac{3}{7}}$ .

  Multiply by 84.  $\frac{567 114}{182 + 120} = \frac{453}{302} = 1\frac{1}{2}$ . Ans.
- 11. Simplify  $\frac{5\frac{4}{3} + 2\frac{3}{7}}{4\frac{2}{3} 3\frac{11}{3}}$ .  $\frac{8\frac{3}{35}}{\frac{3}{35}} = \frac{28\cancel{5}}{35} \times \frac{39}{\cancel{32}} = \frac{351}{35} = 10\frac{1}{35}.$ Ans.
- 12. Simplify  $\frac{8\frac{7}{4}}{14} \frac{7}{1\frac{1}{7}}$ .  $\frac{5}{4} \times \frac{1}{14} \frac{2}{3} \times \frac{7}{8} = \frac{5}{8} \frac{7}{12} = \frac{1}{24}$ .

  2 4 Ans.

- 13. Simplify  $\frac{3\frac{3}{7}}{11\frac{1}{4}}$  of  $\frac{3\frac{1}{7}}{2\frac{3}{7}}$ .  $\frac{24}{7} \times \frac{4}{45} \times \frac{3}{27} \times \frac{5}{12} \frac{3}{7}$ . Ans.
- 14. Simplify  $\frac{5\frac{8}{5} 4\frac{11}{12}}{\frac{5\frac{8}{5} 2\frac{1}{12}}{2\frac{1}{5}}}$ .  $\frac{\frac{35}{36}}{2\frac{3}{12}} = \frac{70}{175} = \frac{2}{5}$ . Ans.
- 15. Simplify  $\frac{2\frac{5}{4}+2\frac{7}{4}}{\frac{4\frac{7}{4}-3\frac{7}{4}}{1\frac{1}{2}\frac{7}{4}} = \frac{45}{8} \times \frac{\frac{28}{45}-3\frac{1}{4}}{2}$ . Ans.
- 16. Simplify  $\frac{2\frac{7}{5} \times \frac{1}{11}}{3\frac{5}{7} + 4\frac{1}{3}}$ .  $\frac{13}{5} \times \frac{9}{11} \times \frac{3}{8} \times \frac{7}{26} = \frac{189}{80} = 2\frac{1}{80}$ .

  Ans.
- 17. Simplify  $\frac{\frac{17}{26} + \frac{11}{18} + \frac{7}{16} + \frac{4}{5}}{\frac{17}{26} \frac{11}{18} + \frac{7}{16} \frac{4}{5}}$ Multiply by 60.  $\frac{51 + 44 + 42 + 48}{51 44 + 42 48} = 185. \text{ Ans.}$
- 18. Simplify  $\frac{4\frac{7}{4}-2\frac{1}{4}}{6\frac{1}{4}-2\frac{1}{4}}$ .

  Multiply by 28.  $\frac{116-63}{182-60}=\frac{53}{122}$ . Ans.

19. Simplify 
$$\frac{2\frac{2}{16}-4\frac{4}{7}+3\frac{1}{8}}{5\frac{4}{7}-4\frac{7}{8}+\frac{3}{8}}$$
.

Multiply by 280.
$$\frac{749-1280+875}{1640-1365+112}=\frac{344}{387}=\frac{8}{9}. \text{ Ans.}$$

20. Simplify 
$$\frac{1\frac{1}{4} \times 1\frac{3}{7} + \frac{1}{8} \text{ of } 2\frac{1}{4} - \frac{1}{2}\frac{3}{8} \times 2}{\frac{1}{2}\frac{3}{8} \text{ of } 2 + \frac{1}{8} \text{ of } 2\frac{1}{4} - 1\frac{1}{4} \text{ of } 1\frac{3}{7}}$$

$$\frac{4\frac{5}{8} + \frac{3}{4} - \frac{1}{4}\frac{3}{8}}{1\frac{3}{8} + \frac{3}{4} - \frac{4}{4}\frac{3}{8}} - \frac{45}{26} + 21 - 26}{26 + 21 - 45} - \frac{40}{2} = 20. \text{ Ans.}$$

21. Simplify 
$$2\frac{1}{4} \times \frac{10\frac{1}{8} - 4\frac{11}{12}}{6\frac{1}{16} + 7\frac{3}{8}} \times \frac{3\frac{5}{11}}{1\frac{2}{8} \times 9\frac{1}{11}}$$
.  
 $\frac{9}{4} \times \frac{516 - 236}{297 + 368} \times \frac{38}{140} = \frac{9}{4} \times \frac{\cancel{56}}{\cancel{133}} \times \frac{\cancel{19}}{\cancel{19}} = \frac{9}{35}$ . Ans.

22. Simplify 
$$\frac{8\frac{7}{8} - 7\frac{6}{7} + 5\frac{5}{6} - 4\frac{4}{5}}{9\frac{9}{10} - 8\frac{1}{15} + 7\frac{7}{6} - 6\frac{5}{7}}$$
$$\frac{7455 - 6600 + 4900 - 4032}{8316 - 7448 + 6615 - 5760} = \frac{1723}{1723} = 1. \text{ Ans.}$$

## EXERCISE XXIX.

- 1. What fraction of 8 is 3?  $\frac{3}{8}$ . Ans.
- 2. What fraction of 3 is 8?  $\frac{8}{3} = 2\frac{3}{4}$ . Ans.
- 3. What fraction of 9 is 7?  $\frac{7}{9}$ . Ans.
- 4. What fraction of 7 is 9?  $\frac{9}{7} = 13. \text{ Ans.}$

- 5. What fraction of 8 is 12?  $\frac{12}{8} = 1\frac{1}{2}$ . Ans.
- 6. What fraction of 12 is 8?  $\frac{8}{12} = \frac{2}{3}$ . Ans.
- 7. What fraction of  $2\frac{1}{5}$  is  $\frac{3}{5}$ .  $\frac{3}{2\frac{1}{5}} = \frac{3}{11}$ . Ans.
- 8. What fraction of  $\frac{3}{5}$  is  $2\frac{1}{5}$ ?  $\frac{2\frac{1}{5}}{\frac{3}{5}} = 3\frac{3}{5}. \text{ Ans.}$

- 9. What fraction of  $2\frac{3}{4}$  is  $1\frac{1}{4}$ ?  $\frac{1\frac{1}{4}}{2\frac{3}{4}} = \frac{5}{11}. \text{ Ans.}$
- 10. What fraction of  $1\frac{1}{4}$  is  $2\frac{3}{4}$ ?  $\frac{2\frac{3}{4}}{1\frac{1}{4}} = 2\frac{1}{8}. \text{ Ans.}$
- 11. What fraction of  $2\frac{1}{8}$  is  $7\frac{1}{8}$ ?  $\frac{7\frac{1}{8}}{2\frac{1}{8}} = 3\frac{8}{56}. \text{ Ans.}$
- 12. What fraction of  $7\frac{1}{3}$  is  $2\frac{1}{3}$ ?  $\frac{2\frac{1}{3}}{7\frac{1}{3}} = \frac{51}{176}. \text{ Ans.}$
- 13. What fraction of  $3\frac{1}{3}$  is  $8\frac{1}{3}$ ?  $\frac{8\frac{1}{7}}{3\frac{1}{4}} = 2\frac{8}{70}. \text{ Ans.}$
- 14. What fraction of \$2 is \$1\frac{1}{2}?  $\frac{$1\frac{1}{4}}{$2} = \frac{3}{4}$ . Ans.
- 15. What fraction of \$2\frac{1}{2}\$ is \$5?  $\frac{$5}{$2\frac{1}{2}} = 2. \text{ Ans.}$
- 16. What fraction of \$\frac{3}{4}\$ is \$\frac{1}{4}\$?  $\frac{\$\frac{1}{4}}{\$\frac{3}{4}} = \frac{1}{3}. Ans.$
- 17. What fraction of \$\frac{3}{2}\$ is \$\frac{3}{2}\$?  $\frac{\$\frac{3}{4}}{\$\frac{3}{2}} = \frac{3}{10}. Ans.$

- 18. What fraction of \$2\frac{1}{2}\$ is \$\frac{1}{2}\$?  $\frac{\$\frac{1}{3}}{\$2\frac{3}{2}} = \frac{4}{33}. \text{ Ans.}$
- 19. What fraction of \$\frac{1}{2}\$ is \$\frac{1}{10}\$?  $\frac{\$ \frac{1}{10}}{\$ \frac{1}{4}} = \frac{1}{5}. \text{ Ans.}$
- 20. What fraction of \$1 is \$\frac{7}{8}? \\ \frac{57}{81} = \frac{7}{8}. \ Ans.
- 21. What fraction of \$10 is \$\frac{3}{4}?  $\frac{\$\frac{2}{4}}{\$10} = \frac{1}{15}. \text{ Ans.}$
- 22. What fraction of \$100 is \$6?  $\frac{$6}{$100} = \frac{3}{50}. \text{ Ans.}$
- 23. What fraction of \$100 is \$4\frac{1}{2}?  $\frac{$4\frac{1}{2}}{$100} = \frac{9}{200}. \text{ Ans.}$
- 24. What fraction of \$4 is \$25?  $\frac{$25}{$4} = 6\frac{1}{4}$ . Ans.
- 25. What fraction of 100 $\frac{8}{1}$  is  $\frac{8}{1}$ ?  $\frac{8}{100} = \frac{76}{905}$ . Ans.
- 26. What fraction of

  21 is  $\frac{15}{15}$  of  $3\frac{1}{7}$ ?  $\frac{15}{21} \times \frac{34}{7} = \frac{1}{7}$ . Ans.

27. What fraction of 
$$18\frac{1}{2}\frac{7}{6}$$
 is  $\frac{4}{6}$  of  $33\frac{3}{6}$ ?  $\frac{4}{18}\frac{33\frac{3}{6}}{18\frac{17}{23\frac{5}{6}}} = 1\frac{1}{6}$ . Ans.

28. What fraction of

$$3\frac{1}{4}$$
 is  $\frac{1}{4} \times 1\frac{1}{4}$ ?

 $\frac{1}{34} = \frac{4}{15}$ . Ans.

29. What fraction of 
$$3\frac{1}{14} \times 5\frac{1}{17}$$
 is 1720?  $\frac{1720}{3\frac{1}{14} \times 5\frac{1}{17}} = 110\frac{275}{3\frac{1}{14}}$ . Ans.

30. What fraction of 
$$3\frac{1}{4} \times \frac{4}{5}$$
 of  $\frac{4}{5}$  is  $1\frac{3}{5}$ ?
$$\frac{1\frac{3}{5}}{3\frac{1}{5} \times \frac{4}{5} \times \frac{4}{5}} = \frac{9}{10}.$$
 Ass.

31. What part of 
$$\frac{35 \times 35}{35 \times 3} = 1$$
 Ans. 
$$\frac{1 \times 4 \times 3}{35 \times 33} = 1$$

32. What part of 
$$13\frac{1}{5} \times \frac{3}{5} \times \frac{3}{5}$$
 is  $\frac{3}{5}$  of  $1\frac{4}{5}$  of  $1\frac{1}{5}$ ?
$$\frac{3 \times 1\frac{4}{5} \times 1\frac{1}{5}}{13\frac{5}{5} \times \frac{3}{5} \times \frac{3}{5}} = 1. \text{ Are}$$

33. What part of 
$$\frac{17}{17} + \frac{1}{18} + \frac{7}{10} + \frac{4}{5}$$
 is  $\frac{17}{27} - \frac{1}{25} + \frac{7}{10} - \frac{4}{5}$ ?

$$\frac{17}{27} + \frac{1}{15} + \frac{7}{10} + \frac{4}{5}$$
Multiply by 60.

$$\frac{51 - 44 + 42 - 48}{51 + 44 + 42 + 48} = \frac{1}{185}$$
. Ans.

34. What part of 
$$4\frac{1}{7} - 2\frac{1}{7}$$
 is  $6\frac{1}{7} - 2\frac{1}{7}$ ?
$$\frac{6\frac{1}{7} - 2\frac{1}{7}}{4\frac{1}{7} - 2\frac{1}{7}} = \frac{182 - 60}{116 - 63} = \frac{122}{53} = 2\frac{16}{53}$$
. Ans.

35. What part of 
$$17\frac{2}{3} - 12\frac{4}{3}$$
 is  $5 - \frac{1}{18} - \frac{1}{40} - \frac{1}{18}$ ?
$$\frac{5 - \frac{1}{18} - \frac{4}{39} - \frac{1}{28}}{17\frac{2}{3} - 12\frac{4}{5}}$$
Multiply by  $6825$ .
$$\frac{34125 - 525 - 700 - 273}{120575 - 87750} = \frac{32627}{32825}$$
. Ans.

36. What part of 
$$24 - 17\frac{4}{18}$$
 is  $7 + \frac{2}{15} - \frac{5}{51} - \frac{11}{15}$ ?
$$\frac{7 + \frac{2}{15} - \frac{5}{51} - \frac{11}{45}}{24 - 17\frac{4}{18}}$$
Multiply by 5265.
$$\frac{36855 + 702 - 325 - 1287}{126360 - 91125} = \frac{35945}{35235} = \frac{1142}{2027}$$
. Ans.

37. What part of 
$$\frac{1}{7}$$
 of  $2\frac{1}{17}$  is  $1\frac{3}{7} + 2\frac{3}{7}$ ?

$$\frac{\frac{13}{3} + \frac{27}{7}}{\frac{3}{7} \times \frac{17}{17}} = \frac{7}{17} \times \frac{5}{3} \times \frac{7}{3} \times \frac{17}{35} = \frac{7}{9}. Ans.$$

38. What part of

$$\frac{\left(\frac{7}{4-\frac{5}{6}}-\frac{5}{6-\frac{3}{8}}\right)+\left(\frac{4}{7-\frac{1}{4}}+\frac{2}{4-\frac{3}{8}}\right)is}{\left(14-\frac{1}{\frac{1}{4}-\frac{5}{3}}\right)+\left(\frac{1}{\frac{1}{4}-\frac{3}{4}}-13\right)?}$$

$$\frac{\left(14-\frac{1}{\frac{1}{3}-\frac{1}{4}}\right)+\left(\frac{1}{\frac{1}{4}-\frac{2}{3}}-13\right)}{\left(\frac{7}{4-\frac{1}{8}}-\frac{5}{6-\frac{3}{8}}\right)+\left(\frac{4}{7-\frac{4}{9}}+\frac{2}{4-\frac{3}{8}}\right)}$$

$$=\frac{\left(14-\frac{4}{13}\right)+\left(\frac{11}{3}-13\right)}{\left(\frac{4}{13}-\frac{3}{8}\right)+\left(\frac{11}{3}-13\right)}=\frac{\frac{204}{19}\times\frac{5}{33}}{\frac{24}{17}\times\frac{4}{33}}=\frac{108}{118}. Ans.$$

# EXERCISE XXX.

1. Reduce to common fractions in their lowest terms 0.125.

$$0.125 = \frac{125}{1000} = \frac{1}{3}$$
. Ans.

2. Reduce to common fractions in their lowest terms 0.625.

$$0.625 = \frac{328}{1000} = \frac{3}{1}$$
. Ans.

3. Reduce to common fractions in their lowest terms 0.675.

$$0.675 = \frac{675}{1000} = \frac{27}{40}$$
. Ans.

4. Reduce to common fractions in their lowest terms 10.864.

$$10.881 - 10.881 - 10.881 - 10.881$$
. Ans.

5. Reduce to common fractions in their lowest terms 50.84.

$$50.84 - 50_{100}^{84} - 50_{10}^{81}$$
. Ans.

6. Reduce to common fractions in their lowest terms 3.00025.

$$3.00025 \Rightarrow 3_{\overline{1000000}} = 3_{\overline{4000}}^{1}$$
. Ans.

7. Reduce to common fractions in their lowest terms 8.1075.

$$8.1075 = 8_{10000}^{1075} = 8_{400}^{48}$$
. Ans.

8. Reduce to common fractions in their lowest terms 35.01024.

$$35.01024 = 35_{\overline{1000000}} = 35_{\overline{8125}}.$$
Ans.

9. Reduce to common fractions in their lowest terms 7.015625. 7.015625 =  $7\frac{156825}{100}$  =  $7\frac{1}{100}$ . Ans.

10. Reduce to common fractions in their lowest terms 20.100256.

$$20.100256 = 20_{1000000}^{100256} = 20_{$1250}^{$128}.$$
Ans.

- Reduce to common fractions in their lowest terms 10.012575.
   10.012575 = 10,12575 = 10,12575 = 10,485 a. Ans.
- 13. Reduce to common fractions in their lowest terms 104.235. 104.235 = 104.235 = 104.235 = 104.235. Ans.
- 13. Reduce to common fractions in their lowest terms 50.0004.  $50.0004 = 50_{10004} = 50_{2506}. \text{ Ans.}$
- 14. Reduce to common fractions in their lowest terms 100.001.  $100.001 = 100_{1000}^{-1}$ . Ans.
- 15. Reduce to common fractions in their lowest terms 8.00725.  $8.00725 = 8_{\frac{745}{100000}} = 8_{\frac{40}{1000}}^{\frac{4}{10}}$ . Ans.
- Reduce to common fractions in their lowest terms 20.018375.
   20.018375 = 20-18875 = 20-1870. Ans.
- Reduce to common fractions in their lowest terms 125,6048.
   125,6048 = 125,5043 = 125,114. Ans.
- 18. Reduce to common fractions in their lowest terms 0.128.  $0.128 = \frac{123}{1000} = \frac{14}{123}. Ans.$
- 19. Reduce to common fractions in their lowest terms 0.73125.  $0.73125 = \frac{731135}{1080160} = \frac{117}{108}$ . Ans.
- 20. Reduce to common fractions in their lowest terms 1.1875.  $1.1875 = 1\frac{1875}{10000} = 1\frac{1}{10}$ . Ans.

  - ace to common fractions in their lowest terms 6.03125.  $6.03125 = 6\frac{8125}{166600} = 6\frac{1}{12}$ . Ans.
  - acc to common fractions in their lowest terms 60.3125.  $60.3125 60^{+1.25}_{10.00} 60^{-3}_{10}$ . Ans.
  - ace to common fractions in their lowest terms 7.0315.  $7.0315 = 7_{1511} = 7_{151}$ . Ans.

# EXERCISE XXXI.

1. Reduce to decimals 7/8.

0.875 8)7.000

- 2. Reduce to decimals  $\frac{18}{18}$ .

  0.9375

  16)15.0000
- 3. Reduce to decimals  $\frac{9}{32}$ . 0.28125 32)9.00000
- 4. Reduce to decimals  $\frac{9}{25}$ .  $\frac{0.36}{25)9.00}$
- 5. Reduce to decimals  $\frac{5}{64}$ . 0.078125 64)5.000000
- 6. Reduce to decimals  $4\frac{11}{800}$ . 0.01375 8)0.110004.01375. Ans.
- 7. Reduce to decimals  $5_{32000}$ .

  0.00015625

  32)0.00500000

  5.00015625. Ans.

- 9. Reduce to decimals 11<sub>4660</sub>.

  0.00475

  4)0.01900

  11.00475. Ans.
- 10. Reduce to decimals  $\frac{9}{125}$ .  $\frac{0.072}{125)9.000}$
- 11. Reduce to decimals  $\frac{0.00425}{4)0.01700}$
- 12. Reduce to decimals  $\frac{128}{128}$ .

  0.9296875

  128)119.0000000
- 13. Reduce to decimals  $\frac{18}{625}$ . 0.0208 625)13.0000
- 14. Reduce to decimals 116.

  0.04296875

  256)11.00000000
- 15. Reduce to decimals  $\frac{3}{160}$ .

  0.01875

  16)0.30000
- 16. Reduce to decimals \( \frac{124}{18} \).
  7.75
  16)124.00

17. Reduce to decimals 4 of 14.

$$\frac{2}{3} \times \frac{3}{5} = \frac{6}{5}.$$

$$\frac{1.2}{5)6.0}$$

18. Reduce to designals 1 of 1 of 70.

$$\frac{3}{4} \times \frac{5}{8} \times \frac{7}{19} - \frac{21}{64}$$

0.328125 64)21.000000

19. Reduce to decimals 34 of 44.

$$\frac{2}{5} \times \frac{37}{9} = \frac{74}{5}.$$

$$\frac{14.8}{5)74.0}$$

20. Reduce to decimals 32 of 32.

$$\frac{29}{32} \times \frac{49}{64} - \frac{1421}{2048}$$
.

0.69384765625

2048)1421,0000000000

### EXERCISE XXXII.

1. In like manner simplify  $7\frac{2}{5} + 4\frac{5}{5} + 9\frac{15}{15} + 11\frac{25}{15}$ .

$$7\frac{2}{5} + 4\frac{6}{5} + 9\frac{1}{5} + 11\frac{2}{5} = 7.4 + 4.625 + 9.65 + 11.90625 = 33.58125.$$
 (1)

$$7\frac{2}{5} + 4\frac{5}{5} + 9\frac{13}{25} + 11\frac{22}{5} = 31\frac{13}{160} = 33\frac{9}{160} = 33.58125.$$
 (2)

2. In like manner simplify  $84\frac{1}{6} + 19\frac{1}{1} \div \frac{4}{5}$ .

$$84\frac{18}{18} + 19\frac{1}{18} + \frac{1}{18} = 84.65 + 19.523809\frac{1}{18} + 0.82 = 104.993809\frac{1}{18}.$$
 (1)

$$84\frac{18}{16} + 19\frac{1}{11} + \frac{41}{56} = 103\frac{1865 + 1100 + 1722}{2100} = 103\frac{4187}{2187} = 104\frac{2987}{2187} = 104.993809\frac{1}{11}.$$
 (2)

3. In like manner simplify 437 + 1347 + 4287 + 248 + 14.

$$4\frac{27}{64} + 13\frac{17}{26} + 42\frac{17}{66} + 2\frac{17}{66} + 1\frac{1}{2} = 4.421875 + 13.85 + 42.74 + 2.8125 + 1.5$$

$$= 65.324375.$$
(1)

$$4\frac{27}{64} + 13\frac{17}{26} + 42\frac{27}{66} + 2\frac{18}{16} + 1\frac{1}{2} = 62\frac{675 + 1860 + 1184 + 1800 + 800}{1600} = 62\frac{818}{1600} = 65.324375.$$
 (2)

4. In like manner simplify  $5\frac{7}{4} + 13\frac{4}{5} + 19\frac{7}{16} + 7\frac{2}{20}$ .

$$5\frac{7}{8} + 13\frac{4}{8} + 19\frac{7}{16} + 7\frac{2}{20} = 5.875 + 13.8 + 19.4375 + 7.15 = 46.2625.$$
 (1)

$$5_{3}^{7} + 13_{3}^{4} + 19_{16}^{7} + 7_{20}^{3} = 44_{20}^{70+64+85+12} = 44_{30}^{161} = 46_{20}^{21} = 46.2625.$$
 (2)

5. In like manner simplify  $5_{10}^{5} + \frac{2}{3}$  of  $1\frac{4}{5} + \frac{7}{5}$  of  $2\frac{7}{5} + \frac{2}{5}$  of  $3\frac{1}{5} + \frac{7}{5} \times 1\frac{1}{5} + \frac{7}{5} \times 2\frac{7}{7} + \frac{2}{5} \times \frac{7}{5}$ 

$$=5.5+0.666\frac{2}{3}\times1.8+0.875\times2.285714\frac{2}{3}+0.75\times0.625$$

$$= 5.5 + 1.2 + 2 + 0.46875 = 9.16875.$$
 (1)

$$5_{\frac{1}{10}} + \frac{2}{3} \times 1_{\frac{4}{5}} + \frac{7}{4} \times 2_{\frac{7}{7}} + \frac{3}{4} \times \frac{5}{5} = 5_{\frac{1}{2}} + 1_{\frac{1}{5}} + 2 + \frac{15}{52} = 8_{\frac{8}{1}\frac{0}{5}+\frac{7}{5}} = 8_{\frac{1}{1}\frac{0}{5}} = 8_{\frac{1}{1}\frac{0}{5}} = 9_{\frac{1}{1}\frac{0}{5}} = 9_{\frac{1}1\frac{0}{5}} = 9_{\frac$$

6. In like manner simplify 1,5 of 25.

$$1_{\frac{5}{12}} \times 2_{\frac{5}{3}} = 1.4166_{\frac{3}{4}} \times 2.625 = 3.71875. \tag{1}$$

$$1_{\frac{5}{12}} \times 2_{\frac{5}{8}} = \frac{17}{\cancel{12}} \times \frac{\cancel{21}}{\cancel{8}} = \frac{119}{32} = 3_{\frac{28}{32}} = 3.71875. \tag{2}$$

7. In like manner simplify  $3\frac{5}{16} + 2\frac{19}{26}$ .

$$3\frac{5}{16} + 2\frac{19}{20} = 3.3125 + 2.95 = 6.2625.$$
 (1)

$$3_{\frac{5}{13}} + 2_{\frac{19}{20}} = 5_{\frac{25+76}{80}} = 5_{\frac{101}{80}} = 6_{\frac{21}{80}} = 6.2625.$$
 (2)

8. In like manner simplify  $7\frac{2}{5} - 4\frac{5}{5}$ .

$$7\frac{2}{5} - 4\frac{5}{8} = 7.4 - 4.625 = 2.775. \tag{1}$$

$$7\frac{2}{5} - 4\frac{6}{5} = 3\frac{16 - 25}{40} = 2\frac{31}{40} = 2.775.$$
 (2)

9. In like manner simplify  $82\frac{1}{3} - 37\frac{1}{16}$ .

$$821 - 3711 = 82.2 - 37.6875 = 44.5125. \tag{1}$$

$$82\frac{1}{6} - 37\frac{1}{16} = 45\frac{1.6 - 5.5}{8.0} = 44\frac{1}{80} = 44.5125.$$
 (2)

10. In like manner simplify  $100 - 17\frac{11}{625}$ .

$$100 - 17\frac{118}{625} = 100 - 17.1808 = 82.8192.$$
 (1)

$$100 - 17\frac{118}{625} = 82\frac{512}{625} = 82.8192.$$
 (2)

11. In like manner simplify  $5\frac{1}{2} - 1\frac{1}{2}$  of  $1\frac{1}{2}\frac{3}{4}$ .

$$5\frac{1}{2} - 1\frac{1}{2} \times 1\frac{1}{2} = 5.5 - 1.5 \times 1.5416\frac{2}{3} = 5.5 - 2.3125 = 3.1875.$$
 (1)

$$5\frac{1}{4} - 1\frac{1}{4} \times 1\frac{1}{4} = 5\frac{1}{4} - 2\frac{5}{16} = 3\frac{3}{16} = 3.1875.$$
 (2)

12. In like manner simplify  $\frac{14}{2} - \frac{11}{64}$ .

$$\frac{14}{25} - \frac{11}{64} = 0.56 - 0.171875 = 0.388125. \tag{1}$$

$$\frac{14}{25} - \frac{11}{64} = \frac{896 - 275}{1600} = \frac{621}{1600} = 0.388125. \tag{2}$$

13. In like manner simplify  $8\frac{1}{6} - 1\frac{1}{2} \times \frac{8}{16}$ .

$$8\frac{1}{5} - 1\frac{1}{2} \times \frac{3}{16} = 8.2 - 1.5 \times 0.1875 = 8.2 - 0.28125 = 7.91875.$$
 (1)

$$8\frac{1}{5} - 1\frac{1}{2} \times \frac{3}{16} = 8\frac{1}{5} - \frac{9}{32} = 8\frac{32 - 45}{160} = 7\frac{147}{160} = 7.91875.$$
 (2)

14. In like manner simplify  $\frac{12}{12} \times 1000$ .

$$\frac{19}{64} \times 1000 - 0.296875 \times 1000 - 296.875. \tag{1}$$

$$\frac{19}{64} \times \frac{1000}{1} = \frac{2875}{8} = 2967 = 296.875. \tag{2}$$

## EXERCISE XXXIII.

1. Reduce to decimals §.

$$0.\dot{5}$$
 9)5.0

2. Reduce to decimals  $\frac{5}{11}$ .

$$0.\overline{45}$$
11)5.00

3. Reduce to decimals 3<sub>12</sub>.

$$3_{12}^{5} = 3.416$$
. Ans.

4. Reduce to decimals 11.

$$0.183$$
6)1.100

5. Reduce to decimals 317.

$$3\frac{1}{4}$$
 = 3.35416. Ans.

6. Reduce to decimals 25.

$$0.\dot{1}3\dot{5} \\ 37)5.000$$

$$2\frac{5}{37} = 2.\dot{1}3\dot{5}$$
. Ans.

7. Reduce to decimals 3700.

$$\frac{0.00081}{37)0.03000}$$

8. Reduce to decimals 1111.

$$11\frac{1}{3}\frac{1}{4} = 11.13\dot{0}9523\dot{8}$$
. Ans.

9. Reduce to decimals  $9_{108}^{11}$ .

$$0.10\overline{185}$$

$$108\overline{)11.00000}$$

$$9_{108} = 9.10\dot{1}8\dot{5}$$
. Ans.

- 10. Reduce to decimals  $11\frac{4}{85}$ .

  0.1142857

  35)4.0000000  $11\frac{4}{35} = 11.1142857$ . Ans.
- 11. Reduce to decimals  $\frac{15}{15}$ .

  0.267857142

  56)15.000000000
- 12. Reduce to decimals  $\frac{8}{21}$ .

  0.380952

  21)8.000000
- 13. Reduce to decimals  $\frac{13}{3}$ . 0.39 33)13.00

- 14. Reduce to decimals \$7.

  9.5285714

  7)3.7000000
- 16. Reduce to decimals  $5\frac{6}{26}$ . 0.230769 13)3.000000  $5\frac{6}{26} = 5\frac{3}{13} = 5.230769$ . Ans.
- 17. If  $\frac{117}{5^7 \times 2^8}$  be expressed as a decimal, the quotient will contain how many decimal places?

As 7 is the highest power of 2 or 5 in the denominator, and as there are no other factors than 2 or 5, there will be seven decimal places in the quotient.

18. If  $\frac{119}{2^5 \times 13}$  be expressed as a decimal, how many decimal places will *precede* the recurring period?

As 5 is the highest power of 2 or 5 in the denominator, and as there is another factor than 2 or 5, five decimal places will precede the repetend.

19. If  $\frac{-57}{5^2 \times 7}$  be reduced to a decimal, how many decimal places will precede the recurring period?

As 2 is the highest power of 2 or 5 in the denominator, and as there is another factor than 2 or 5, two decimal places will precede the repetend.

### EXERCISE XXXIV.

1. Reduce to common fractions in their lowest terms 0.245.

2. Reduce to common fractions in their lowest terms 0.425.

3. Reduce to common fractions in their lowest terms 53.00243.

$$53.00\dot{2}4\dot{3} = 53_{\frac{1}{9}\frac{1}{9}\frac{1}{9}00} = 53_{\frac{1}{8}\frac{1}{9}00}.$$
Ans.

4 Reduce to common fractions in their lowest terms 7.2011.

$$7.2011 - 73998$$
. Ans.

5. Reduce to common fractions in their lowest terms 2.5306.

$$2.53\dot{0}\dot{6} = 2\frac{1}{2}\frac{1}{2}\frac{1}{2}\frac{1}{2} = 2\frac{1}{2}\frac{7}{2}\frac{1}{2}$$
. Ans.

6. Reduce to common fractions in their lowest terms 0.00426.

$$0.004\dot{2}\dot{6} = \frac{482}{99000} = \frac{211}{49500}$$
. Ana

7. Reduce to common fractions in their lowest terms 31.203.

$$31.203 - 31\frac{291}{230} - 31\frac{67}{230}$$
. Ans.

8. Reduce to common fractions in their lowest terms 0.351.

$$0.351 - \frac{1}{2} - \frac{1}{2}$$
. Ans.

9. Reduce to common fractions in their lowest terms 1.416.

$$1.416 - 1888 - 15$$
. Ans.

10. Reduce to common fractions in their lowest terms 0.5575.

$$0.5\overline{5}7\overline{5} = \frac{8878}{8878} = \frac{887}{887}$$
. Ans.

11. Reduce to common fractions in their lowest terms 2.081.

$$2.081 - 2\frac{81}{990} - 2\frac{9}{110}$$
. Ans.

12. Reduce to common fractions in their lowest terms 5.12297. 5.12297 - 513335 - 5.22. Ans.

13. Reduce to common fractions in their lowest terms 
$$0.3590^{\circ}$$

$$0.3590 = \frac{2555}{2555} = \frac{120}{100}$$
Ans.

14. Reduce to common fractions in their lowest terms 4.3162.  $4.3\dot{1}6\dot{2} = 48188 = 4117$ . Ans.

- 15. Reduce to common fractions in their lowest terms 0.7283.  $0.7283 = \frac{2688}{100} = \frac{2688}{100}$ . Ans.
- 16. Reduce to common fractions in their lowest terms 5.142857.  $5.142857 = 5\frac{14285}{199998} = 5\frac{71428}{199998}$ . Ans.
- 17. Reduce to common fractions in their lowest terms 0.2368. 0.2368 = 3488 = 1188. Ans.
- 13. Reduce to common fractions in their lowest terms 1.136.  $1.136 = 1\frac{27}{290} = 1\frac{27}{29} = 1\frac{3}{29}$ . Ans.
- 19. Reduce to common fractions in their lowest terms 1.531.  $1.531 \Rightarrow 1\frac{53}{111} \Rightarrow 1\frac{59}{111}$ . Ans.
- 20. Reduce to common fractions in their lowest terms 3.28963.  $8.28963 - 328963 = 3 \frac{6.43}{2220}$ . Ans.
- 21. Reduce to common fractions in their lowest terms 5.8783.

  5.8783 57385 5737. Ans.
- 22. Reduce to common fractions in their lowest terms 1.69408.

  1.69408 = 188488 = 111888. Ans.
- 23. Reduce to common fractions in their lowest terms 0.48324.  $0.48324 = \frac{48378}{48324} = \frac{447}{447}$ . Ans.
- 24. Reduce to common fractions in their lowest terms 0.0012213.  $0.0012213 = \frac{13213}{91239230} = \frac{1357}{1111100}$ . Ans.

#### EXERCISE XXXV.

1. Find the G.C.M. and L.C.M. of 2, 14, 18.

#### **}} ∽** ₽.

G. C. M. of 7, 14, 2 **–** 1.

L.C.M. of 9, 27, 5 **=** 105,

 $\therefore$  G. C. M. of fractions  $= \frac{1}{\sqrt{4\pi}}$ .

L. C. M. of 7, 14, 2 **-** 14.

G. C. M. of 9, 27, 5 <del>-</del> 1.

.. L. C. M. of fractions = 14.

2. Find the G.C M. and L.C.M. of 21, 21, 48.

24 - 왕, 23 - 남, 송 - 남.

G. C. M. of 20, 12, 1 -1.

L. C. M. of 9, 5, 10 **- 90.** 

... G. C. M. of fractions = 1.

L. C. M. of 20, 12, 1 **=** 60.

G. C. M. of 9, 5, 10 = 1. ∴ L. C. M. of fractions = 60.

Find the G.C.M. and L.C.M. of 33‡, 50‡.

334 - 444, 504 - 444.

G. C. M. of 234, 405

L. C. M. of 7, <del>--</del> 56.

... G. C. M. of fractions = 4.

L. C. M. of 234, 405 -10,530.

G. C. M. of 7, -1.

... L. C. M. of fractions = 10,530.

Find the G.C.M. and L.C.M. 야 돐, 縣, 舒,

G. C. M. of 7, 35, 49

L. C. M. of 24, 36, 60 -360.

... G. C. M. of fractions - +1x.

L. C. M. of 7, 35, 49

G. C. M. of 24, 36, 60 -12.

L. C. M. of fractions — 345 =20%

5. Find the G.C.M. and L.C.M. of 51, 71, 81, 48, 91, 64.

54, 74, 84, 44, 94, 6층 = 부, 후, 부, 부, 두, 꽃,

G.C.M. of 11, 22, 33, 44, 55, 77 = 11.

L. C. M. of 2, 3, 4, 9, 6, 12 **- 36.** 

... G. C. M. of fractions = }}.

L. C. M. of 11, 22, 33, 44, 55, 77 = 4620.

G. C. M. of 2, 3, 4, 9, 6, 12 **--** 1.

.. L. C. M. of fractions -4620.



**-1**. G. C. M. of 1, 1, 1, 1, 1, 1, 1

**- 60.** L. C. M. of 2, 3, 4, 5, 6, 10, 12

.. G. C. M. of fractions - 2/6-

L. C. M. of 1, 1, 1, 1, 1, 1, 1 **-1.** 

G. C. M. of 2, 3, 4, 5, 6, 10, 12 -1.

.. L. C. M. of fractions -1.



7. Find the G.C.M. and L.C.M. of 501, 671, 448, 841, 707.

 $50\frac{1}{2}$ ,  $67\frac{1}{8}$ ,  $44\frac{1}{8}$ ,  $84\frac{1}{6}$ ,  $707 = \frac{101}{2}$ ,  $\frac{202}{8}$ ,  $\frac{404}{9}$ ,  $\frac{505}{8}$ , 707.

G. C. M. of 101, 202, 404, 505, 707 = 101.

L. C. M. of 2, 3, 9, 6, 1 = 18.

.. G. C. M. of fractions  $=\frac{101}{18}=5\frac{1}{18}$ .

L. C. M. of 101, 202, 404, 505, 707 = 14, 140.

G. C. M. of 2, 3, 9, 6, 1-1.

.. L. C. M. of fractions = 14, 140.

8. Find the G. C. M. and L. C. M. of  $\frac{4}{5}$ ,  $\frac{5}{5}$ ,  $\frac{6}{7}$ ,  $\frac{7}{8}$ ,  $\frac{9}{10}$ .

G. C. M. of 4, 5, 6, 7, 8, 9 = 1.

L. C. M. of 5, 6, 7, 8, 9, 10 = 2520.

 $\therefore$  G. C. M. of fractions  $=\frac{1}{2520}$ .

L. C. M. of 4, 5, 6, 7, 8, 9 = 2520.

G. C. M. of 5, 6, 7, 8, 9, 10 = 1.

 $\therefore$  L. C. M. of fractions = 2520.

9. Find the G. C. M. of 112, 111, 43, 43, 25

 $1_{\frac{1}{14}}, 1_{\frac{1}{21}}, 4_{\frac{2}{7}}, \frac{25}{4\frac{5}{2}} = \frac{15}{14}, \frac{40}{21}, \frac{80}{7}, \frac{25}{4\frac{5}{2}}.$ 

G. C. M. of 15, 40, 30, 25 = 5.

L. C. M. of 14, 21, 7, 42 = 42.

 $\therefore$  G. C. M. of fractions  $=\frac{5}{42}$ .

L. C. M. of 15, 40, 30, 25 = 600.

G. C. M. of 14, 21, 7, 42 = 7.

 $\therefore$  L.C.M. of fractions =  $\frac{690}{7}$  =  $85\frac{5}{7}$ .

10. Find the G.C.M. and L.C.M. of 182, 571.

$$18\frac{2}{5} = \frac{92}{5}$$
,  $57\frac{1}{2} = \frac{115}{2}$ .

G. C. M. of 92, 115 = 23.

L. C. M. of 5, 2 - 10.

.. G. C. M. of fractions  $=\frac{28}{10}=2\frac{8}{10}$ .

L. C. M. of 92, 115 = 460.

G. C. M. of 5, 2 - 1.

.. L.C. M. of fractions - 460.

11. Find the G. C. M. and L. C. M. of 1344, 1284, 1154.

 $134\frac{1}{2}$ ,  $128\frac{1}{2}$ ,  $115\frac{1}{2} = \frac{1}{2}$ ,  $\frac{1}{2}$ ,  $\frac{1}{2}$ ,  $\frac{1}{2}$ .

G. C. M. of 539, 385, 231 - 77.

L.C.M. of 4, 3, 2

= 12.

 $\therefore$  G. C. M. of fractions  $=\frac{77}{12}=6\frac{8}{12}$ .

L. C. M. of 539, 385, 231 - 8085.

G. C. M. of 4, 3, 2,

**– 1**.

.. L. C. M. of fractions - 8085.

12. Find the G. C. M. and L. C. M. of 222, 127, 187, 188.

 $2\frac{22}{25}$ ,  $1\frac{27}{75}$ ,  $\frac{68}{100} = \frac{72}{25}$ ,  $\frac{112}{75}$ ,  $\frac{63}{100}$ .

G.C.M. of 72, 112, 63 -1.

L. C. M. of 25, 75, 100 - 300.

.. G. C. M. of fractions - 10.

L. C. M. of 72, 112, 63 - 1008.

G.C. M. of 25, 75, 100 - 25.

.. L. C. M. of fractions  $-\frac{1998}{25} = 40\frac{8}{25}$ .

13. A, B, and C start together and travel round a circular island, in the same direction. It takes A 2½ days, B 2½, C 2¾ days to walk round the island. They travel until they all meet at the point of starting. In how many days will they be together at the point of starting?

 $2\frac{1}{3}$ ,  $2\frac{5}{6}$ ,  $2\frac{7}{8} = \frac{7}{8}$ ,  $\frac{17}{6}$ ,  $\frac{28}{8}$ .

L. C. M. of 7, 17, 23 = 2737.

G. C. M. of 3, 6, 8 = 1.

∴ L. C. M. = 2737.

2737 days. Ans.

14. If the step of a man be 2\frac{1}{3}ft., and that of a horse be 2\frac{2}{3}ft., find the smallest number of feet which is an exact number of man-paces and of horse-paces.

$$2\frac{1}{3}$$
,  $2\frac{3}{4} = \frac{7}{3}$ ,  $\frac{11}{4}$ .

L. C. M. of 7, 11 = 77.

G. C. M. of 3, 4 = 1.

 $\therefore$  L. C. M. = 77.

77 ft. Ans.

15. Find the largest number that is contained without remainder in  $2\frac{5}{9}$ ,  $6\frac{7}{18}$ ,  $11\frac{1}{2}$ , and  $19\frac{1}{6}$ .

25, 
$$6\frac{7}{18}$$
,  $11\frac{1}{2}$ ,  $19\frac{1}{6} = \frac{23}{3}$ ,  $\frac{115}{18}$ ,  $\frac{23}{3}$ ,  $\frac{115}{6}$ .

G. C. M. of 23, 115, 23, 115 = 23.

L. C. M. of 9, 18, 2, 6 = 18.

C. C. M. =  $\frac{24}{18}$  =  $\frac{1}{18}$ .

# EXERCISE XXXVI.

1. Simplify 3788, 48788, 584296, 4887.

$$\frac{2709}{6966} = \frac{7}{18}. \qquad \frac{43785}{56835} = \frac{973}{1263}. \qquad \frac{2436}{567216} = \frac{203}{47268}. \qquad \frac{4087}{5063} = \frac{67}{83}.$$

2. Which is greater, and how much,  $\frac{7}{4}$  or  $\frac{12}{3}$ ?

$$\frac{7}{9}$$
,  $\frac{19}{24} = \frac{56}{72}$ .  $\therefore \frac{19}{24}$  is greater by  $\frac{1}{72}$ .

- 3. Find the sum of  $3\frac{2}{5}$ ,  $2\frac{4}{11}$ ,  $5\frac{1}{2}$ ,  $7\frac{7}{10}$ ,  $1\frac{3}{22}$ .  $3\frac{2}{5} + 2\frac{4}{11} + 5\frac{1}{2} + 7\frac{7}{10} + 1\frac{3}{22} = 18\frac{44}{110} + \frac{55}{110} + 7\frac{7}{110} = 18\frac{23}{110} = 20\frac{1}{10}$ . Ans.
  - 4. Simplify  $5\frac{1}{2} 3\frac{3}{7} + 2\frac{9}{10} 1\frac{3}{5}$ . Sum of plus terms =  $8\frac{3}{5}$ . Sum of minus terms =  $5\frac{1}{35}$ . Difference =  $3\frac{1}{35}$ .
  - 5. Simplify  $1\frac{4}{5} + 3\frac{5}{6} 2\frac{7}{12} + 4\frac{3}{20} 3\frac{7}{15}$ . Sum of plus terms =  $9\frac{47}{60}$ . Sum of minus terms =  $6\frac{3}{60}$ . Difference =  $3\frac{1}{15}$ .
  - 6. Simplify  $\frac{3\frac{1}{2} + 3\frac{5}{6}}{4\frac{1}{2} 2\frac{7}{2}}$  $\frac{3\frac{1}{2} + 3\frac{5}{6}}{4\frac{1}{2} - 2\frac{7}{2}} = \frac{42 + 46}{52 - 31} = \frac{88}{21} = 4\frac{4}{21}. \text{ Ans.}$

7 Simplify the expressions: 
$$7 + 2\frac{1}{4}$$
;  $\frac{7}{1\frac{1}{4}}$ ;  $\frac{95\frac{1}{4}}{8\frac{7}{11}}$ ;  $15 + \frac{7}{3}$ ;  $\frac{16}{5\frac{1}{4}}$ ;  $7\frac{4}{11} + 9$ ,  $43\frac{1}{4} + 37\frac{1}{4}$ ;  $\frac{67}{18\frac{1}{4}}$ ;  $5\frac{4}{6} + 4\frac{1}{6}$ ;  $\frac{1}{4} \cdot \frac{of}{4\frac{1}{3}}$ ;  $106 + 8\frac{1}{6}$ ;  $\frac{17}{4\frac{7}{17}}$ ;  $7 + 2\frac{1}{4} = \frac{4}{11} \times \frac{7}{1} = \frac{28}{11} = 2\frac{1}{11}$ ;  $48\frac{1}{4} + 37\frac{1}{3} = \frac{3}{112} \times \frac{173}{4} = \frac{519}{448} = 1\frac{71}{441}$ ;  $\frac{7}{1\frac{1}{4}} = \frac{8}{11} \times \frac{7}{1} = \frac{56}{11} = 5\frac{1}{11}$ ;  $\frac{67}{18\frac{1}{4}} = \frac{4}{79} \times \frac{79}{11} = \frac{4}{11}$ ;  $\frac{95\frac{1}{4}}{8\frac{7}{11}} = \frac{11}{95} \times \frac{191}{2} = \frac{2101}{190} = 11\frac{11}{118}$ ;  $\frac{54}{4} + \frac{4\pi}{6} = \frac{6}{29} \times \frac{29}{5} = \frac{6}{5} = 1\frac{1}{5}$ ;  $\frac{4}{15} + \frac{2}{3} = \frac{3}{2} \times \frac{15}{1} = \frac{45}{2} = 22\frac{1}{2}$ ;  $\frac{4}{17} \cdot \frac{of}{4} = \frac{1}{9} \times \frac{9}{2} \times \frac{4}{7} \times \frac{2}{8} = \frac{9}{14}$ ;  $\frac{16}{5\frac{1}{4}} = \frac{3}{16} \times \frac{16}{11} = 3$ ;  $106 + 8\frac{1}{4} = \frac{6}{8} \times \frac{169}{2} \times \frac{19}{14} = 12$ ;  $\frac{16}{71} = \frac{3}{75} \times \frac{17}{11} = \frac{289}{75} = 3\frac{4}{7}$ .

$$7\frac{1}{1} \times 8 = \frac{245}{32} \times \frac{9}{1} = \frac{243}{4} = 80\frac{1}{4};$$

$$43\frac{1}{1} \times 6\frac{1}{8} = \frac{573}{8} \times \frac{93}{8} = \frac{578}{2} = 286\frac{1}{2};$$

$$\frac{1}{1} = \frac{5}{41} \times \frac{41}{6} = \frac{5}{6};$$

$$51 = \frac{86}{17} \times \frac{51}{1} = 258;$$

$$\frac{17}{19} \times \frac{228}{1156} = \frac{4}{11};$$

$$\frac{1}{3} = \frac{121}{156};$$

$$\frac{1}{2} \times \frac{3}{8} \times \frac{2}{3} \times \frac{2}{5} = \frac{1}{16};$$

$$\frac{1}{2} \times \frac{3}{4} \times \frac{7}{11} \times \frac{3}{9} \times \frac{3}{7} = \frac{1}{11}.$$

9. By what must \(\frac{1}{2}\) be multiplied to obtain \(\frac{1}{2}\)? \(\frac{1}{2}\) to obtain \(\frac{2}{3}\)? \(\frac{1}{2}\) to obtain \(\frac{1}{3}\)? \(\frac{1}{2}\) to obtain \(\frac{1}{3}\)?

$$\frac{1}{2} + \frac{1}{6} = \frac{3}{1} \times \frac{1}{2} = 3;$$

$$\frac{5}{6} + \frac{1}{2} = \frac{2}{1} \times \frac{5}{6} = \frac{5}{3} = 1\frac{3}{3};$$

$$\frac{2}{3} + \frac{1}{6} = \frac{3}{1} \times \frac{2}{3} = 4;$$

$$\frac{5}{6} + \frac{2}{3} = \frac{3}{2} \times \frac{5}{6} = \frac{5}{4} = 1\frac{1}{2};$$

$$\frac{7}{8} + \frac{3}{5} = \frac{5}{3} \times \frac{7}{8} = \frac{35}{24} = 1\frac{11}{24}.$$

10. By what must \( \frac{1}{6} \) be divided to obtain \( \frac{1}{6} \)? \( \frac{2}{6} \) to obtain \( \frac{1}{6} \)? \( \frac{1}{6} \) to obtain \( \frac{1}{6} \)? \( \frac{1}{6} \) to obtain \( \frac{1}{6} \)? \( \frac{1}{6} \) to obtain \( \frac{1}{6} \)?

$$\frac{1}{6} \div \frac{1}{2} = \frac{2}{1} \times \frac{1}{6} = \frac{1}{3}; \qquad \frac{7}{8} \div \frac{4}{5} = \frac{5}{4} \times \frac{7}{8} = \frac{35}{32} = 1_{\frac{3}{3}}; 
\frac{2}{3} \div \frac{1}{6} = \frac{6}{1} \times \frac{2}{3} = 4; \qquad \frac{3}{5} \div \frac{7}{8} = \frac{8}{7} \times \frac{3}{5} = \frac{24}{35}; 
\frac{5}{6} \div \frac{5}{6} = \frac{6}{5} \times \frac{5}{5} = 1; \qquad 8 \div 7_{\frac{13}{3}} = \frac{32}{243} \times \frac{8}{1} = \frac{256}{243} = 1_{\frac{13}{243}}.$$

11. What number exceeds 5# by 47?

$$53 + 47 = 916 + 68 = 979 = 1073$$

12. From what must 6\\ be subtracted to leave \( \frac{1}{2} \) of 3\\ \frac{1}{2} \cdot ?

$$\frac{1}{2} \times 3\frac{1}{9} = \frac{1}{2} \times \frac{\frac{14}{28}}{9} = \frac{14}{9} = 1\frac{5}{9};$$

$$6\frac{1}{5} + 1\frac{5}{9} = 7\frac{2\cdot 7 + 2\cdot 5}{4\cdot 5} = 7\frac{5\cdot 2}{4\cdot 5} = 8\frac{7}{4\cdot 5}.$$

13. What fraction falls short of  $\frac{7}{12}$  by  $\frac{8}{28}$ ?

$$\frac{7}{12} - \frac{3}{20} = \frac{35 - 9}{60} = \frac{26}{60} = \frac{13}{30}.$$

14. What fraction is that to which  $\frac{5}{76}$  must be added to give  $\frac{1}{27}$ ?

$$\frac{11}{57} - \frac{5}{76} = \frac{44 - 15}{228} = \frac{29}{228}$$

15. Convert into decimals: \(\frac{1}{2}\); \(\frac{1}\); \(\frac{1}\); \(\frac{1}{2}\); \(\frac{1}{2}\); \(

**. **. T#. T#		. 6A.	
2)1.0	8)7.000	0,0625	6)1.00
0.5	0.875	9	0.16
4)1.00	16)1.0000	0.5625	
4)1.00 0.25	ED: COMMON CO		6 <u>)</u> 5,00 0,83
2)1.0		Q.0625	0.83
3)1.0	0.0625	11	
0.3	3	0.6875	7)3.000000
4)3.00	0.1875	0.0010	0.428571
0.75		0.0625	9\5.0
8)1.000	0.0625	13	9 <u>)5.0</u> 0.5
0.125	5		0.5
8)3.000	0.3125	0.8125	11)3.00
0.375	0.0625	0.0625	0.27
	7	15	
8)5.000			4)0.700
0.625	0.4375	0.9375	0.175

16. Convert into common fractions: 0.16; 0.016; 0.125; 0.13; 0.725; 0.625; 0.00625; 0.8125; 0.03125; 0.08; 0.54; 0.016, 0.5437, 0.027, 0.277; 0.68494; 1.345.

18. Multiply 6.954 by 5.303, and express the result as a whole number and common fraction.

- 19. Simplify  $1\frac{1}{2}$  of  $2\frac{4}{5} + 6\frac{7}{5} + 2\frac{3}{4}$  and reduce the result to a decimal.  $1\frac{1}{2} \times 2\frac{4}{5} + 6\frac{7}{5} + 2\frac{3}{4} = \frac{3}{2} \times \frac{14}{5} + \frac{4}{11} \times \frac{55}{5} = 4\frac{1}{5} + 2\frac{1}{4} = 6\frac{2+5}{10} = 6\frac{7}{10} = 6.7$ .
- 20. From what number can 417 be taken 9 times and leave no remainder?

$$4\frac{17}{36} \times 9 = \frac{161}{36} \times \frac{9}{1} = \frac{161}{4} = 40\frac{1}{4}.$$

21. Of what fraction is 171 the 7th part?

$$17\frac{1}{3} \times 7 = \frac{52}{3} \times \frac{7}{1} = \frac{364}{3} = 121\frac{1}{3}.$$

22. Add \(\frac{4}{5}\), 0.35, \(\frac{8}{5}\), \(\frac{3}{5}\), 0.112, 45.28.

$$\frac{4}{5} + 0.35 + \frac{5}{5} + \frac{3}{4} + 0.112 + 45.28$$
  
=  $0.8 + 0.35 + 0.625 + 0.75 + 0.112 + 45.28 = 47.917$ .

23. Convert into decimals  $\frac{18}{18}$ ;  $\frac{8}{11}$ ;  $\frac{4}{35}$ ;  $\frac{17}{80}$ ;  $\frac{14}{18}$ ;  $\frac{5}{18}$ ;  $\frac{7}{88}$ .

24. What part of  $\frac{15}{18}$  is  $\frac{8}{1241}$ ?

$$\frac{3}{1241} + \frac{15}{73} = \frac{73}{13} \times \frac{3}{1241} = \frac{1}{85}.$$

25. Divide 0.0015 by 0.012, and express the result as a common fraction in lowest terms.

$$\begin{array}{c}
0.125 \\
12)1.500
\end{array}$$

$$0.125 = \frac{1}{4}.$$

26. Convert into decimals: 32; 32800; \$\frac{1}{4}; \$\frac{1}{4}\$.

0.09375

0.00009375 32)0.00300000 0.2297 74)17.0000 0.141857 7)1.000000

27. If the product of two factors is  $\frac{\pi}{2}$ , and one factor is  $1\frac{1}{4}$ , find the other factor.

$$\frac{5}{8} + 1\frac{1}{2} - \frac{4}{5} \times \frac{5}{8} - \frac{1}{2}$$

28. If the dividend is 11 and the quotient 61, find the divisor.

$$\frac{11}{12} + 6\frac{1}{2} = \frac{2}{13} \times \frac{11}{12} = \frac{11}{78}$$

29. The dividend is  $12\frac{17}{12}$ , quotient 3, remainder  $1\frac{5}{12}$ ; find the divisor.

$$(12\frac{17}{72} - 1\frac{5}{12}) + 3 = 10\frac{59}{72} + 3 - \frac{1}{8} \times \frac{779}{72} - \frac{779}{218} - 3\frac{181}{218}.$$

30. Find the G.C.M. and the L.C.M of 833, 1127, 1421, 343.

G. C. M.  $-7 \times 7 - 49$ .

L. C. M. 
$$= 7^3 \times 17 \times 23 \times 29 = 3,889,277$$
.

31. Arrange in order of magnitude 9, 22, 12, 17, 28.

$$\frac{2}{11} = \frac{4848}{848}$$
.  $\frac{23}{48} = \frac{4324}{8948}$ .  $\frac{13}{49} = \frac{4328}{8948}$ .

32. Find the L.C.M. of  $\frac{15}{17}$ ,  $\frac{25}{51}$ ,  $\frac{65}{102}$ .

L.C. M. of 15, 26, 65 = 390.

G. C. M. of 17, 51, 102 - 17.

 $\therefore$  L.C.M. of fractions =  $\frac{390}{17}$  =  $22\frac{15}{17}$ .

33. Find the G. C. M. of \$5, \$2, \$1, and 61.

G. C. M. of 65, 39, 91, 13 = 13.

L. C. M. of 68, 2, 64, 2 = 1088.

... G. C. M. of fractions  $=\frac{18}{1088}$ .

34. Convert into common fractions in lowest terms: 7.2011; 6.954; 5.303; 21.396.

7.2011 = 
$$7\frac{2000}{3000}$$
.  
6.954 =  $6\frac{45}{300}$  =  $6\frac{21}{22}$ .  
5.303 =  $5\frac{200}{300}$  =  $5\frac{10}{300}$ .  
21.396 =  $21\frac{20}{300}$  =  $21\frac{44}{111}$ .

35. Simplify 
$$\frac{3\frac{7}{6} \times 1_{1\frac{1}{4}} + 4_{1\frac{1}{2}} - 3_{1\frac{1}{6}}}{5\frac{1}{6} - 7\frac{7}{8} + 28\frac{7}{20} + \frac{1}{8}}$$
$$\frac{3\frac{7}{6} \times 1_{1\frac{1}{7}} + 4_{1\frac{1}{2}} - 3_{1\frac{1}{6}}}{5\frac{1}{6} - 7\frac{7}{8} + 28\frac{7}{20} + \frac{1}{8}} = \frac{4 + 4_{1\frac{1}{2}} - 3_{1\frac{1}{6}}}{5\frac{1}{8} - \frac{1}{8} + \frac{1}{8}} = \frac{7}{8}.$$

36. Simplify 
$$\frac{6\frac{3}{4} + 5\frac{1}{2} \times 3\frac{1}{7} - 7\frac{1}{4}}{3\frac{1}{5} + 2\frac{1}{2} - 4\frac{1}{10}}$$

$$\frac{6\frac{3}{4} + 5\frac{1}{2} \times 3\frac{1}{7} - 7\frac{1}{4}}{3\frac{1}{5} + 2\frac{1}{2} - 4\frac{1}{10}} = \frac{6\frac{3}{4} + 17\frac{3}{7} - 7\frac{1}{4}}{3\frac{1}{6} + 2\frac{1}{2} - 4\frac{1}{10}}$$

$$= \frac{945 + 2420 - 1015}{448 + 350 - 574} = \frac{2350}{224} = 10\frac{55}{112}.$$

37. Simplify 
$$\frac{2\frac{4}{8} - 1\frac{1}{2} + 9\frac{1}{11}}{4\frac{1}{8} - 2\frac{1}{4} + 13\frac{7}{11}}$$
$$\frac{2\frac{4}{8} - 1\frac{1}{4} + 9\frac{1}{11}}{4\frac{1}{8} - 2\frac{1}{4} + 13\frac{7}{11}} = \frac{616 - 330 + 2000}{924 - 495 + 3000} = \frac{2286}{3429} = \frac{2}{3}$$

38. Simplify 
$$\frac{(3.71 - 1.908) \times 7.03}{2.2 - \frac{74}{3.33}}$$
$$\frac{(3.71 - 1.908) \times 7.03}{2.2 - \frac{74}{3.33}} = \frac{12.66806}{2} = 6.33403.$$

39. Simplify 
$$\frac{5\frac{5}{8} + \frac{2}{8}}{1\frac{1}{8} \text{ of } \frac{5}{8} + 10\frac{1}{3}} \times \frac{2}{8} \text{ of } \frac{1\frac{1}{2} \text{ of } 4\frac{1}{3}}{13\frac{7}{8} \text{ of } 5\frac{1}{3}}$$
.
$$\frac{5\frac{5}{8} + \frac{2}{8}}{1\frac{1}{8} \text{ of } \frac{5}{8} + 10\frac{1}{3}} \times \frac{2}{8} \text{ of } \frac{1\frac{1}{2} \text{ of } 4\frac{1}{3}}{13\frac{7}{8} \text{ of } 5\frac{1}{3}}$$

$$= \frac{45}{8} \times \frac{3}{2} \times \frac{5}{8} \times \frac{9}{8} \times \frac{31}{8} \times \frac{2}{8} \times \frac{3}{2} \times \frac{37}{9} \times \frac{37}{111} \times \frac{3}{16} = \frac{279}{64} = 4\frac{28}{64}.$$

40. Simplify 
$$1\frac{1}{3}$$
 of  $2\frac{1}{3} + 6\frac{1}{3} + 2\frac{1}{4} + \left(5\frac{1}{3} + \frac{0.24 + 0.53}{2.2 - 0.64}\right)$ .

 $1\frac{1}{3}$  of  $2\frac{1}{4} + 6\frac{1}{3} + 2\frac{1}{4} + \left(5\frac{1}{4} + \frac{0.24 + 0.53}{2.2 - 0.64}\right) - 4\frac{1}{3} + 2\frac{1}{3} + 5\frac{1}{2} + \frac{44}{14}$ 

$$= 4\frac{1}{3} + 2\frac{1}{4} + 5\frac{1}{3} + \frac{261}{334} = 11\frac{21.0 + 5.2.5 + 5.2.5}{10.6.6}$$

$$= 11\frac{11}{10.6}\frac{1}{10.6} = 12\frac{11}{10.6}$$

41. Simplify 0.9 of # of # of 15#.

0.9 of 
$$\frac{4}{5}$$
 of  $\frac{4}{5}$  of  $15\frac{4}{5} = \frac{9}{19} \times \frac{3}{3} \times \frac{4}{7} \times \frac{9}{4} = \frac{81}{16} = 5\frac{1}{16}$ .

42. What part of # 18 #

$$\frac{1}{4} - \frac{1}{2} \times \frac{3}{2} - \frac{3}{4}$$

43. What part of 0.390625 is 0.05?

$$\frac{0.05}{0.390625} - \frac{1}{\frac{1}{15}} = \frac{\frac{16}{94}}{\frac{1}{25}} \times \frac{1}{\frac{1}{29}} = \frac{16}{125}.$$

44. 0.09 is what fraction of 0.2045?

$$\frac{0.09}{0.2045} = \frac{1}{1888} = \frac{1}{22} = \frac{4}{9}.$$

t into decimals ##; ##; ##.

0.73134328358208955223880597014925\$

C. M. of three numbers is 15, and their L. C. M. is 450 numbers?

$$450 = (5 \times 3) \times 2 \times 3 \times 5$$
  
 $5 \times 3 = 15 = G, G, M,$   
 $15 \times 2 = 30,$   
 $15 \times 3 = 45,$   
 $15 \times 5 = 75,$ 

## EXERCISE XXXVII.

1. Reduce 3 yds. 2 ft. to inches.

3 yds. 2 ft.  

$$\times \frac{3}{9}$$
  
 $\frac{2}{11}$  ft.  
 $\times \frac{12}{132}$  in.

2. Reduce 4 mi. 124 rds. to feet. 4 mi. 124 rds.

3. Reduce 27 rds. 41 yds. to inches.

4. Reduce 290 leagues to feet.

290 leagues.  

$$\frac{\times 3}{870}$$
 knots.  
 $\frac{\times 6086}{5294820}$  ft.

5. Reduce 82,976,432 in. to miles.

12|82976432 in.

1309 mi. 192 rds. 4 yds. 2 ft. 8 in.

6. Reduce 7 mi. 3½ yds. to inches.

7. Reduce 27 mi. 222 rds. to inches.

8. Reduce 712 mi. to mches.

9. Reduce 540,451 ft. to miles.

11 360300 820 32754 rds. 6 half-yards = \$ yds. 102 mi. 114 rds. 102 m. 114 rds. 3 yds. 1 ft.

16. Reduce 271,256 in. to miles,

sduce 723,964 ft. to miles.

11 482642 320 43876 rds. 6 half-yards = 3 yds. 137 mi. 36 rds. 137 mi. 36 rds. 3 yds. 1 ft. 12. Reduce 238,205 in. to miles.

13. Reduce 10 chains to inches.

14. Reduce 289,185 in. to fathoms.

3238 fath. 4 ft. 1 in.

15. If the height of a horse be 16 hands, how many feet is his height?

16. If a train move 40 ft. in a second, what is its rate in miles per hour? (One hour = 3600 seconds.)

3600  
40 ft.  

$$5280)144000$$
 ft.  
 $27\frac{148}{288}$  mi.  
 $=27\frac{3}{11}$  mi.

## EXERCISE XXXVIII.

1. Reduce 92,638 sq. yds. to inches. 92638 sq. yds.

2. Reduce 1,223,527 sq. in. to yards.

3. Reduce 721 sq. mi. to rods.

4. Reduce 34,729 sq. yds. to rods.

6. Reduce 1 A. to feet,

5. Reduce 3 A. 107 sq. rds. 27 sq. yds. 7 sq. ft. 23 sq. in. to inches.

Reduce 99,894,712 sq. in. to acres.

15 A. 148 sq. rds. 2 sq. yds. 2 sq. ft. 40 sq. in.

8. Reduce 15,376 sq. yds. to acres.

301)15376 sq. yds.

121)61504

160)508 sq. rds. 36 quarter-sq. yds = 9 sq. yds. 3 A. 28 sq. rds.

3 A. 28 sq. rds. 9 sq. yds.

9. Reduce 562,934 sq. in. to rods.

144)562934 sq. in.

9)3909 sq. ft. 38 sq. in.

30½)434 sq. yds. 3 sq. ft.

4 121)1736

14 sq. rds. 42 quarter-sq. yds. - 101 sq. yds.

14 sq. rds.  $10\frac{1}{2}$  sq. yds. 3 sq. ft. 38 sq. in.

- 14 sq. rds. 10 sq. yds. 7 sq. ft. 110 sq. in.

## EXERCISE XXXIX.

1. Reduce 7 cu. yds. 13 cu. ft. to cubic feet.

7 cu. yds. 13 cu. ft. × 27 189 13 202 cu. ft.

2. Reduce 25 cu. yds. 5 cu. ft. 143 cu. in. to cubic inches.

25 cu. yds. 5 cu. ft. 143 cu. in.

 $\times \frac{27}{675}$ 

5 380 on 3

680 ca. ft.

 $\frac{\times 1728}{1175040}$ 

143

1175183 cu. in.

3. Reduce 74,325 cu. in. to cubic feet.

1728)74325 cu. in.

43 cu. ft. 21 cu. in.

43 cu. ft. 21 cu. in.

4. Reduce 439,000 cu. in. to cubic yards.

1728)439000 cu. in.

27)254 cu. ft. 88 cu. in.

9 cu. yds. 11 cu. ft.

9 cu. yds. 11 cu. ft. 88 cu. in.

5. Reduce 921,730 cu. in. to cubic yards.

1728)921730 cu. in.

27)533 cu. ft. 706 cu. in.

19 cu. yds. 20 cu. ft.

19 cu. yds. 20 cu. ft. 706 cu. in.

6. Wood cut in lengths of 4 ft. is piled to a height of 3½ ft. How long must the pile be to contain a cord?

7. A pile of wood 127 ft. long, 4 ft. wide, and 3 ft. 8 in. high is sold for \$7 a cord. How much money is received for it?

127 ft.  

$$\times 4$$
 ft.  
508 sq. ft.  
 $\times 3\frac{2}{3}$   
128)18624  
 $14\frac{3}{5}$  cd.  
 $\times 37$   
 $\times 101\frac{2}{5}$  = \$101.86.

## EXERCISE XL.

1. Reduce 3 pks. 5 qts. 1 pt. to pints.

2. Reduce 4234 pts. to bushels.

59 pts.

8. Reduce 24 gals. 2 qts. 1 pt. 2 gi. to gills.

4. Reduce 272 liquid quarts to dry quarts.

$$\frac{272}{1} \times \frac{57\frac{8}{4}}{67\frac{1}{8}} = \frac{272}{1} \times \frac{231}{4} \times \frac{5}{336} = \frac{935}{4} = 233\frac{3}{4} \text{ qts.}$$

5. Reduce 400 dry quarts to liquid quarts.

$$\frac{67\frac{1}{5}}{57\frac{4}{2}} \times 400 = \frac{\frac{16}{336}}{\cancel{5}} \times \frac{4}{\cancel{231}} \times \frac{\cancel{499}}{1} = \frac{5120}{11} = 465\frac{5}{11} \text{ qts.}$$

6. Express a bushel in cubic feet, carrying the decimal to three places.

7. Express a cubic foot as the decimal fraction of a bushel.

8. Reduce 17151 bushels to pints.

$$\frac{1715\frac{1}{4} \text{ bu.}}{\times 64}$$
 $\frac{\times 64}{109792 \text{ pts.}}$ 

9. 3047 gals. to barrels.

$$\frac{3047}{31\frac{1}{2}} = \frac{3047}{1} \times \frac{2}{63} = \frac{6094}{63} = 96\frac{46}{63} \text{ bbl.}$$

## EXERCISE XLI.

1. Reduce 27,587 grs. to pounds troy.

4 lbs. 9 oz. 9 dwt. 11 grs.

2. Reduce 34,652 lbs. to long tons.

3. Reduce 136,851 oz. to tons.

4 t. 5 cwt. 53 lbs. 3 oz.

4. Reduce 864,205 grs. (troy) to pounds.

5. Reduce 864,205 grs. (apoth.) to pounds avoirdupois.

Reduce 5 lbs. 7 os. 6 dwts.grs. to grains.

7. Reduce 745 lbs. avoirdupois to troy weight.

$$\frac{175}{7999} \times \frac{745}{1}$$
 lbs.

= 905 to 164 lbs.
 os. 11 dwt. 16 grs.
 745 lbs. troy to sight.
 149
 × 745 lbs.

- $-613\frac{1}{35}$  lbe.
- = 613 lbs. 711 drs.

Reduce 23,047,125 drs. to tons.

> 16)23047125 drs. 16)1440445 oz. 5 drs. 100)90027 lbs. 13 os. 20)900 cwt. 27 lbs. 45 t.

45 t. 27 lbe. 13 oz. 5 drs.

Reduce 90,252,381 drs. te tons.

16)90252381 drs. 16)5640773 os. 13 drs. 100)332548 lbs. 5 os. 20)3525 cwt. 48 lbs. 176 t. 5 cwt.

176 t. 5 cwt. 48 lbs. 5 oz. 13 drs.

11. Reduce 1 pint to minims.

1 fl. oz. xvj.

16
16 fl. drm, viij.

8
128 M. lx.
60
7680 M.

12. Reduce 8000 m, to ounces.

60)8000 m 8)135 m lx. 20 m. 16 fl. drm. viij 5 m lx.

16 fl. drm. viij. 5 դլ lz. 20 դլ.

### EXERCISE XLII.

1. Reduce 6 hrs. 17 min. 25 sec. to seconds.

2. Reduce 1 yr. 13 dys. 4 min. to minutes.

1 yr. 13 d. 4 min.  

$$\times \frac{365}{365}$$
  
 $\frac{13}{378}$  d.  
 $\times \frac{24}{9072}$  h.  
 $\times \frac{60}{544320}$   
 $\frac{4}{544324}$  min.

3. Reduce 48,567 min. to days. 60)48567 min.

24)809 hrs. 27 min. 33 d. 17 hrs.

33 d. 17 hrs. 27 min.

4. Reduce 742,392 sec. to days.

60)742392 sec. 60)12373 min. 12 sec. 24)206 hrs. 13 min. 8 d. 14 hrs.

8 d. 14 hrs. 13 min. 12 sec.

5. Find the number of days, reckoning from noon of the one to noon of the other, between the following days in the year 1880: July 4 and December 2; February 1 and May 29; January 3 and October 15; also, between December 25, 1880, and May 25, 1881.

6. How many minutes are there from midnight of March 7 to midnight of June 20?

 Find the number of seconds from eight o'clock Monday morning till six o'clock the next Saturday evening.

16 hm.
24 hrs.
24 hrs.
24 hrs.
24 hrs.
18 hrs.
180 hrs.
× 60
7800 min.
× 60

8. Which of the years 1600, 1656, 1700, 1734, 1800, 1818, 1880, 1900, 1924, 2000 are lesp years?

1600 (divisible by 400). 1656 " " 4). 1880 " " 4). 1924 " " 4). 2000 " " 400).

#### EXERCISE XLIII.

Reduce 2° 30′ 25′′ to seconds.

a 15° 3′ 22″ to seconds.

Reduce 56,760" to degrees.

Reduce 212,221" to degrees.

5. The hour and minute hands of a watch form an angle of how many degrees at 3 o'clock? at 4 o'clock? at 6 o'clock? at 7½ o'clock? at 11 o'clock? at 12 o'clock?

$$\frac{3}{12} = \frac{1}{4} = 90^{\circ}. \qquad \frac{4}{12} = \frac{1}{8} = 120^{\circ}. \qquad \frac{6}{12} = \frac{1}{2} = 180^{\circ}.$$

$$\frac{1\frac{1}{2}}{12} = \frac{1}{12} \times \frac{9}{2} = \frac{1}{8} = 45^{\circ}. \qquad \frac{1}{12} = 30^{\circ}. \qquad \frac{0}{12} = 0^{\circ}.$$

6. How many geographical miles in the width of the torrid zone (46° 55')? How many statute miles?

$$46^{\circ} 55' = 46\frac{55}{66}^{\circ} = 46.91\frac{1}{3}$$
.

 $\times 60$ 
 $2760$ 
 $55$ 
 $2815'$ 
 $= 2815 \text{ geog. mi.}$ 
 $46^{\circ} 55' = 46\frac{5}{66}^{\circ} = 46.91\frac{1}{3}$ .

 $\times 69.16$ 
 $3244.7566\frac{1}{3}$ 
 $= 3244.75\frac{1}{3} \text{ stat. mi.}$ 

### EXERCISE XLIV.

1. Reduce £583 6 s. 8 d. to pence.

£583 6 s. 8 d.  

$$\frac{\times 20}{11660}$$
  
 $\frac{6}{11666}$  s.  
 $\frac{\times 12}{139992}$   
 $\frac{8}{140000}$  d.

2. Reduce £79 18 s.  $11\frac{1}{2}d$ . to farthings.

£79 18 s. 
$$11\frac{1}{2}$$
 d.  
 $\frac{\times 20}{1580}$   
 $\frac{18}{1598}$  s.  
 $\frac{\times 12}{19176}$   
 $\frac{11\frac{1}{2}}{19187\frac{1}{2}}$  d.  
 $\frac{\times 4}{76750}$  far.

3. Reduce 28,572 d. to pounds.

4. Reduce 272,191 d. to half-sovereigns.

5. Reduce 27,281 crowns to guineas.

#### ARITHMETIC.

ce 1,716,114 guineas

1716114 g.  $\times 21$ 

36038394 s.

:1801919 14 a.

291,374 far. to

291374 far.

2)72843 d. 2 far.

20)6070 a. 3 d.

£303 10 s.

3 10 s. 3 d. 2 far.

ce 709,126d. to guiness.

2)709126 d.

21)59093 a. 10 d.

2813 g. 20 a.

3 g. 20 s. 10 d.

9. Reduce 286,347 far. to Crowns.

4)286347 far.

12)71586 d. 3 far.

5)5965 s. 6 d.

1193 crowns.

1193 crowns 6 d. 3 far.

10. Reduce 20 france to dollars.

\$0.193

 $\times 20$ 

\$3.86

11. Reduce 20 marks to dollars.

\$0.238

 $\times 20$ 

\$4.78

12. Reduce 5 roubles to dollars.

\$0.734

 $\times 5$ 

\$3.67

d the whole sum of money in a box containing 35 soveralf-sovereigns, 13 crowns, 41 half-crowns, and 85 shillings.

overeigns = 700 s.

ialf-sov. = 270 s.

- 65 s. TOWNS

ialf-crowns = 1024 s.

hillinge

12221 s.

20)12221 4.

£61 2} 4.

-£61 2 a. 6 d.

#### EXERCISE XLV.

ess 59° F. in Centigrade scale; in Réaumur's scale. 59° F. is 27° above freezing-point.

$$\frac{3}{27} \times \frac{5}{9} = 15^{\circ} \text{ C}.$$

$$\frac{3}{27} \times \frac{4}{9} = 12^{\circ} \text{ R.}$$

2. Express 77° F. in Centigrade scale; in Réaumur's scale.

77° F. = 45° above freezing-point.

$$\frac{5}{45} \times \frac{5}{9} \text{ C.} = 25^{\circ} \text{ C.}$$
  $\frac{45}{1} \times \frac{4}{9} \text{ R.} = 20^{\circ} \text{ R.}$ 

3. Express 950° F. in Centigrade scale; in Réaumur's scale.
950° F. = 918° above freezing-point.

$$\frac{102}{918} \times \frac{5}{9} \text{ C.} = 510^{\circ} \text{ C.} \qquad \frac{918}{1} \times \frac{4}{9} \text{ R.} = 408^{\circ} \text{ R.}$$

4. Express – 40° F. in Centigrade scale; in Réaumur's scale.

– 40° F. = 72° below freezing-point.

$$\frac{5}{9}$$
 of  $-72^{\circ}$  C.  $= -40^{\circ}$  C.  $\frac{4}{9}$  of  $-72^{\circ}$  R.  $= -320^{\circ}$  R.

5. Express - 4° F. in Centigrade scale; in Réaumur's scale.
 -4° F. = 36° below freezing-point.

$$\frac{5}{9}$$
 of  $-36^{\circ}$  C. =  $-20^{\circ}$  C.  $\frac{4}{9}$  of  $-36^{\circ}$  R. =  $-16^{\circ}$  R.

- 6. Express 10° C. in Fahrenheit's scale; in Réaumur's scale.  $10^{\circ} \text{ C.} = \frac{9}{5} \text{ of } 10^{\circ} + 32^{\circ} \text{ F.} = 50^{\circ} \text{ F.}$   $\frac{4}{5} \text{ of } 10^{\circ} \text{ R.} = 8^{\circ} \text{ R.}$
- 7. Express 22° C. in Fahrenheit's scale; in Réaumur's scale. 22° C. =  $\frac{9}{5}$  of 22° + 32° F. =  $71\frac{3}{5}$ ° F.  $\frac{4}{5}$  of 22° R. =  $17\frac{3}{5}$ ° R.

8. Express – 30° C. in Fahrenheit's scale; in Réaumur's scale.

$$-30^{\circ} \text{ C.} = \frac{9}{5} \times -30^{\circ} + 32^{\circ} \text{ F.} = -22^{\circ} \text{ F.}$$
  $\frac{4}{5} \times -30^{\circ} \text{ R.} = -24^{\circ} \text{ R.}$ 

9. Express – 113° C. in Fahrenheit's scale; in Réaumur's scale.

$$-11\frac{3}{7}$$
° C.  $=\frac{3}{5}\times-11\frac{3}{7}$ ° + 32° F.  $=11\frac{3}{7}$ ° F.  $\frac{4}{5}\times-11\frac{3}{7}$ ° R.  $=-9\frac{1}{7}$ ° R.

10. Express 4° R. in Fahrenheit's scale; in Centigrade scale.

4° R. = 
$$\frac{9}{4}$$
 of 4° + 32° F. = 41° F.  $\frac{5}{4}$  of 4° C. = 5° C.

11. Express 12° R. in Fahrenheit's scale; in Centigrade scale. 12° R. =  $\frac{9}{4}$  of 12° + 32° F. = 59° F.  $\frac{5}{4}$  of 12° C. = 15° C. on the continue of the continu

 $-13^{\circ}$  F.  $\frac{1}{2}$  of  $-20^{\circ}$  C.  $=-25^{\circ}$  C.

it's scale; in Réanmur's scale.

de scale; in Réanmur's scale. ow freezing-point.

4 of - 32° B. = - 144° R.

### BE XLVI.

### 4. Add:

mi.	rds.	yda.	ff.	in.
6	120	8	2	2
18	15	1	1	6
3	215	2	2	3
7	95	1	1	8
35	126	31	1	7
		1-	- 1,	_6
35	126	4	0	1

### 5. Add:

A.	ėų, 24a,	eq. yde.	eq. ft.	eq. to
74	21	5	4	100
23	37	13	5	83
12	106	17	8	7
41	50	23	0	24
151	55	294	0	70
			6	108
151	55	29	7	34

M Add 5 bu. 3 pks. 6 qts. 1 pt.; 6 bu. 2 pks. 7 qts.; 7 bu. 1 pk. 1 qt. 1 pt.; 1 pk. 7 qts.; 2 bu. 3 pks. 1 pt.

bu.	pks.	qts.	pts.
5	3	6	1
6	2	7	0
7	1	1	1
0	1	7	0
2	3	0	1
23	0	6	1

7. Add 48 t. 13 cwt. 75 lbs. 6 oz. 4 drms.; 25 t. 12 cwt. 27 lbs. 8 oz. 13 drms.; 51 t. 10 cwt. 44 lbs. 15 drms.; 80 t. 5 cwt. 6 oz.; 19 cwt. 27 lbs.; 25 lbs. 8 oz. 10 drms.; 5 t. 5 cwt. 5 oz.

t.	ow t.	lbs.	OS.	drs.
48	13	<b>7</b> 5	6	4
25	12	27	8	13
51	10	44	0	15
80	5	0	6	0
0	19	27	0	0
0	0	<b>25</b>	8	10
5	5	0	<b>5</b>	0
212	6	0	3	10

8. Add 50 gals. 3 qts. 1 pt. 3 gi.; 12 gal. 1 qt. 1 pt. 1 gi.; 5 gals. 2 qts. 1 pt. 2 gi.; 75 gal. 3 qts. 1 pt. 3 gi.; 80 gals. 3 qts. 0 pts. 1 gi.; 17 gals. 1 qt. 1 pt. 3 gi.

gals.	q <b>ts</b> .	pie.	gi.
<b>50</b>	3	1	3
12	1	1	1
5	2	1	2
<b>7</b> 5	3	1	3
80	3	0	1
17	1	1	3
<b>24</b> 3	1	0	1

9. Add 13 lbs. 4 oz. 8 dwt. 6 grs.; 25 lbs. 8 oz. 13 dwt. 20 grs.; 8 lbs. 11 oz. 14 grs.; 20 lbs. 16 dwt. 8 grs.; 15 lbs. 9 oz. 12 dwt.; 4 oz. 3 dwt.

lbs.	08.	dwt.	grs.
13	4	8	6
25	8	13	20
8	11	0	14
20	0	16	8
15	9	12	0
0	4	<b>3</b>	0
84	2	14	0

10. Add 4 gals. 3 qts. 1 pt.; 3 gals. 2 qts. 1½ pts.; 12 gals. 3 qts.; 14 gals. 1½ pts.; 5 gals. 2 qts. 1 pt.

gals.	qts.	pta.
4	3	1
3	2	11/2
<b>12</b>	3	0
14	0	$1\frac{1}{2}$
5	2	1
41	0	1

11. Add 60° 50′ 50′′; 20° 41′ 52′′; 30° 25′ 20′′; 20° 32′ 43′′.

•	•	· <b>#</b>
60	<b>50</b> -	<b>5</b> 0 ~
20	41	<b>52</b>
<b>30</b>	<b>25</b>	20
20	<b>32</b>	43
132	30	45

#### EXERCISE XLVII.

1. Subtract 23 lbs. 8 oz. 19 dwt. 10 grs. from 58 lbs. 6 oz. 17 dwt. 21 grs.

58	6	17	21
23	8	19	10
34	9	18	11

2. Subtract 5 bu. 1 pk. 6 qts. 1 pt. from 5 bu. 3 pks. 3 qts.

5 5	pks. 3	ун. З	pia. O
5	1	6	ī
	1	4	1

3. Subtract 32 cu, yds. 13 cu. ft. 1600 cu. in from 39 cu. yds. 17 cu. ft. 1400 cu. in.

39	17	es. in. 1400
32	13	1600
-	3	1528

£92 15 a 1½ d.
a. 4 d.
13 4
15 1½
18 2 3 far.

22 gals, 3 qts, 1 pt, 2 qts, qts, pts.

6. Subtract 17 t. 7 cwt. 17 lbs. 8 oz. 10 drs. from 25 t. 13 cwt. 15 lbs. 12 oz. 5 drs.

25	13	15	12	<b>473.</b> 5
$\frac{17}{8}$	5	17 98	-6 5	$\frac{10}{11}$

Subtract 13 A. 150 sq. rds.
 sq. ft. 10 sq. in. from 20 A.

20 13	ng. rde. 0 150	98	aq. in. 0 10
6	9	1731	134
		. 4-	- 36
6	9	174	26

8. Subtract 58° 33′ 36″ from 90° 11′ 21″.

٥		
90	11	21
58	33	36
31	37	45

Subtract 2 yrs, 213 dys. 17
 hrs. from 3 yrs. 147 dys, 14 hrs.

3	147	14
2	213	17
	298	21

10. Subtract 3 mi. 217 rds. 4 yds. 1 ft. 3 in. from 4 mi. 100 rds. 3 yds.

4 3		100 217	74a. 3 4	n. 0 1	0 3
_	202	31	1	9	
—	202	4	0	 	

# EXERCISE XLVIII.

1. Multiply £31 2 s. 6½ d. by 8.

£,	8.	đ.
31	2	6 <del>1</del>
		8
249	0	4

2. Multiply 19 gals. 3 qts. 1 pt. by 70.

gals,	qts.	pts.		
19	3	1 '		
		70		
1391	1	0		

3. Multiply 3 lbs. 4 oz. 8 dwt. 10 grs. by 10.

ibe.	•z. 4	dwt. 8	grs. 10
-			10
33	8	4	4

4. Multiply 5 t. 10 cwt. 67 lbs. by 10.

<b>t</b> 5	owt. 10	1bs. 67 10
55	6	70

5. Multiply 43 bu. 2 pks. by 63

6. Multiply 15 wks. 3 dys. 5 hrs. 12 min. by 7.

wks. 15	dys. 3	hrs. 5	min. 12 7
108	1	12	24

7. Multiply 5 cu. yds. 16 ca. ft. 371 cu. in. by 6.

ou. yds. 5	ou. ft. 10	en. in 371	
		6	
32	7	498	

8. Multiply 27 A. 76 sq .ds. 22 sq. yds. 5 sq. ft. by 90.

A. sq. rds. sq. yds. sq. ft.

	<b>27</b>	76	22	5	
				9	
	247	50	211	0	
			1/2 =	= 4 <u>1</u>	
	247	50	21	41	
sq. mi.			•	10	
3	553	27	31	0	sq. in.
			_	= 2	36
3	553	27	3	2	36

9. Multiply 32 rds. 3 yds. 1 ft. by 57.

57  

$$\times \frac{1}{3}$$
  
 $3)\overline{57}$   
 $19$  yds.  
 $5\frac{19}{190}$   
 $5\frac{1}{190}$   
 $5\frac{1}{190}$   
 $320)$   
 $1824$   
 $5\frac{1}{1824}$   
 $320)$   
 $1858$   
 $5$  mi. 258 rds.  
 $11)$   
 $380$   
 $34$  ... 6 half-yds. = 3 yds.

5 mi. 258 rds. 3 yds. Ans.

10. Multiply 34 dys. 10 hrs. 13 min. 12 sec. by 108.

10 yrs. 67 dys. 23 hrs. 45 min, 36 sec. Ans.

11. Multiply 5 mi. 126 rds. 19 yds. 6 in. by 7125.

7125  

$$\times 6$$
  
12 42750  
 $3 \frac{3562}{1187} \dots 6 \text{ in.}$   
 $1187 \dots 1 \text{ ft.}$   
 $2 \frac{2}{11) \frac{273124}{24829} \dots \frac{4}{2} = 2\frac{1}{2} \text{ yds.}$ 

7125	7125
$\times 126$	$\times 5$
<b>320</b> ) 897750	35625
2883 19 rds.	2883
	38508 mi

38,508 mi. 19 rds. 2½ yds. 1 ft. 6 in. = 38,508 mi. 19 rds. 3 yds. Ans.

## 12. Multiply 11 3 5 32 D 11 grs. by 2197.

2, 100. 0 J 1 J 1 O 1 B.D. .

## EXERCISE XLIX.

1. Divide 54 mi. 124 rds. 1 yd. 2 ft. 6 in. by 33.

2. Divide 5 cu. yds. 1 cu. ft. 84 cu. in. by 1716 cu. in.

3. Divide 8426 wks. 6 dys. 21 hrs. 10 min. 21 sec. by 1029.

wks. dys. hrs. min. sec.

1029) 
$$8426$$
 6 21 10 21 (8

 $8232$ 
 $194$ 
 $\times 7$  (+6)

1029)  $1364$  (1
 $1029$ 
 $335$ 
 $\times 24$ 
 $8040$ 
 $21$ 
 $1029) 8061$  (7
 $7203$ 
 $858$ 
 $\times 60$ 
 $1029) 51490$  (50
 $5145$ 
 $40$ 
 $60$ 
 $2400$ 
 $21$ 
 $1029) 2421$  ( $2363$ 
 $2058$ 
 $363$ 

8 wks. 1 dy. 7 hrs. 50 min. 2\frac{121}{44} sec.

Ans.

**4.** Divide £394 2 s.  $10\frac{1}{2}$  d. by £5 2 s.  $4\frac{1}{2}$  d.

£394 2 s.  $10\frac{1}{2} d$ . = 378,378 far. £5 2 s.  $4\frac{1}{2} d$ . = 4914 far.

77. Ans. 4914)378378

5. Divide 22 wks. 2 dys. by 11 hrs. 31 min. 12 sec.

22 wks. 2 dys. = 13,478,400 sec. 11 hrs. 31 min. 12 sec. = 41,472 sec.

325. Ans.

41472)13478400

6. Divide 74,128 sq. mi. 517 A. 80 sq. rds. by 10,000.

7 sq. mi. 264 A. 39 sq. rds. Ans.

7. Divide 38° 37′ 42″ by 5° 31′ 6″.

38° 37′ 42′′ = 139,062′′. 5° 31′ 6′′ = 19,866′′. 19866) 139062 (7. Ans. 139062

## EXERCISE L.

1. Find the value of  $\frac{4}{3}$  of a mile.

† mi. = † of 320 rds. = 256 rds.

Ans.

2. Find the value of  $\frac{8}{16}$  of an acre.

$$\frac{3}{16}$$
 A. =  $\frac{3}{16}$  of 160 sq. rds.  
= 30 sq. rds. Ans.

3. Find the value of § of a hundredweight.

$$\frac{5}{8}$$
 cwt. =  $\frac{5}{8}$  of 100 lbs. =  $62\frac{1}{2}$  lbs.  $\frac{1}{2}$  lb. =  $\frac{1}{2}$  of 16 oz. = 8 oz. 62 lbs. 8 oz. Ans.

4. Find the value of  $\frac{3}{3}$  of a pound sterling.

£ 
$$\frac{2}{3} = \frac{2}{3}$$
 of 20 s. =  $13\frac{1}{3}$  s.  $\frac{1}{3}$  s. =  $\frac{1}{3}$  of 12 d. = 4 d. 13 s. 4 d. Ans.

5. Find the value of 9 of a mile.

$$\frac{9}{11}$$
 mi. =  $\frac{9}{11}$  of 320 rds. =  $261\frac{9}{11}$  rds.  
 $\frac{9}{11}$  rds. =  $\frac{9}{11}$  of  $5\frac{1}{2}$  yds. =  $4\frac{1}{2}$  yds.  
 $\frac{1}{2}$  yd. =  $\frac{1}{2}$  of 3 ft. =  $1\frac{1}{2}$  ft.  
 $\frac{1}{2}$  ft. =  $\frac{1}{2}$  of 12 in. = 6 in.  
261 rds. 4 yds. 1 ft. 6 in. Ans.

6. Find the value of  $\frac{7}{11}$  of an acre.

$$\frac{7}{11}$$
 A. =  $\frac{7}{11}$  of 160 sq. rds. =  $101_{11}^{9}$  sq. rds.  
 $\frac{9}{11}$  sq. rds. =  $\frac{9}{11}$  of  $30\frac{1}{4}$  sq. yds. =  $24\frac{3}{4}$  sq. yds.  
 $\frac{3}{4}$  sq. yds. =  $\frac{3}{4}$  of 9 sq. ft. =  $6\frac{3}{4}$  sq. ft.  
 $\frac{3}{4}$  sq. ft. =  $\frac{3}{4}$  of 144 sq. in. =  $108$  sq. in.  
101 sq. rds. 24 sq. yds. 6 sq. ft. 108 sq. in. Ans.

7. Find the value of # of a degree.

$$\frac{4}{9}$$
° =  $\frac{4}{9}$  of  $60'$  =  $26\frac{2}{3}'$ .  
 $\frac{2}{3}'$  =  $\frac{2}{3}$  of  $60''$  =  $40''$ .  
 $26'$   $40''$ . Ans.

8. Find the value of  $\frac{1}{8}$  of a year.

$$\frac{1}{3}$$
 yr. =  $\frac{1}{3}$  of 365 dys. =  $121\frac{2}{3}$  dys.  $\frac{2}{3}$  dy. =  $\frac{2}{3}$  of 24 hrs. = 16 hrs. 121 dys. 16 hrs. Ans.

9. Find the value of 0.15625 of a bushel.

10. Find the value of 0.625 of a gallon.

0.625 gal.  $\frac{\times 4}{2.5 \text{ qts.}}$   $\frac{\times 2}{1 \text{ pt.}}$ 

2 qts. 1 pt. Ans.

11. Find the value of 0.875 of a leap-year.

12. Find the value of 0.325 of a pound troy.

## EXERCISE LI.

1. Find the value of  $6\frac{2}{3}$  of 3 A.  $101\frac{1}{3}$  sq. rds.

2. Find the value of 14 of 7 hrs. 21 min. 27 sec.

hrs. 7	min. 21	100. 27
		$\times 3$
7) 22	4	21
3	9	114
7	21	27
10	30	384

3. Find the value of 10.0175 of 1 dy. 13 hrs.

10.0175  

$$\times 37$$
 hrs.  
370.6475  
 $\times 60$   
38.85 min.  
 $\times 60$   
51 sec.

370 hrs. 38 min. 51 sec. = 15 dys. 10 hrs. 38 min. 51 sec. Ans. 4. Find the value of  $17\frac{7}{12}$  of 10 yds. 2 ft.  $3\frac{1}{5}$  in.

34 rds. 2 yds. 0 ft. 44 in. Ans.

5. Find the value of 0.01284 of 14 mi.

0.01284  

$$\times 14$$
 mi.  
0.17976 mi.  
 $\times 320$   
 $57.5232$  rds.  
 $\times 5\frac{1}{2}$   
 $2.8776$  yds.  
 $\times 3$   
 $2.6328$  ft.  
 $\times 12$   
 $7.5936$  in.

57 rds. 2 yds. 2 ft. 7.5936 in. Ans.

6. Find the value of 0.42776 of 12 t. 10 cwt.

10 cwt. = 
$$\frac{1}{2}$$
 t.  
0.42776  
 $\times 12\frac{1}{2}$  t.  
5.347 t.  
 $\times 20$   
6.94 cwt.  
 $\times 100$   
94 lbs.

5 t. 6 cwt. 94 lbs. Ans.

7. Find the value of  $\frac{2}{3}$  of 1 lb.  $+3\frac{2}{3}$  oz.  $+5\frac{2}{3}$  dwt.

$$\frac{2}{3}$$
 lb.  $=\frac{2}{5}$  of 12 oz.  $=\frac{44}{5}$  oz.  $\frac{44}{5}$  oz.  $+\frac{32}{6}$  oz.  $=\frac{84}{15}$  oz.  $=\frac{1}{45}$  of 20 dwt.  $=\frac{4}{5}$  dwt.  $=\frac{4}{5}$  dwt.  $=\frac{4}{5}$  dwt.  $=\frac{1}{5}$  dwt.  $=\frac{1}{5}$  of 24 grs.  $=\frac{23}{5}$  grs. 8 oz. 6 dwt. 23 grs. Ans.

8. Find the value of 0.35 of 4 lbs. 5 oz. 6 dwt. 16 grs.

$$0.35 = \frac{85}{100} = \frac{7}{20}$$
.

1be. oz. dwt. grs.

4 5 6 16

 $\frac{\times 7}{20}$ 

20)  $\frac{31}{1}$   $\frac{1}{6}$   $\frac{6}{13}$   $\frac{16}{8}$  Ans.

9. Find the value of 3.726 mi. -33.57 rds.

$$3.726$$
 mi.  
 $\times 320$   
 $\overline{1192.32}$  rds.  
 $33.57$   
 $\overline{1158.75}$  rds.

- $= 3 \text{ mi. } 198 \text{ rds. } 4 \text{ yds. } 4\frac{1}{2} \text{ in. } Ans.$
- 10. Find the value of  $\frac{3}{78}$  of a year +  $\frac{9}{56}$  of a week +  $\frac{7}{12}$  of an hour.

$$\frac{8}{78}$$
 yr.  $= \frac{8}{78}$  of 365 dys.  $= 15$  dys.  $\frac{9}{56}$  wk.  $= \frac{9}{56}$  of 7 dys.  $= \frac{11}{8}$  dys.  $\frac{1}{8}$  dy.  $= \frac{1}{8}$  of 24 hrs.  $= 3$  hrs.  $\frac{7}{12}$  hr.  $= \frac{7}{12}$  of 60 min.  $= 35$  min.

= 2 wks. 2 dys. 3 hrs. 35 min. Ans.

11. Find the value of 5.268 of 2 dys. + 2.829 of 16 hrs. + 0.9528 of 25 min.

5.268	2.829	0.9528
$\times 2$ dys.	$\times$ 16 hrs.	$\times$ 25 min.
10.536 dys.	45.264 hrs.	23.82 min.
× 24	12.864 hrs.	7.68 min.
12.864 hrs.	58.128 hrs.	31.5 min.
	$\times$ 60	$\times$ 60
	7.68 min.	30 sec.

10 dys. 58 hrs. 31 min. 30 sec. = 12 dys. 10 hrs. 31 min. 30 sec. Ans.

12. Find the value of  $\frac{3}{16}$  of a mile  $+\frac{2}{3}$  of 40 rds.  $+\frac{2}{3}$  of a yd.

$$\frac{3}{16}$$
 mi. =  $\frac{3}{16}$  of 320 rds. = 60 rds.

  $\frac{3}{6}$  of 40 rds.
 =  $26\frac{3}{8}$  rds.

  $\frac{3}{6}$  rds. +  $26\frac{3}{8}$  rds.
 =  $86\frac{3}{8}$  rds.

  $\frac{3}{8}$  rds. =  $\frac{3}{8}$  of  $5\frac{1}{2}$  yds. =  $3\frac{3}{8}$  yds.
 =  $3\frac{3}{8}$  yds.

  $\frac{3}{8}$  yd. +  $\frac{3}{8}$  yd. =  $1\frac{1}{24}$  yds.
 =  $1\frac{1}{24}$  yds.

  $\frac{1}{24}$  yds. + 3 yds. =  $1\frac{1}{2}$  in.
 =  $1\frac{1}{2}$  in.

 86 rds. 4 yds.  $1\frac{1}{2}$  in. Ans.

13. Find the value of  $\frac{3}{4}$  of 2 cwt. 84 lbs.  $+\frac{3}{7}$  of 5 cwt. 98 lbs.  $+\frac{3}{7}$  of  $7\frac{1}{2}$  lbs.

2 cwt. 84 lbs. 5 cwt. 98 lbs. 
$$\times \frac{100}{4)284}$$
 lbs.  $\times \frac{100}{598}$  lbs.  $\times \frac{3}{100}$   $\times \frac{3}{100}$  lbs.  $\times \frac{3}{100}$   $\times \frac{100}{2564}$  lbs.  $\times \frac{3}{100}$  lbs.  $\times \frac{3}{100}$  cwt. 13 lbs.  $\times \frac{3}{100}$  cwt. 56 lbs. 4 oz. 94 drs.  $\times \frac{3}{100}$  of 74 lbs.  $\times \frac{3}{100}$  lbs.  $\times \frac{3}{100}$  lbs.  $\times \frac{3}{100}$  cwt. 56 lbs. 4 oz. 94 drs.

 $\frac{2}{5}$  of  $7\frac{1}{2}$  lbs. = 3 lbs. 13 lbs.

2 cwt. 13 lbs. 2 cwt. 56 lbs. 4 oz. 94 drs.

3 lbs.

4 cwt. 72 lbs. 4 oz. 94 drs. Ans.

## EXERCISE LII.

1. Express a pound avoirdupois as the fraction of a pound troy.

1 lb. avoird. = 7000 troy grs.  
1 lb. troy = 5760 troy grs.  

$$\frac{7000}{5760} = \frac{175}{144}$$
. Ans.

2. Express an ounce avoirdupois as the fraction of an ounce troy.

$$\frac{437\frac{1}{2} \text{ grs.}}{16)7000} \qquad 1 \text{ oz. troy} = 480 \text{ grs.}$$

$$\frac{437\frac{1}{2}}{480} = \frac{875}{960} = \frac{175}{192}. \text{ Ans.}$$

3. Express 363 sq. yds. as the fraction of an acre.

$$\begin{array}{r}
1 \text{ A.} \\
\times 160 \\
\hline
160 \text{ sq. rds.} \\
\times 30\frac{1}{4840} = \frac{3}{40}. \text{ Ans.}
\end{array}$$

$$\frac{363}{4840} = \frac{3}{40}. \text{ Ans.}$$

4. Express  $\frac{2}{3}$  of £21s.  $3d. + \frac{5}{11}$  of £14s. 9d. as the fraction of £214s.

5. Express 2 mi. 138 rds. 1 yd. as the fraction of 3 mi. 265 rds. 3 yds. 1 ft. 6 in.

6. Express \$\frac{2}{3}\$ of 560 lbs. as the fraction of 5 long tons.

$$\frac{3}{7}$$
 of 560 lbs. = 160 lbs.  $\frac{2240 \text{ lbs.}}{\times 5}$   $\frac{160}{11200} = \frac{1}{70}$ . Ans.  $\frac{11200 \text{ lbs.}}{\times 5}$ 

7. Express 3 of 200 rds. as the fraction of 4 miles.

$$\frac{2}{3}$$
 of 200 rds. =  $133\frac{1}{3}$  rds.

$$\frac{320 \text{ rds.}}{\times 4} \qquad \frac{133\frac{1}{3}}{1280} = \frac{1}{1280} \times \frac{5}{3} = \frac{5}{48}. \text{ Ans.}$$
1280 rds.

8. Express ½9 of 2 dys. 2 hrs. 24 min. as the fraction of 2 wks. 1 d.

$$\frac{1120}{21600} = \frac{7}{135}.$$
 Ans.

9. Express 4 of the difference between 3 yds. 2 ft. 11 in. and 10 yds. 7 in. as the fraction of 8 yds.

$$\frac{179\frac{1}{5}}{288} = \frac{1}{288} \times \frac{28}{5} = \frac{28}{45}. Ans.$$

10. Express  $\frac{19}{25}$  of the difference between  $\frac{9}{8}$  of 7 hrs. and  $\frac{7}{25}$  of 15 min. as the fraction of 12 hrs. 18 min.

7 hrs. = 420 min.

$$\frac{5}{8} \times \frac{105}{1} = \frac{525}{2}$$
 $\frac{7}{28} \times \frac{15}{1} = \frac{21}{5}$ 
 $\frac{12}{5} \times \frac{15}{2} = \frac{21}{5}$ 
 $\frac{123}{21} \times \frac{123}{19} = 123 \text{ min.}$ 
 $\frac{12 \text{ hrs. 18 min.}}{738 \text{ min.}}$ 

$$\frac{60}{738 \text{ min.}}$$

$$\frac{525}{2} \times \frac{21}{5} = \frac{2583}{10}$$

$$\frac{123}{738} = \frac{1}{6}$$
Ans.

11. Express 3 pt. as the fraction of a gallon.

1 gal. = 8 pts. 
$$\frac{2}{8} = \frac{1}{8} \times \frac{2}{5} = \frac{1}{20}$$
. Ans.

12. What part of 4 lbs. 1 os. 8 dwt. 15 grs. is 1 lb. 1 os. 9 dwt. 15 grs.

4 lbs. 1 os. 8 dwt. 15 grs.:

15 grs. = 
$$\frac{15}{14}$$
 dwt. =  $\frac{1}{4}$  dwt.

15 grs. =  $\frac{15}{14}$  dwt. =  $\frac{1}{4}$  dwt.

15 grs. =  $\frac{15}{14}$  dwt. =  $\frac{5}{4}$  dwt.

16 grs. =  $\frac{15}{14}$  dwt. =  $\frac{5}{4}$  dwt.

17 grs. =  $\frac{15}{14}$  dwt. =  $\frac{15}{14}$  dwt.

17 grs. =  $\frac{15}{14}$  dwt.

17 grs. =  $\frac{15}{14}$  dwt. =  $\frac{15}{14}$  dwt.

17 grs. =  $\frac{15}{14}$  dwt. =  $\frac{15}{14}$  dwt.

17 grs. =  $\frac{15}{14}$  dwt. =  $\frac{15}{14}$  dwt.

$$\frac{\frac{1}{4}\frac{79}{440}}{\frac{1}{4}\frac{79}{10}} - \frac{\frac{3}{1929}}{\frac{7929}{11}} \times \frac{719}{949} = \frac{3}{11}. Ans.$$

What part of 2 mi, is ‡ of 6 rds, 3 yds, 2 in.?

$$\frac{1}{2} = \frac{1}{2} \text{ of } \frac{59}{4320} = \frac{59}{8640}$$
. Ans.

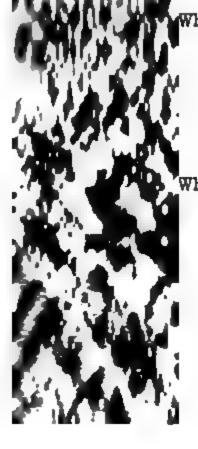
What part of a quahel is 1 pk. 2 qts. 1 pt.?

1 pk. 2 qts. 1 pt.:  
1 pt. = 
$$\frac{1}{4}$$
 qt.  
2 $\frac{1}{2}$  qts. =  $\frac{2\frac{1}{4}}{8}$  pks. =  $\frac{5}{16}$  rks.  
1 $\frac{5}{16}$  pks. =  $\frac{1\frac{5}{16}}{4}$  bu. =  $\frac{21}{4}$  bu. Ass.

What part of 20 A. are 19 A. 3.5 sq. ch.

3.5 sq. ch. 
$$=\frac{3.5}{10}$$
 A.  $=\frac{7}{20}$  A.

$$\frac{19\frac{7}{12}}{20} - \frac{387}{20} \times \frac{1}{20} = \frac{387}{400}. Ans.$$



16. What part of 5 tons are 3 t. 240 lbs.?

240 lbs. = 
$$\frac{240}{2000}$$
 t. =  $\frac{8}{25}$  t.  $3\frac{8}{25}$ . t.

$$\frac{3\frac{3}{25}}{5} = \frac{1}{5} \times \frac{78}{25} = \frac{78}{125}$$
. Ans.

17. 38 sq. rds. 194 sq. ft. 108 sq. in = what part of an acre?

38 sq. rds. 194 sq. ft. 108 sq. in.:

108 sq. in. = 
$$\frac{108}{144}$$
 sq. ft. =  $\frac{3}{4}$  sq. ft.  
194 $\frac{3}{4}$  sq. ft. =  $\frac{194\frac{3}{4}}{272\frac{1}{4}}$  sq. rds. =  $\frac{779}{1089}$  sq. rds.  
38 $\frac{779}{1089}$  sq. rds. =  $\frac{38\frac{779}{1089}}{160}$  A. =  $\frac{42161}{174240}$  A. Ans.

### EXERCISE LIII.

1. Express 16 s. 3\frac{3}{4} d. as the decimal of a pound.

2. Express 233 rds. 9 ft. 10.8 in. as the decimal of a mile.

3. Express 71 sq. rds. 54 sq. ft. 64.8 sq. in. as the decimal of an acre.

4. Express 15 hrs. 14 min. 6 sec. as the decimal of 2 days.

$$\frac{0.6348}{2} = 0.3174$$
. Ans.

5. Express 38 sq. rds. 21 sq. yds. 5 sq. ft. 108 sq. in. as the decimal of an acre.

6. Express 3 mi. 242 rds. 2 yds. 2 ft. 3 in. as the decimal of 7 mi. 160 rds.

12 3.00 in. 320 160  
3 2.25 ft. 7.5 mi.  

$$\frac{5\frac{1}{2}}{320}$$
 2.75 yds.  
 $\frac{242.5 \text{ rds.}}{3.7578 \text{ mi.}}$   
 $\frac{3.7578}{7.5} = 0.501$ . Ans.

7. Express 5 hrs. 13 min. 30 sec. as the decimal of a week.

8. Express 27° 14' 45" as the decimal of 90°.

$$\begin{array}{r}
60 \mid 45.00 \text{/} \\
60 \mid 14.75 \text{/} \\
27.246^{\circ}
\end{array}$$

$$\frac{27.246}{90} = 0.303. \text{ Ans.}$$

9. Express 54 dys. 2 hrs. 40 min. as the decimal of 3651 dys.

$$\begin{array}{c|c}
60 & 40.0 \text{ min.} \\
24 & 2.6 \text{ hrs.} \\
\hline
54.1 \text{ dys.} \\
\hline
\frac{54.1}{3651} = 0.148. \text{ Ans.}
\end{array}$$

10. Express 2 lbs. avoirdupois as the decimal of 10 lbs troy.

2 lbs. av. = 14,000 grs. troy.  
10 lbs. troy = 57,600 grs. troy.  

$$\frac{14000}{57600} = 0.243. Ans.$$

11. Express 44,920.9025 hrs. as the decimal of a year.

$$1 \text{ yr.} = 8760 \text{ hrs.}$$

$$\frac{44920.9025}{8760} = 5.128. \text{ Ans.}$$

12. Express 1 drm. avoirdupois as the decimal of 1 dwt. troy.

1 drm. avoird. = 
$$\frac{1}{286}$$
 of 7000 trey gre.  
= 27.344 troy gre.  
1 dwt. = 24 troy gre.  
 $\frac{27.344}{24}$  = 1.139. Ans.

13. Express 10 milligrams as the decimal of a grain, if a kilogram equals 2 lbs. 8 oz. 3 dwt. 1 gr.

2 lbs. 8 oz. 3 dwt. 1 gr. = 15,438 grs.  
1 kg. = 
$$100,000 \times 10$$
 mg.  
 $\frac{15433}{100000} = 0.15433$ . Ans.

14. Express 14.52 sq. yds. as the decimal of a square chain.

1 sq. ch. = 16 sq. rds.  
= 
$$484$$
 sq. yds.  
 $\frac{14.52}{484}$  = 0.03. Ans.

15. Express 8 cwt. 77 lbs. 9.6 oz. as the decimal of a ton.

#### Exercise LIV.

1. Find the difference in longitude between two places, if the difference in time be 1 hr. 15 min.

1 hr. 15 min. = 75 min. = 
$$\frac{1}{4}$$
 (75°) = 18° 45′. Ans.

2. Find the difference in longitude between two places, if the difference in time be 2 hrs. 11 min.

2 hrs. 11 min. = 131 min. = 
$$\frac{1}{4}$$
 (131°) = 32° 45′. Ans.

3. Find the difference in longitude between two places, if the difference in time be 5 hrs. 10 min. 10 sec.

5 hrs. 10 min. 10 sec. = 310 min. 10 sec. = 
$$\frac{1}{4}$$
 (310° 10′)  
= 77° 32′ 30′′. Ans.

4. Find the difference in longitude between two places, if the difference in time be 3 hrs. 25 min. 35 sec.

3 hrs. 25 min. 35 sec = 205 min. 35 sec. = 
$$\frac{1}{4}$$
 (205° 35′)  
= 51° 23′ 45′′. Ans.

5. Find the difference in longitude between two places, if the difference in time be 6 hrs. 12 min. 30 sec.

6 hrs. 12 min. 30 sec. = 
$$372$$
 min. 30 sec. =  $\frac{1}{4}$  (372° 30′)  
= 93° 7′ 30′′. Ans.

6. Find the difference in longitude between two places, if the difference in time be 4 hrs. 8 min. 12 sec.

4 hrs. 8 min. 12 sec. = 248 min. 12 sec. = 
$$\frac{1}{4}(248^{\circ} 12') = 62^{\circ} 3'$$
. Ans.

7. Find the difference in longitude between two places, if the difference in time be 18 hrs. 10 min.

18 hrs. 10 min. = 1090 min. = 
$$\frac{1}{4}(1090^{\circ}) = 272^{\circ} 30'$$
. Ans.

8. Find the difference in longitude between two places, if the difference in time be 15 hrs. 15 min. 15 sec.

15 hrs. 15 min. 15 sec. = 915 min. 15 sec. = 
$$\frac{1}{4}$$
 (915° 15') = 228° 48' 45''. Ans.

Find the difference in time between two places, if the difference in longitude be 9° 20'.

$$9^{\circ} \ 20' = 4 \times (9 \text{ min. } 20 \text{ sec.}) = 37 \text{ min. } 20 \text{ sec. } Ans.$$

10. Find the difference in time between two places, if the difference in longitude be 70° 30'.

70° 30′ 
$$-4 \times (70 \text{ min. } 30 \text{ sec.}) = 4 \text{ hrs. } 42 \text{ min. } Ans.$$

11. Find the difference in time between two places, if the difference in longitude be 56° 38′ 12″.

$$56^{\circ}$$
 36'  $12'' = 56^{\circ}$  36.2' = 4 × (56 min. 36.2 sec.)  
= 3 hrs. 46 min. 24.8 sec. Ans.

12. Find the difference in time between two places, if the difference in longitude be 106° 32′ 36″.

13. Find the difference in time between two places, if the difference in longitude be 120° 14′ 30″.

120° 14′ 30″ = 120° 14.5′ = 
$$4 \times (120 \text{ min. } 14.5 \text{ sec.})$$
  
=  $8 \text{ hrs. } 58 \text{ sec. } Ans.$ 

and the difference in time between two places, if the differongitude be 100° 45′ 54′′.

00° 45′ 54′′ = 100° 45.9′ = 
$$4 \times (100 \text{ min. } 45.9 \text{ sec.})$$
  
= 6 hrs. 46 min. 3.6 sec. Ans.

md the difference in time between two places, if the differongitude be 2° 2′ 2′′.

$$V' = 2^{\circ} 2_{10}^{1} = 4 \times (2 \text{ min. } 2_{10}^{1} \text{ sec.}) = 8 \text{ min. } 8_{15}^{4} \text{ sec. } Ans.$$

and the difference in time between two places, if the differengitude be 75° 10'.

$$75^{\circ} \ 10' = 4 \times (75 \ \text{min.} \ 10 \ \text{sec.}) = 5 \ \text{hrs.} \ 40 \ \text{sec.} \ Ans.$$

#### EXERCISE LV.

The longitude of some public building in:

- (1) Berlin is 13° 23′ 43″ E. (2) Rome, 12° 27′ 14″ E.
- (3) Constantinople, 28° 59' E.
- (4) Pekin, 116° 23′ 45″ E.
- (5) San Francisco, 122° 26′ 15′′W.
- (6) St. Louis, 90° 15′ 15′′ W.
- (7) Jerusalem, 35° 32′ E.
- (8) Bombay, 72° 54′ E.
- (9) Calcutta, 88° 19′ 2″ E.
- (10) Chicago, 87° 35' W.
- (11) New York, 74° 0′ 3″ W.
- (12) Montreal, 73° 25' W.
- 1. When it is noon at Greenwich, what is the clock-time at each of the above places?

(1)  

$$13^{\circ} \ 23' \ 43''$$
  
=  $13^{\circ} \ 23\frac{13}{60}'$   
=  $4 \times (13 \text{ min. } 23\frac{13}{60} \text{ sec.})$   
=  $53 \text{ min. } 3\frac{113}{15} \text{ sec. P.M.}$   
=  $12 \text{ hrs. } 53 \text{ min. } 34\frac{13}{15} \text{ sec. P.M.}$   
Ans.

**(2**)

12° 27′ 14′′ = 12° 27 $\frac{7}{30}$ ′ = 4 × (12 min. 27 $\frac{7}{30}$  sec.) = 49 min. 48 $\frac{1}{3}$  sec. P.M. = 12 hrs. 49 min. 48 $\frac{1}{3}$  sec. P.M. Ans.

(3)

28° 59′

 $= 4 \times (28 \text{ min. } 59 \text{ sec.})$ 

- 1 hr. 55 min. 56 sec. P.M. Ans.

(4)

116° 23′ 45′′ - 116° 23‡′

 $= 4 \times (116 \text{ min. } 23\frac{3}{4} \text{ sec.})$ 

- 7 hrs. 45 min. 35 sec. P.M. Ans.

(5) 122° 26′ 15″ = 122° 26½′ = 4 × (122 min. 26½ sec.) = 8 hrs. 9 min. 45 sec.

12 hrs. 8 hrs. 9 min. 45 sec.

3 hrs. 50 min. 15 sec. A.M. Ans.

(6) 90° 15′ 15′′ = 90° 15¼′

 $= 4 \times (90 \text{ min. } 15\frac{1}{4} \text{ sec.})$ = 6 hrs. 1 min. 1 sec.

12 hrs. M.

6 hrs. 1 min. 1 sec.

5 hrs. 58 min. 59 sec. A.M. Ans.

(7)

35° 32′

 $= 4 \times (35 \text{ min. } 32 \text{ sec.})$ 

= 2 hrs. 22 min. 8 sec. P.M. Ans.

(8)

72° 54′

 $= 4 \times (72 \text{ min. } 54 \text{ sec.})$ 

= 4 hrs. 51 min, 36 sec. P.M. Ans.

(9) (11)74° 0/ 3// 88° 19' 2" - 74° 10 = 88° 1937  $= 4 \times (74 \text{ min.} \frac{1}{2} \text{ sec.})$ = 4 brs. 56 min.  $\frac{1}{2} \text{ sec.}$  $= 4 \times (88 \text{ min. } 19\frac{1}{10} \text{ sec.})$ - 5 hrs. 53 min. 187 sec. Ans. 12 hrs. M. 4 hrs. 56 min. 1 sec. 7 hrs. 3 min. 594 sec. A.M. Ans. (10)879 35/  $-4 \times (87 \text{ min. } 35 \text{ sec.})$  $-4 \times (73 \text{ min. } 25 \text{ sec.})$ = 5 hrs. 50 min. 20 sec. = 4 brs. 53 min. 40 sec. 12 hrs M. 12 hrs. M. 5 hm. 50 min. 20 sec. 4 hrs. 53 min. 40 eec. 6 hrs. 9 min. 40 sec. A.M. Ans. 7 hrs. 6 min. 20 sec. A.M. Ans. 2. When it is half-past four P.M. at Chicago, what is the clocktime at each of the above places?

(1) 87° 35′ W. 87° 35′ W. 28° 59′ E. 13° 23/ 43// E. 116° 34' 100° 58/ 43//  $= 4 \times (116 \text{ min. } 34 \text{ eec.})$ = 100° 5844/ - 7 hrs. 46 min. 16 sec.  $=4\times(100 \text{ mm. } 5844 \text{ sec.}$ 4 hrs. 30 min. P.M. = 6 hrs. 43 min. 5413 sec. 12 hrs. 16 mm. 16 sec. A.M. Ans. 4 hrs. 30 min. P M. 11 hrs. 13 min, 5412 sec. P.M. (4) Ana. 87° 35/ W. 116° 23′ 45″ E. 203° 58/ 45// (%) 360° 35/ W. 203° 58/ 45" 27/ 14// E. 156° 1/ 15" 2/ 14//  $= 156^{\circ} 11/$  $= 4 \times (156 \text{ min. } 1\frac{1}{2} \text{ sec.})$ in. 2<del>7</del> sec.) iin. 8<del>14</del> sec. - 10 hrs. 24 min. 5 sec. 4 hrs. 30 min. P M. IID. P.K. 10 hre. 24 min 5 sec. iin. 814 sec. P.M. 6 hrs. 5 min. 55 sec. A.M. Ana Ans.

**(5)** 122° 26¼′ W. 87° 35′ W. 34° 511/  $= 4 \times (34 \text{ min. } 51\frac{1}{4} \text{ sec.})$ = 2 hrs. 19 min. 25 sec. 4 hrs. 30 min. P.M. 2 hrs. 19 min. 25 sec. 2 hrs. 10 min. 35 sec. P.M. Ans. (6)90° 151′ W. 87° 35<sup>7</sup> W. 2° 401/  $=4\times(2 \text{ min. } 401 \text{ sec.})$ = 10 min. 41 sec.4 hrs. 30 min. P.W. 10 min. 41 sec. 4 hrs. 19 min. 19 sec. P.M. Ans. **(7)** 87° 35′ W. 35° 32′ E. 123° 7′  $= 4 \times (123 \text{ min. } 7 \text{ sec.})$ = 8 hrs. 12 min. 28 sec. 4 hrs. 30 min. P.M. 12 hrs. 42 min. 28 sec. A.M. Ans: **(8)** 72° 54′ E. 87° 35′ W. 160° 29′ = 4  $\times$  (160 min. 29 sec.) = 10 hrs. 41 min. 56 sec.4 hrs. 30 min. P.M. 15 hrs. 11 min. 56 sec. = 3 hrs. 11 min. 56 sec. A.M. Ans.

213 **(9)** 88° 19′ 2/′ E. 87° 35′ 175° 54' 2"  $=175^{\circ}54\frac{1}{30}$  $4 \times (175 \text{ min. } 54\frac{1}{30} \text{ sec.})$  $= 11 \text{ hrs. } 43 \text{ min. } 36_{15}^{2} \text{ sec.}$ 4 hrs. 30 min. P.M. 16 hrs. 13 min.  $36_{15}$  sec.  $= 4 \text{ hrs. } 13 \text{ min. } 36\frac{2}{15} \text{ sec. A.m.}$ Ans. (10)(4 hrs. 30 min. p.m.). Ans. (11)87° 35′ W. 74° 0′ 3′′ 13° 34′ 57′′  $=13^{\circ} 34\frac{19}{26}'$  $= 4 \times (13 \text{ min. } 34\frac{13}{16} \text{ sec.})$  $= 54 \text{ min. } 19\frac{4}{5} \text{ sec.}$ 4 hrs. 30 min. P.M. 5 hrs. 24 min. 194 sec. P.M. Ans. (12)87° 35′ W.

87° 35′ W.

73° 25′ W.

14° 10′

= 4 × (14 min. 10 sec.)

= 56 min. 40 sec.

4 hrs. 30 min. p.m.

5 hrs. 26 min. 40 sec. p.m. Ans.

3. When it is eight o'clock A.M. at Constantinople, what is the clock-time at each of the above places?

 $=15^{\circ} 35\frac{1}{66}$ 

 $=4 \times (15 \text{ min. } 35\frac{17}{66} \text{ sec.})$ 

 $= 1 \text{ hr. } 2 \text{ min. } 21\frac{2}{15} \text{ sec.}$ 

8 hrs. A.M.

1 hr. 2 min. 21-2 sec.

6 hrs. 57 min. 3813 sec. A.M. Ans.

 $=16^{\circ} 31\frac{28}{30}$ 

 $= 4 \times (16 \text{ min. } 31\frac{28}{30} \text{ sec.})$ 

= 1 hr. 6 min.  $7\frac{1}{15}$  sec.

8 hrs. A.M.

ş

1 hr. 6 min. 7<sup>1</sup>/<sub>15</sub> sec.

6 hrs. 53 min. 5214 sec. A.M. Ans.

(3) (8 hrs. A.M.). Ans.

> (4) 116° 23½′ E. 28° 59′ E. 87° 24½′

 $=4 \times (87 \text{ min. } 24\frac{3}{4} \text{ sec.})$ 

= 5 hrs. 49 min. 39 sec.

8 hrs. A.M.

1 hr. 49 min. 39 sec. P.M. Ans.

 $-4 \times (151 \text{ min. } 25\frac{1}{4} \text{ sec.})$ 

= 10 hrs. 5 min. 41 sec.

8 hrs. A.M.

10 hrs. 5 min. 41 sec.

9 hrs. 54 min. 19 sec. P.M.

Ans

= 119° 141/

 $= 4 \times (119 \text{ min. } 14\frac{1}{4} \text{ sec.})$ 

= 7 hrs. 56 min. 57 sec.

8 hrs. A.M.

7 hrs. 56 min. 57 sec.

3 min. 3 sec. A.M.

= 12 hrs. 3 min. 3 sec. A.M. Ans.

 $=4\times(6 \text{ min. } 33 \text{ sec.})$ 

= 26 min. 12 sec.

8 hrs. A.M.

8 hrs. 26 min. 12 sec. A.M.

Ans

```
(10)
                 (8)
                                                            87° 35′ W.
             72° 54′ E.
                                                            28° 59′ E.
             28° 59′ E.
                                                          116° 34′
             43° 55′
                                                  = 4 \times (116 \text{ min. } 34 \text{ sec.})
 = 4 \times (43 min. 55 sec.)
                                                  - 7 hrs. 46 min. 16 sec.
 = 2 hrs. 55 min. 40 sec.
                                                     8 hrs. A.M.
     8 hrs. A.M.
                                                     7 hrs. 46 min. 16 sec.
    10 hrs. 55 min. 40 sec. A.M.
                                                              13 min. 44 sec. A.M.
                                   Ans.
                                                = 12 hrs. 13 min. 44 sec. A.M.
                                                                                   Ans.
                 (9)
                                                                 (11)
                                                           74° 0′ 3′′ W.
          88° 19′ 2′′ E.
                                                           28° 59′ E.
          28° 59′ E.
                                                         102° 59′ 3″
          59° 20′ 2′′
                                                    =102^{\circ} 59\frac{1}{20}'
= 59^{\circ} 20\frac{1}{30}
                                                    = 4 \times (102 \text{ min. } 59\frac{1}{20} \text{ sec.})
= 4 \times (59 \text{ min. } 20\frac{1}{80} \text{ sec.})
                                                    = 6 \text{ hrs. } 51 \text{ min. } 56\frac{1}{3} \text{ sec.}
= 3 hrs. 57 min. 20\frac{2}{15} sec.
    8 hrs. A.M.
                                              8 hrs. A.M.
                                              6 hrs. 51 min. 561 sec.
  11 hrs. 57 min. 2013 sec. A.M.
                                                       8 min. 3\frac{1}{2} sec. A.M. Ans.
                                   Ans.
                                              1 hr.
                                         (12)
                                     73° 25′ W.
                                     28° 59′ E.
                                   102° 24'
                            = 4 \times (102 \text{ min. } 24 \text{ sec.})
                            = 6 hrs. 49 min. 36 sec.
                      8 hrs. A.M.
```

6 hrs. 49 min. 36 sec.

1 hr. 10 min. 24 sec. A.M. Ans.

#### EXERCISE LVI.

#### When it is noon at Greenwich the time at

- (1) Boston, Mass., is 7 hrs. 15 min. 46 sec. A.M.
- (2) Augusta, Me., 7 hrs. 20 min. 40 sec. A.M.
- (3) Columbia, S.C., 6 hrs. 35 min. 32 sec. A.M.
- (4) Little Rock, Ark., 5 hrs. 51 min. 12 sec. A.M.
- (5) Salt Lake, 4 hrs. 30 min. A.K.
- (6) Albany, N.Y., 7 hrs. 5 min. 1 sec. A.M.
- (7) Columbus, O., 6 hrs. 27 min. 48 sec. A.M.
- (8) Harrisburg, Penn., 6 hrs. 52 min. 40 sec. A.M.
- (9) New Orleans, La., 6 hrs. A.M.
- (10) Springfield, Ill., 6 hrs. 1 min. 48 sec. A.M.
- (11) Washington, D.C., 6 hrs. 51 min. 44 sec. A.M.

# 1. What is the longitude of each of the shove places?

What i	is the long	gitude of each	of the above pla	BC65 ?
	(1)			<b>(4)</b>
bra.	min.	<b>990.</b>	hrs.	min. sec.
12	0	0	12	0 0
7	5	46	5	51 12
4	44	14	6	8 48
	4 min. 14			nin. 48 sec.
	of 284° 14		$= \frac{1}{4} \text{ of } 3$	
<b>-71</b> °	o 8/80//	W. Ans.	= 92° 1	2/ W. Ans.
	(2)			(5)
hrs.	min.	<b>800.</b>	hrs.	min.
12	0	0	12	0
7	20	40	4	30
4	<b>39</b>	20	7	<b>30</b>
= 27	9 min. 20	sec.	<b>- 4</b> 50 n	nin.
	of 279° 20		$=\frac{1}{4}$ of 4	
<b>=</b> 69	° 50′ W.	Ans	<b>–</b> 112°	30' ₩. Ans.
	(3)			(6)
hrs.	min.	560.	hrs.	min. sec.
12	0	0	12	0 0
6	35	32	7	5 1
5	<b>24</b>	28	4	54 59
=32	4 min. 28	8ec.	= 294  n	oin. 59 sec.
	of 324° 28			94° 59′
<b>-</b> 81°	° 7′ W	Ans.	<b>–</b> 73° 4	4′ 45′′ W. J

73° 44′ 45′′ W. Ans.

	(7)				(9 <del>)</del>				
hrs.	min.	sec.		hrs.					
12	0	0 .		12					
6	27	48		6					
5	32	12	<del>-</del> 6						
= 332 min. 12 sec.				= 360 min.					
$=\frac{1}{4}$ of 332° 12′				$-1$ of $360^{\circ}$					
$= 83^{\circ} 3' \text{ W. } Ans.$				=90 ° W. Ans.					
	(8)				(10)				
hrs.	min.	<b>600.</b>	•	hre.	min.	aqo.			
12	O	0		12	0	0			
6	52	40		6	1	48			
5	7	20		5	58 .	12			
= 30	7 min. 20	sec.		<b>=</b> 35	8 min. 12	sec.			
= \frac{1}{2} \text{ of } 307° \text{ 20'}				$= \frac{1}{2}$ of 358° 12′					
= 76° 50′ W. Ans.				= 89° 33′ W. Ans.					
•			(11)						
		hrs.	min.	sec.					
		12	0	0					
		6	51	44					
		5	8	16					
		<del>- 30</del> 8	8 min. 16	80C.					

### EXERCISE LVII.

= 77° 4′ W. Ans.

 $=\frac{1}{4}$  of 308° 16′

1. Reduce 7 gals. 3 qts. 1 pt. to gallons and decimal of a gallon.

2. Reduce £4.375 to pounds, shillings, and pence.

£
$$A.375$$
 $20$ 
 $7.5 s.$ 
 $12$ 
 $6 d$ 
£4 7 s. 6 d. Ans.

Reduce 7.6875 gals. to gallons, quarts, and pints.

7 gale, 2 qts. 1.5 pts, Ana,

4. Reduce to pounds, shillings, and pence \$5.875; \$7.38; \$17.85; \$21.75; if \$4.85 be equal to a pound.

\* How many square yards in res?

6. If 2 qts. of linseed oil be mixed with \( \frac{1}{2} \) pt. spirits of turpentine, what fraction of the mixture is turpentine? How much turpentine in one pint of the mixture?

2 qts. = 4 pts.  
4 pts. + 
$$\frac{1}{4}$$
 pts. =  $\frac{4}{4}$  pts.  
 $\frac{1}{4\frac{1}{2}} - \frac{2}{9} \times \frac{1}{2} - \frac{1}{9}$  (1)  
 $\frac{1}{4}$  of 1 pt. =  $\frac{1}{4}$  pt. (2)

7. Reduce 5.1732 mi. to yards, feet, and inches.

9104 yds. 2 ft. 5.952 in. Ans.

8. If a man walk 88 mi. in 26 hrs., how many feet does he walk each second?

$$\frac{22}{5789} \times \frac{44}{1} \times \frac{1}{3699} \times \frac{1}{26} = \frac{968}{195} \text{ ft.}$$

$$15 \quad 13$$

$$= 4\frac{1}{1}\frac{8}{1}\frac{8}{1} \text{ ft. } Ans.$$

9. Of a mixture of sand and lime 0.27 of the weight is lime. How many ounces of lime in a pound of the mixture? How many troy grains of lime in an avoirdupois pound of the mixture?

10. A gill of water is put into a quart measure, and the measure filled with milk. What part of the mixture is water?

8 gi. = 1 qt.  

$$\therefore 1 \text{ gi.} = \frac{1}{3} \times 1 \text{ qt.} = \frac{1}{3} \text{ qt.}$$

$$\therefore \frac{1}{3} \text{ is water.}$$

11. Reduce 555 ft. to the decimal of a mile.

12. Reduce 1 mi. 13 rds. 2 yds. 2 ft. 6 in. to inches.

13. How many cubic inches in 2½ cubic feet?

14. How many pounds avoirdupois does a cubic yard of water weigh if a cubic foot weigh 1000 ounces?

15. Express the weight of a cubic yard of water as the decimal of a ton.

$$\frac{16875}{2666} = \frac{275}{266} = \frac{27}{27}.$$

$$0.84375 \text{ t. } Ans.$$

$$32)27.00000$$

16. What is the weight of 7 bu. 3½ pks. of potatoes?

$$3\frac{1}{4}$$
 pks.  $=\frac{3\frac{1}{4}}{4}$  bu.  $=\frac{7}{8}$  bu. 60 lbs.  $\frac{\times 7\frac{7}{8}}{472\frac{1}{4}}$  lbs. Ans.

17. A farmer sowed 5 bu. 1 pk. 1 qt. of seed, and harvested from it 103 bu. 3 pks. 5 qts. How much did he raise from a bushel of seed?

5 bu. 1 pk. 1 qt.:  
1 qt. = 
$$\frac{1}{8}$$
 pk.  
1 $\frac{1}{8}$  pk. =  $\frac{1}{8}$  bu. =  $\frac{9}{82}$  bu.  
5 $\frac{9}{82}$  bu.

103 bu. 3 pks. 5 qts.:  
5 qts. = 
$$\frac{5}{8}$$
 pk.  
3 $\frac{5}{8}$  pks. =  $\frac{3\frac{5}{8}}{4}$  bu. =  $\frac{3\frac{9}{3}}{3}$  bu.  
103 $\frac{39}{3}$  bu.

$$\frac{103\frac{29}{5\frac{9}{82}}}{5\frac{9}{82}} = \frac{3325}{169} = 19\frac{114}{169} \text{ bu.}$$

$$\frac{114}{169} \text{ of 4 pks.} = 2\frac{118}{169} \text{ pks.}$$

$$\frac{118}{169} \text{ of 8 qts.} = 5\frac{99}{169} \text{ qts.}$$

$$19 \text{ bu. 2 pks. 5.6 qts. } Ans.$$

18. How many bushels in 5 t. of oats?

2000 lbs. 
$$\frac{5}{10000}$$
 lbs.  $\frac{312\frac{1}{2}}{32)10000}$  bu. Ans.

19. How many bottles, each holding 1 pt. 3 gi., can be filled from a barrel of cider?

1 pt. 3 gi.:  
3 gi. = 
$$\frac{3}{4}$$
 pt.  
1\frac{3}{4} pt. =  $\frac{1\frac{3}{4}}{8}$  gal. =  $\frac{7}{32}$  gal.  
16 9  
 $\frac{31\frac{1}{4}}{7} = \frac{32}{7} \times \frac{63}{2} = 144$ . Ans.

20. If a steamer make 13 mi. 6 rds. an hour, how far will she go between 6 A.M. and 6 P.M.? How many hours will she require to make 113 miles?

21. If a locomotive run at the rate of 111 rds. a minute, how many hours will it require to run from Boston to Buffalo, 498 miles?

498 mi.

× 320

159360 rds.

143535

111)159360

6)143.535

24 nearly. Ans.

22. What is the cost of 12 A. 146 sq. rds. land at \$16.25 an acre?

146 sq. rds. =  $\frac{78}{80}$  A. 1278 × \$16½ =  $\frac{1033}{80}$  ×  $\frac{$65}{4}$ =  $\frac{$13429}{64}$  = \$209.83. Ans.

28. What is the cost of 8 t. 3 cwt. 27 lbs. of coal at \$5.75 a ton?

100 27 lbs.
20 3.27 cwt.
8.1635 t.

×\$5\$
\$46.94. Ans.

24. What is the cost of 7 t. 1560 lbs. of hay at \$15.50 a ton?

1560 lbs. = 
$$\frac{1358}{2568}$$
 t. =  $\frac{78}{100}$  t.  
7.78  
 $\times \$15\frac{1}{2}$   
 $\$120.59$ . Ans.

25. What is the cost of a carload of wheat weighing 20,000 lbs., at \$1.05 a bushel?

6) 
$$2000$$
 $333\frac{1}{3}$ 
×  $$1.05$ 
 $$350$ . Ans.

26. Reduce 5 rds. 4 yds. 2½ ft. to the decimal of a mile.

27. Reduce 9 sq. ch. 11.25 sq. rds. to the decimal of an acre.

28. Reduce 0.09375 bu. to quarts.

29. Reduce 7560 chains to miles.

30. How many gross are 2000 pens?

$$13\frac{8}{9}$$
. Ans.  $144)2000$ 

31. Find the cost of 27.248 A., at \$93.75 an acre.

32. Which is the greater, 2.8 of 3 ft. 11 in. or 3.11 of 2 ft. 8 in., and by how much?

3 ft. 11 in. 2 ft. 8 in.  

$$\times \frac{12}{47}$$
 in.  $\times \frac{12}{32}$  in.  
 $\times \frac{2.8}{131.6}$  in.  $\times \frac{3.11}{99.52}$  in.  
 $\frac{99.52}{2}$   
12)32.08 in.  
2 ft. 8.08 in.

The former by 2 ft. 8.08 in. Ans.

33. Reduce 171 lbs. 6 oz. troy to the decimal of a ton avoirdupois.

34. Express 14.52 sq. yds. as the decimal of a square chain.

35. If a sovereign be equal to 25.22 francs, or to \$4.85, what decimal of a dollar is a franc?

36. Express 2.805 florins—1.89 half-crowns as the decimal of £0.472.

$$0.09375$$
. Ans.  $472)44.25000$ 

37. If 0.327 of some work be done in 3 hrs. 38 min., how long will the whole work require?

3 hrs. 38 min.

60
218 min.

$$\frac{666.6}{327)218000.0}$$

 $0.\dot{6} = \frac{6}{9} = \frac{2}{3}.$ 

 $666.6 \text{ min.} = 666\frac{2}{3} \text{ min.}$ 

 $= 11 \text{ hrs. } 6\frac{2}{3} \text{ min.}$ 

= 11 hrs. 6 min. 40 sec. Ans.

38. A can run a mile in 7.68 min.; B can run at the rate of 7.68 mi. an hour. Which is the faster runner?

.. A is the faster runner.

39. How many miles an hour does a person walk who takes 2 steps a second and 1900 steps in a mile?

$$\begin{array}{r}
 60 \\
 \times 2 \\
 \hline
 120 \\
 \times 60 \\
 \hline
 7200 \text{ steps.} \\
 \hline
 3\frac{15}{18} \text{ mi. } Ans. \\
 \hline
 19)72$$

40. If an ounce troy of gold be worth \$20, what is the value of a pound avoirdupois?

\$20  
$$\times 12$$
  
\$240 per lb. troy.

$$\frac{175}{7999} \times \frac{5}{3} \times \frac{349}{1} = \frac{875}{3} = $291.67.$$
144
Ans.

41. Two stars cross the meridian at 6 hrs. 4 min. 42.3 sec. and 7 hrs. 2 min. 57.21 sec., respectively. What is the interval between the observations?

42. How long will it take to fill  $\frac{13}{25}$  of a cistern, when the whole requires 6 hrs. 10 min.?

6 hrs. 10 min.  
10 min. = 
$$\frac{10}{60}$$
 hr. =  $\frac{1}{6}$  hr.  
6 $\frac{1}{6}$  hrs.  
6 $\frac{1}{6}$  ×  $\frac{13}{25}$  =  $\frac{37}{6}$  ×  $\frac{13}{25}$   
=  $\frac{431}{150}$  =  $3\frac{31}{150}$  hrs.

\$\frac{21}{150}\$ of 60 min. = 12\frac{2}{5}\$ min.
\$\frac{2}{5}\$ of 60 sec. = 24 sec.
3 hrs. 12 min. 24 sec. Ans.

43. The circumference of a circle is 6 yds. 1 ft. 5.1 in., and is divided into 360 degrees. What is the length of 55 degrees?

$$\begin{array}{c} 55 = \frac{11}{13} \\ 6 \text{ yds. 1 ft. 5.1 in.} \\ \times \frac{3}{19} \text{ ft.} \\ \times \frac{12}{228} \\ \times \frac{5.1}{233.1} \text{ in.} \\ \hline 3.2375 \\ 72)233.1000 \\ 3.2375 \text{ in.} \\ \times 11 \\ \hline \end{array}$$

3.2375 in. ×11 12)35.6125 in. 2 ft. 11.6125 in. Ans.

44. Multiply 2 t. 16 cwt. 63\{\frac{1}{2}}\]
lbs. by 1\{\frac{1}{2}}.

45. Into how many shares has £120 been divided when each share is £3 8 s. 64 d.7

6\$ 
$$d = \frac{65}{12}$$
  $a = 46$ .

8\$  $a = £\frac{84}{20} = £4$ .

13  $\frac{3}{15}$ ,  $\frac{8}{9} = \frac{39}{45}$ 

14 the less?

15 the less?

16 the less?

18 the less?

18 the less?

18  $\frac{13}{15}$ ,  $\frac{8}{9} = \frac{39}{45}$ 

19 the former is the greater. Ans.

19  $\frac{120}{34} = \frac{7}{24} \times \frac{129}{1} = 35$ . Ans.

10  $\frac{12}{34} = \frac{9}{8} \times \frac{13}{15} = \frac{39}{40}$ . Ans.

10  $\frac{12}{34} = \frac{9}{8} \times \frac{13}{15} = \frac{39}{40}$ . Ans.

46. If 👬 of one line be equal to & of another line, which is the greater? and what fraction of it is the less?

$$\frac{13}{15}$$
,  $\frac{8}{9} = \frac{39, 40}{45}$ 

$$\frac{11}{4} = \frac{3}{8} \times \frac{13}{15} = \frac{39}{40}. Ans.$$

47. Multiply 5 mi. 206 rds. 2 ft. 2 in. by 786.

48. The returns of a gold mine are 241 t. of ore yielding 2 or rs. of fine gold a ton, and 193 t. yielding 1 oz. 12 dwt. Find the value of the whole yield, at \$19.45 an one.

49. Divide 93 long tons 56 lbs. by 23 lbs. 5 oz.

50. Telegraph poles on railroads are generally erected at intervals of 88 yds. Show that if a passenger count the number of poles which the train passes in three minutes, that number will express the number of miles an hour the train is going.

1760 yds. = 1 mi. 60 min. = 1 hr. 88 yds. = 
$$\frac{1}{20}$$
 mi. 3 min. =  $\frac{1}{20}$  hr.

51. If Greenwich time be 5 hrs. 8 min. 16 sec. later than Washington time, and Chicago be 87° 35′ W., what is the difference between Washington and Chicago time?

$$87^{\circ} 35' = 4 \times (87 \text{ min. } 35 \text{ sec.})$$
= 5 hrs. 50 min. 20 sec.

5 hrs. 8 min. 16 sec.

42 min. 4 sec. Ans.

## EXERCISE LVIII.

1. A train from New York to Philadelphia, 90 miles, makes the whole distance in 2 hrs. 5 min. What is its rate?

2 hrs. 5 min. = 
$$2\frac{1}{12}$$
 hrs.  
90 mi. +  $2\frac{1}{12}$  =  $43\frac{1}{5}$  mi. Ans.

2. Winlock, in 1869, found that electricity went through 7200 miles of wire in ‡ of a second. What was its rate per second?

$$7200 \text{ mi.} + \frac{2}{3} = 10,800 \text{ mi.}$$
 Ans.

3. If the time required for a signal to pass through the cable from Brest to Duxbury, 3799 miles, be 0.816 of a second, what is the rate per second?

4. If the report of a gun 12 miles distant is heard in 55 seconds after the flash is seen, what is the velocity of sound, in feet, per second?

5. If a man walk 31 miles in 46 minutes, what is his rate per hour?

6. If a horse go 47½ miles in 10 hrs. 40 min., what is his average rate per hour?

7. If a stone on a glacier move 95½ feet in 188 days, what is its rate, in inches, per day?

$$95\frac{1}{2}$$
 ft. +  $188 = \frac{1}{2}\frac{2}{16}$  ft. =  $6\frac{9}{16}$  in. Ans.

8. If a horse trot & of a mile in 2} minutes, in what time can be trot a mile?

sin run 18 miles in 39 minutes, how long does it take to

nd travel 1125 feet a second, how long will it take to ale?

$$1 \text{ mi.} = 5280 \text{ ft.}$$
  
 $5280 + 1125 = 4.7 \text{ sec. } Ans.$ 

rain require 3 hours to travel 1041 miles, find its avertravelling a mile.

$$104\frac{1}{2}$$
 mi.  $+ 3 = 34\frac{1}{2}$  mi.  
 $\sin_1 + 34\frac{1}{2} = 1\frac{1}{2}\frac{1}{2}$  min.  $= 1$  min.  $43\frac{1}{13}\frac{1}{2}$  sec. Ans.

12. If a mower cut 7½ acres of grass in 3½ days, what part of a day will it take him to cut one acre? If a day consist of 10 working-hours, what part of an acre does he cut in an hour?

$$3\frac{1}{2}$$
 dys.  $\div 7\frac{1}{2} = \frac{7}{15}$  dy. Ans.  $3\frac{1}{2}$  dys. of 10 hrs.  $= 35$  hrs., and  $7\frac{1}{4}$  A.  $\div 35 = \frac{3}{14}$  A. Ans.

13. If a mower cut 3½ square rods in ½ of an hour, how many acres can he cut in a day of 10 hours?

$$3\frac{1}{2}$$
 sq. rds. +  $\frac{1}{8}$  = 28 sq. rds.  
 $10 \times 28$  sq. rds. = 280 sq. rds. =  $1\frac{3}{4}$  A. Ans.

14. If a fountain yield 117½ gallons in ‡ of an hour, at what rate per hour is it flowing?

$$117\frac{1}{2}$$
 gals.  $+\frac{3}{4} = 156\frac{3}{2}$  gals. Ans.

15. If a merchant's profits be \$3147 in 7½ months, what are his profits for a year?

$$7\frac{1}{2}$$
 mo. =  $\frac{7\frac{1}{2}}{12}$  yr. =  $\frac{5}{8}$  yr.   
\$ 3147 +  $\frac{5}{8}$  = \$5035.20. Ans.

16. If a wheel turn 17° 30' in 35 minutes, in how many hours does it make a complete revolution?

$$17^{\circ} 30' + 35 = 30' = \frac{1}{2}^{\circ}$$
 in one min.  $360 + \frac{1}{2} = 720$  min. = 12 hrs. Ans.

17. If a man's expenditures be \$4358 in 131 months, what is his yearly rate of expenditure?

$$13\frac{1}{8}$$
 m.  $=\frac{13\frac{1}{8}}{12}$  yr.  $=\frac{10}{9}$  yr.  $\frac{10}{9}$  yr.  $\frac{13}{9}$  4358  $+\frac{10}{9}$  = \$3922.20. Ans.

18. If a cistern lose by leakage 7 gals. 1 pt. in 49 hrs. 40 min., what is its hourly rate of loss?

49 hrs. 40 min. = 49
$$\frac{2}{3}$$
 hrs.  
7 gals. 1 pt. = 57 pts.  
57 pts. + 49 $\frac{2}{3}$  =  $1\frac{2}{120}$  pts.

19. If the circumference of the earth at the equator be 24,900 miles, at what rate per hour is a person there carried round, cas whole rotation being made in 23 hrs. 56 min.?

20. If a man travel 3<sup>§</sup> miles in 7<sup>§</sup> minutes, how many miles will he travel in 50 minutes? and how long will he take to travel 50 miles?

21. If A can mow a certain meadow in 4 days, and B in 3 days, how long will it take both?

If A can mow it in 4 days, in one day he can mow  $\frac{1}{4}$  of it.

If B can mow it in 3 days, in one day he can mow  $\frac{1}{4}$  of it.

Both together can mow  $\frac{1}{4} + \frac{1}{4} = \frac{7}{12}$  of it in one day.

.. both together can mow the whole in 34 days, or 15 days. Ass.

22. If A can lay a certain wall in 4½ days, and B in 5½ days, how long will it take both?

If A can do it in  $4\frac{1}{4}$  days, in one day he can do  $\frac{1}{4\frac{1}{4}} = \frac{2}{5}$  of it.

can do it in  $5\frac{1}{4}$  days, in one day he can do  $\frac{1}{5\frac{1}{4}} = \frac{2}{11}$  of it.

I together can do  $\frac{2}{5} + \frac{2}{11} = \frac{2}{5}$  of it in one day.

oth together can do the whole in  $\frac{2}{15}$  days, or  $2\frac{1}{15}$  days. Ass.

a pipe will fill a vessel in 4½ hours, and another in 3½ hours, will it take both to fill the vessel?

to pipe will fill it in 4½ hrs., in one hr. it will fill  $\frac{1}{4\frac{1}{4}} = \frac{1}{4}$  of it.

other pipe will fill it in 3½ hrs., in one hr. it will fill  $\frac{1}{3\frac{1}{4}} = \frac{1}{7}$  of it.

pipes together will fill  $\frac{3}{4} + \frac{3}{4} = \frac{34}{12}$  of it in one hour. oth pipes together will fill it in  $\frac{34}{12} = 1\frac{34}{12}$  hrs. = 1 hr. 58 min.  $7\frac{1}{4}$  sec. Ans.

24. If A can go from Boston to Albany in 9½ hours, and B from Albany to Boston in 11½ hours, and they start at the same time, in how many hours will they meet?

If A can go in  $9\frac{1}{4}$  hrs., in 1 hour he can go  $\frac{1}{9\frac{1}{4}} = \frac{4}{37}$  of the distance.

If B can go in 11½ hrs., in 1 hour he can go  $\frac{1}{114} = \frac{3}{34}$  of the distance.

Both together can go  $\frac{4}{37} + \frac{3}{34} = \frac{247}{1258}$  of the distance in 1 hour.

... they will meet in  $\frac{1258}{247}$  hrs. =  $5\frac{23}{247}$  hrs.

25. A requires 4 days, B 3 days, and C 41 days, to do a certain piece of work. How long will it take all three working together?

If A can do it in 4 days, in one day he can do 1 of it.

If B can do it in 3 days, in one day he can do 1 of it.

If C can do it in  $4\frac{1}{2}$  days, in one day he can do  $\frac{1}{4\frac{1}{4}} = \frac{2}{3}$  of it.

All together can do  $\frac{1}{4} + \frac{1}{8} + \frac{2}{8} = \frac{2}{8}$  of it in one day.

... it will take them, all working together,  $\frac{3}{2}$  days =  $1\frac{7}{29}$ . Ans.

26. A can mow  $\frac{2}{3}$  of a field in 3 days; B can mow  $\frac{2}{3}$  of it in 4 days. How long will it take both to mow the field?

3 days +  $\frac{5}{3}$  =  $5\frac{2}{5}$  days, and 4 days +  $\frac{2}{3}$  = 6 days.

If A can mow it in  $5\frac{2}{5}$  days, in one day he can mow  $\frac{1}{5\frac{3}{5}} = \frac{5}{27}$  of it.

If B can mow it in 6 days, in one day he can mow & of it.

Both together can mow  $\frac{3}{27} + \frac{1}{6} = \frac{19}{54}$  of it in one day.

... both together can mow it in  $\frac{54}{15}$  days =  $2\frac{15}{15}$  days. Ans.

27. One pipe can fill a cistern half full in \( \frac{1}{2} \) of an hour, and another can fill it three-quarters full in \( \frac{1}{2} \) an hour. How long will it take both pipes to fill the cistern?

 $\frac{3}{4}$  hr.  $+\frac{1}{4} = 1\frac{1}{2}$  hrs., and  $\frac{1}{2}$  hr.  $+\frac{3}{4} = \frac{2}{3}$  hr.

If one pipe fills it in  $1\frac{1}{2}$  hrs., in one hour it will fill  $\frac{1}{1\frac{1}{4}} = \frac{2}{3}$  of it.

If another pipe fills it in  $\frac{3}{4}$  hr., in one hour it will fill  $\frac{1}{\frac{3}{4}} = \frac{3}{4}$  of it.

Both together will fill  $\frac{2}{3} + \frac{1}{2} = \frac{13}{6}$  of it in one hour.

... both together will fill it in  $6 + 13 = \frac{6}{13}$  hr. Ans.

28. A cistern which holds 100 gallons can be filled from a pipe in 25 minutes, and emptied by a waste-pipe in 45 minutes. If both are opened together, how long will it take to fill the cistern, and how much water will be wasted?

The water-pipe fills  $\frac{1}{25}$  every minute.

The waste-pipe empties 45 every minute.

When both are open,  $\frac{1}{25} - \frac{1}{45} = \frac{4}{225}$  is gained every minute.

... the whole will be filled in  $\frac{225}{4} = 56\frac{1}{4}$  min. Ans.

If  $\frac{1}{45}$  of the cistern is wasted every minute, in  $56\frac{1}{4}$  minutes  $56\frac{1}{4} \times \frac{1}{45}$  would be wasted.

Now, as the cistern holds 100 gals., the number of gallons wasted would be  $56\frac{1}{4} \times \frac{1}{45} \times 100$  gals.

$$56\frac{1}{4} \times \frac{1}{45} \times 100 = \frac{225}{4} \times \frac{1}{45} \times \frac{25}{100} = 125 \text{ gals. Ans.}$$

29. A pipe can fill a cistern one-third full in  $\frac{1}{4}$  of an hour; a waste-pipe can empty  $\frac{1}{4}$  of the cistern in 20 minutes. If both pipes are opened, in what time will the cistern be filled?

 $\frac{1}{4} \text{ hr.} \times 3 = \frac{3}{4} \text{ hr.} = 45 \text{ min.}, \text{ and } 20 \text{ min.} \times 4 = 80 \text{ min.}$ 

The water-pipe fills  $\frac{1}{45}$  every minute.

The waste-pipe empties 1/8 every minute.

When both are open,  $\frac{1}{45} - \frac{1}{80} = \frac{7}{720}$  is gained every minute.

:. the whole will be filled in  $\frac{720}{7} = 1025$  min.

= 1 hr. 42 min. 51\space sec. Ans.

- 30. If one pipe runs into a cistern at the rate of 2 gallons in 3 minutes, and another at the rate of 5 gallons in 4 minutes, while the water is running out of a third pipe at the rate of 4 gallons in 5 minutes, how long will it take to gain 71 gallons in the cistern?
  - 2 gals. + 3 = \frac{2}{3} gals., 5 gals. + 4 = \frac{5}{4} gals., and 4 gals. + 5 = \frac{4}{3} gals.

    If one pipe pours in \frac{2}{3} gals. per minute, another pours in \frac{5}{4} gals. per minute, and another empties \frac{4}{5} gals. per minute, the cistern gains \frac{2}{3} + \frac{5}{4} \frac{1}{5} = \frac{2}{6} \frac{7}{6} gals. per minute.
  - ... it will take as many minutes to gain 71 gals. as  $71 + \frac{67}{66} = 63\frac{39}{67}$  min. = 1 hr. 3 min.  $34\frac{67}{67}$  sec.

31. A and B can do a piece of work in 2½ days; A and C in 3½ days; B and C in 4½ days. Required the time in which all three, working together, can do the work, and in which each can do it alone.

If A and B can do it in  $2\frac{1}{2}$  days, they can do  $\frac{1}{2\frac{1}{2}} = \frac{2}{5}$  of it in one day.

If A and C can do it in  $3\frac{1}{8}$  days, they can do  $\frac{1}{3\frac{1}{8}} = \frac{3}{10}$  of it in one day.

If B and C can do it in  $4\frac{1}{4}$  days, they can do  $\frac{1}{4\frac{1}{4}} = \frac{4}{17}$  of it in one day.

All can do  $\frac{2}{5} + \frac{3}{10} + \frac{4}{17} = \frac{159}{170}$  in 2 days, or  $\frac{159}{840}$  of it in one day.

... all can do it in  $\frac{340}{159} = 2\frac{22}{159}$  days. Ans.

If A, B, and C can do  $\frac{159}{340}$ , and B and C  $\frac{4}{17}$  of it in one day, A can do  $\frac{159}{340} - \frac{4}{17} = \frac{79}{340}$  of it in one day.

... A can do the whole in  $\frac{340}{79} = 474$  days. Ans.

If A, B, and C can do  $\frac{159}{340}$ , and A and C  $\frac{3}{10}$  of it in one day, B can do  $\frac{159}{340} - \frac{3}{10} = \frac{57}{340}$  of it in one day.

... B can do the whole in  $\frac{340}{57} = 555$  days. Ans.

If A, B, and C can do  $\frac{159}{340}$ , and A and B  $\frac{2}{5}$  of it in one day, C can do  $\frac{159}{340} - \frac{2}{5} = \frac{23}{340}$  of it in one day.

 $\therefore$  C can do the whole in  $\frac{840}{28} = 14\frac{18}{28}$  days. Ans.

32. Sampson & Reed sold § of a lot of wheat to one party, § of the remainder to another, and had 93 bushels left. How much had they at first?

After selling § of the wheat they had § left.

After selling  $\frac{3}{4}$  of  $\frac{3}{8}$  of the wheat they had  $\frac{1}{4}$  of  $\frac{3}{8} = \frac{3}{32}$  left.

Then 93 bush. =  $\frac{3}{32}$  of the lot.

... the whole lot = 93 bush.  $+\frac{3}{32}$  = 992 bush. Ans.

33. In a certain school  $\frac{9}{16}$  of the scholars are girls,  $\frac{4}{7}$  of the boys are over 16 years old, and 6 boys are under 16. How many girls, and how many scholars in all?

After the girls, or  $\frac{9}{16}$  of the school, are taken out, there remain  $\frac{7}{16}$  of the school, or the boys.

After  $\frac{4}{7}$  of  $\frac{7}{16}$  are taken out,  $\frac{3}{7}$  of  $\frac{7}{16} = \frac{3}{16}$  are left.

... the whole number of scholars is  $6 + \frac{3}{16} = 32$  scholars. Ans.

 $\frac{9}{16}$  of 32 scholars = 18, number of girls. Ans.

 In a certain school 11 are boys; \( \frac{1}{2} \) of the girls are under 16, and 13 girls are over 16. How many boys and how many girls in the school?

After the boys, or 12 of the school, are taken out, there remains 11 of the school, or the girls.

1

After  $\frac{p_2}{\sqrt{2}}$  of  $\frac{1}{2}$  are taken out,  $\frac{1}{2}$  of  $\frac{1}{2}$  =  $\frac{1}{2}$  are left.

 $\therefore$  the whole number of scholars =  $13 + \frac{14}{14} = 48$  scholars.

11 of 48 = 22 girls. Ans. 12 of 48 = 26 boys. Ans.

35. If from a certain number # of it be subtracted, then # of the remainder, then \$ of that remainder, and 8 still remain, what is the number?

After # of it is subtracted, # is left.

After  $\frac{1}{4}$  of  $\frac{1}{4}$  is subtracted,  $\frac{1}{4}$  of  $\frac{1}{4} = \frac{1}{4}$  is left.

After  $\frac{1}{2}$  of  $\frac{1}{3}$  is subtracted,  $\frac{4}{3}$  of  $\frac{1}{3} = \frac{4}{35}$  is left.

 $\therefore$  the number = 6 +  $\frac{4}{15}$  = 35. Ans.

36. 20 is # of # of what number?

6. 20 is 
$$\frac{1}{6}$$
 of  $\frac{3}{6}$  of  $\frac{3}{6}$  of what number?

 $\frac{8}{8}$  of  $\frac{2}{3}$  of  $\frac{2}{3} - \frac{1}{6}$ . ... the number = 20 +  $\frac{1}{6}$  = 120. Ans.

87. 6 is \$ of \$ of \$ of what number?

$$\frac{6}{7}$$
 of  $\frac{4}{5}$  of  $\frac{1}{4} = \frac{6}{35}$ . ... the number =  $6 + \frac{\pi}{35} = 35$ . Ans.

38. Express  $\frac{1}{\sqrt{2}}$  of 1 lb. troy +  $\frac{1}{\sqrt{2}}$  of 1 lb. avoirdupois as troy and as avoirdupois weights.

av. = 
$$\frac{1}{29}$$
 of  $\frac{7999}{5769} = \frac{175}{4176}$  lbs. troy.  
 $\frac{175}{176} = \frac{144 + 175}{4176} = \frac{319}{4176} = \frac{11}{144}$  lbs. troy.  
s. =  $\frac{11}{144}$  of 12 oz. =  $\frac{11}{14}$  oz. =  $\frac{11}{14}$  of 20 dwt. = 18 $\frac{1}{14}$  dwt.  
= 18 dwt. 8 grs. Ans.

s. troy = 
$$\frac{11}{144}$$
 of  $\frac{144}{7999} = \frac{11}{175}$  lbs. av.

$$B_{1} = \frac{11}{175}$$
 of 16 oz. =  $1\frac{1}{175}$  oz. av. Ans.

39. The cargo of a ship, worth \$45,000, belongs to three partners. A owns  $\frac{7}{5}$  of  $\frac{3}{5}$  of it, B's share is equal to  $3\frac{3}{14}$  of  $\frac{2}{5}$  of A's share, and C owns the remainder. What ought each to receive from the sale?

$$\frac{7}{3}$$
 of  $\frac{8}{5} = \frac{7}{15}$  of ship.  $\frac{7}{15}$  of \$45,000 = \$21,000, A's share.  $3\frac{8}{14}$  of  $\frac{2}{9}$  of  $\frac{7}{15} = \frac{1}{3}$  of ship.  $\frac{1}{3}$  of \$45,000 = \$15,000, B's share. \$45,000 - (\$21,000 + \$15,000) = \$9000, C's share.

40. Find the largest number which is contained an integral number of times in each of the following:  $2\frac{1}{5}$ ,  $6\frac{7}{15}$ ,  $11\frac{1}{2}$ ,  $19\frac{1}{6}$ .

25, 
$$6\frac{7}{18}$$
,  $11\frac{1}{2}$ ,  $19\frac{1}{6} = \frac{28}{9}$ ,  $\frac{115}{18}$ ,  $\frac{28}{2}$ ,  $\frac{115}{6}$ . G. C. M. of 23, 115, 23, 115 = 23.

L. C. M. of 9, 18, 2, 
$$6 = 18$$
.

... G. C. M. of fractions = 
$$\frac{28}{18} = 1\frac{5}{18}$$
. Ans.

41. A person bequeathed  $\frac{5}{12}$  of his property to A,  $\frac{1}{4}$  of it to B,  $\frac{1}{6}$  to C,  $\frac{1}{8}$  to D, and the remainder, \$550, to E. What was the value of the whole property?

$$\frac{5}{12} + \frac{1}{4} + \frac{1}{8} + \frac{1}{8} = \frac{23}{24}$$
.  
After  $\frac{23}{24}$  is subtracted,  $\frac{1}{24}$  remains.  
∴ whole money = \$550 +  $\frac{1}{24}$  = \$13,200. Ans.

42. Arrange in descending order of magnitude, \(\frac{1}{2}\), \(\frac{1}{2}\), \(\frac{1}{2}\),

$$\frac{13}{25}$$
,  $\frac{15}{26}$ ,  $\frac{16}{27} = \frac{9126, 10125, 10400}{17550}$ .

- : the order of magnitude is  $\frac{1}{27}$ ,  $\frac{15}{26}$ ,  $\frac{13}{25}$ . Ans.
- 43. A bankrupt's debts are \$2520, and the value of his property is \$1890. How much can he pay on a dollar?

$$\frac{$1890}{2520} = \frac{$3}{4} = $0.75$$
. Ans.

44. A bankrupt's debts are \$4264, and he pays  $62\frac{1}{2}$  cents on a dollar; what are his assets?

$$0.62\frac{1}{2} = \frac{5}{8}$$
 of  $\frac{$4264}{1} = $2665$ . Ans.

45. If 15 yards of silk cost \$18.75, how much will 201 yards cost?

and 20½ yds. cost 
$$20½ \times \frac{$18½}{15}$$
.

$$20\frac{1}{15} \times \frac{$18\frac{1}{4}}{15} = \frac{61}{3} \times \frac{1}{15} \times \frac{$75}{4} = \frac{$305}{12} = $25.42$$
. Ans.

46. If 3} pounds of tea cost \$3.80, how much can I buy for \$21.87?

If 32 lbs. cost \$3.80, 1 lb. costs  $\frac{$3.80}{35}$ , and as much can be

bought for \$21.87 as 
$$2187 + \frac{380}{31}$$
.

$$2187 + \frac{380}{3\frac{2}{3}} = \frac{12}{5} \times \frac{1}{500} \times \frac{2182}{1} = \frac{27179}{1908} = 19\frac{2979}{1908} \text{ lbs. Ans.}$$

47. If  $\frac{1}{14}$  of a ton of coal cost \$1.12, what is the price of 5½ cwt.?

$$5\frac{1}{2}$$
 cwt.  $=\frac{5\frac{1}{2}}{20}$  t.  $=\frac{11}{46}$  t.

If  $\frac{4}{14}$  t. cost \$1.12, 1 t. costs  $\frac{$1.12}{14}$ , and  $\frac{11}{46}$  t. costs  $\frac{11}{46} \times \frac{$1.12}{14}$ 

$$\frac{11}{49} \times \frac{\$1.17}{1} \times \frac{14}{3} = \frac{\$21.56}{15} = \$1.44. \text{ Ans.}$$

 $f_{11}^{A}$  of a piece of work be done in 25 days, how much will in 112 days?

 $\frac{1}{4}$  can be done in 25 days, the whole can be done in  $\frac{25}{4}$  days,

nd as much can be done in 112 days as 112 +  $\frac{25}{11}$ 

$$+\frac{25}{11} = \frac{2}{11} \times \frac{1}{25} \times \frac{7}{3} = \frac{14}{165}$$
. Ans.

49. A man walks 18 mi. 106 rds. 3‡ yards in 5½ hours. How long does he take to walk a mile and a half?

18 mi. 106 rds. 
$$3\frac{3}{5}$$
 yds.:  $106\frac{2}{3}$  rds.  $=\frac{106\frac{2}{5}}{320} = \frac{1}{5}$  mi.  $106\frac{2}{5}$  rds.  $=\frac{106\frac{2}{5}}{320} = \frac{1}{5}$  mi.  $106$  rds.  $3\frac{2}{5}$  yds.  $=18\frac{1}{5}$  mi.

If he walks  $18\frac{1}{3}$  mi. in  $5\frac{1}{2}$  hrs., he will walk  $\frac{18\frac{1}{3}}{5\frac{1}{4}}$  mi. in 1 hr.,

and it will take him as long to walk  $1\frac{1}{2}$  miles as  $1\frac{1}{2} + \frac{18\frac{1}{4}}{5\frac{1}{4}}$ .

$${\overset{\bullet}{1}}_{\frac{1}{2}} + \frac{18\frac{1}{3}}{5\frac{1}{2}} = \frac{11}{2} \times \frac{3}{55} \times \frac{3}{2} = \frac{9}{20} \text{ hr.} = 27 \text{ min. } Ans.$$

50. When an ounce of gold is worth \$19.45, what is the value of 0.04 of a pound?

$$$19.45 \times 12 \times 0.04 = $9.336$$
. Ans.

51. If 9 horses can plow 46 acres in a certain time, how many acres can 12 horses plow in the same time?

Since 9 horses can plow 46 acres in a certain time, 1 horse can plow  $\frac{1}{3}$  of 46 acres in the same time, and 12 horses can plow  $12 \times \frac{1}{3}$  of  $46 = 61\frac{1}{3}$  acres. Ans.

52. If 12 men can reap a field in 4 days, in what time will 32 men reap it?

Since 12 men can reap a field in 4 days, 1 man can reap it in  $12 \times 4$  days, and 32 men can reap it in  $\frac{12 \times 4}{32}$  days =  $1\frac{1}{2}$  days. Ans.

53. If 72 men dig a trench in 63 days, in how many days will 42 men dig another trench three times as great?

Since 72 men can dig a trench in 63 days,

1 man can dig it in  $72 \times 63$  days.

1 man can dig one 3 times as large in  $3 \times 72 \times 63$  days,

and 42 men can dig it in  $\frac{3 \times 72 \times 63}{42}$  days = 324 days. Ans.

54. If a man travels 540 miles in 24 days, walking 6 hours a day, how many miles can be travel in 3 days, walking 8 hours a day?

Since he can go 540 mi. in  $24 \times 6$  hrs. = 144 hrs., in one hour he can go  $\frac{1}{144}$  of 540 mi., and in  $3 \times 8$  hrs. = 24 hrs. he can go  $24 \times \frac{1}{144}$  of 540 mi. = 90 mi. Ans.

55. If 15 men can perform a piece of work in 22 days, how many men will finish another piece of work four times as large in \frac{1}{2} of the time?

Since 15 men can do the work in 22 days, it will take  $4 \times 15$  men to do 4 times the work in 22 days, and to do 4 times, the work in  $\frac{1}{5}$  of 22 days it will take  $5 \times 4 \times 15$  men = 300 men. Ans.

56. A garrison of 2100 has provisions for 9 months, but receives reinforcements of 600 men. How long will the provisions last?

Since the provisions will last 2100 men 9 months, they will last 1 man  $2100 \times 9$  months, and they will last 2100 + 600 = 2700 men

$$\frac{2100\times9}{2700}$$
 mos. = 7 mos. Ans.

57. If a cubic foot of ice weigh 57% pounds, how many cubic feet of ice will weigh a ton?

Since 1 cubic foot of ice weighs 57 $\frac{3}{8}$  lbs.; to weigh a ton it will take  $\frac{2000}{57\frac{3}{8}}$  cu. ft. =  $34\frac{394}{459}$  cu. ft. Ans.

58. How many bushels of wheat will serve 72 people 8 days when 4 bushels serve 6 people 24 days?

72 people will eat twelve times as much as 6 people in the same time.

And the same number of people will eat  $\frac{1}{8}$  as much in 8 days as in 24 days.

Hence, 72 people in 8 days will eat  $12 \times \frac{1}{8}$  times as much as 6 people in 24 days.

 $12 \times \frac{1}{3} \times 4$  bushels = 16 bushels. Ans.

59. If 2 horses eat 8 bushels of oats in 16 days, how many horses will eat 3000 bushels in 24 days?

In 16 days 8 bu. can be eaten by 2 horses.

In 1 day 8 bu. can be eaten by  $16 \times 2$  horses.

In 1 day 1 bu. can be eaten by  $\frac{16 \times 2}{8}$  horses.

In 24 days 1 bu. can be eaten by  $\frac{16\times2}{24\times8}$  horses.

In 24 days 3000 bu. can be eaten by  $\frac{3000 \times 16 \times 2}{24 \times 8}$  horses, = 500 horses. Ans.

60. If a man travel 150 miles in 5 days, when the days are 12 hours long, in how many days of 10 hours each will he travel 500 miles?

He can go 150 miles in 5 days of 12 hours = 60 hours.

He can go 1 mile in  $\frac{60}{180}$  hour.

He can go 500 miles in  $\frac{500 \times 60}{150}$  hours.

He can go 500 miles in  $\frac{500 \times 60}{150 \times 10}$  days of 10 hours,

= 20 days. Ans.

61. If a regiment of 939 soldiers consume 351 bushels of wheat in 21 days, how many soldiers will consume 1404 bushels in 7 days?

1404 bu. will last the same number of men four times as long as 351 bu.

And the same amount will last three times the number of men for 7 days as for 21 days.

 $3 \times 4 \times 939$  soldiers = 11,268 soldiers. Ans.

62. If 5 men can reap a field of  $12\frac{1}{2}$  acres in  $3\frac{1}{2}$  days, working 16 hours a day, in what time can 7 men reap a field of 15 acres, working 12 hours a day?

5 men can reap  $12\frac{1}{2}$  acres in  $3\frac{1}{2}$  days of 16 hours = 56 hours.

1 man can reap  $12\frac{1}{4}$  acres in  $5 \times 56$  hours.

1 man can reap 1 acre in  $\frac{5 \times 56}{12\frac{1}{4}}$  hours.

1 man can reap 15 acres in  $\frac{15 \times 5 \times 56}{12\frac{1}{2}}$  hours.

7 men can reap 15 acres in  $\frac{15 \times 5 \times 50}{7 \times 12\frac{1}{4}}$  hours.

7 men can reap 15 acres in  $\frac{15 \times 5 \times 56}{12 \times 7 \times 12\frac{1}{4}}$  days of 12 hours,

- 4 days. Ans.

63. If 7 men mow 22 acres in 8 days, working 11 hours a day, in how many days, working 10 hours a day, will 11 men mow 360 acres?

7 men can mow 22 acres in 8 days of 11 hours - 88 hours,

I man can mow 22 acres in 7 × 88 hours.

1 man can mow 1 acre in  $\frac{7 \times 88}{22}$  hours.

12 men can mow 1 acre in  $\frac{7 \times 88}{12 \times 22}$  hours.

12 men can mow 360 acres in  $\frac{360 \times 7 \times 88}{12 \times 22}$  hours.

12 men can mow 360 acres in  $\frac{360 \times 7 \times 88}{10 \times 12 \times 22}$  days of 10 hours, = 84 days. Ans.

64. If 44 cannon, firing 30 rounds an hour for 3 hours a day, consume 300 barrels of powder in 5 days, how long will 400 barrels last 66 cannon, firing 40 rounds an hour for 5 hours a day?

non firing 30 rounds for 3 hours consume 300 bbls in 5 days.

non firing 30 rounds for 1 hour consume 300 bbls. in 3 × 5 days.

non firing 1 round for 1 hour consume 300 bbls. in  $30 \times 3 \times 5$  days.

non firing 1 round for 1 hour consumes 300 bbls. in  $44 \times 30 \times 3 \times 5 \text{ days.}$ 

non firing 1 round for 1 hour consumes 1 bbl. in  $\frac{44 \times 30 \times 3 \times 5}{300}$  days.

66 cannon firing 1 round for 1 hour consume  $44 \times 30 \times 3 \times 5$ 

1 bbl. in 
$$\frac{44 \times 30 \times 3 \times 5}{300 \times 66}$$
 days.

66 cannon firing 40 rounds for 1 hour consume

1 bbl. in 
$$\frac{44 \times 30 \times 3 \times 5}{40 \times 300 \times 66}$$
 days.

66 cannon firing 40 rounds for 5 hours consume

1 bbl. in 
$$\frac{44 \times 30 \times 3 \times 5}{5 \times 40 \times 300 \times 66}$$
 days.

66 cannon firing 40 rounds for 5 hours consume

400 bbls. in 
$$\frac{400 \times 44 \times 30 \times 3 \times 5}{5 \times 40 \times 300 \times 66}$$
 days = 2 days. Ans.

65. How many times will a wheel 2‡ feet in circumference turn round in travelling over 12‡ yards?

The wheel revolves once in going 24 feet.

- :. it will turn around as many times in going 12 $\frac{4}{7}$  yds. = 38 $\frac{4}{7}$  ft. as 38 $\frac{4}{7}$  + 2 $\frac{4}{7}$  = 15. Ans.
- 66. How much ground will be travelled over by a wheel 13 yards in circumference, when it has made 4½ turns?

If the wheel turns once in going  $1\frac{3}{7}$  yds., in making  $4\frac{1}{2}$  turns it will go  $4\frac{1}{2}$  times  $1\frac{3}{7}$  yds.  $=6\frac{3}{7}$  yds. Ans.

67. Find the circumference of a wheel which makes 9 turns in travelling over 7½ yards.

If it makes 9 turns in going  $7\frac{1}{5}$  yds., it will go  $7\frac{1}{5}$  yds.  $+9 = \frac{4}{5}$  yd.  $= 2\frac{2}{5}$  ft. in making one turn.

- ... the circumference of the wheel is 23 feet. Ans.
- 68. If the circumference of a wheel be 47 of 1 yd. 11 ft., how many times will it turn in travelling 31 miles?

1 yd. 
$$1\frac{1}{8}$$
 ft. =  $1\frac{1\frac{1}{8}}{3}$  yds. =  $1\frac{3}{8}$  yds.  $3\frac{3}{7}$  mi. =  $3\frac{3}{7} \times 1760$  yds.

If the wheel makes 1 turn in going  $\frac{2}{7}$  of  $1\frac{3}{8}$  yds., it will make as many turns in going  $3\frac{3}{7} \times 1760$  yds. as  $\frac{3\frac{3}{7} \times 1760}{\frac{2}{7} \times \frac{1}{8}} = 1396\frac{4}{11}$ . Ans.

69. If the wheel of a locomotive be 31 times 5.52 feet in circumference, how many times does it turn in a minute, when the locomotive is running at the rate of 13.34 miles an hour?

 $5.52 - 5\frac{1}{2}$ , and  $13.34 - 13\frac{1}{2}$ .

If it is going at the rate of 13 $\frac{1}{60}$  miles per hour, it is going at the rate of  $\frac{13\frac{17}{60}}{60}$  miles per minute, or at the rate of  $\frac{13\frac{17}{60} \times 5280}{60}$  feet per minute.

If it turns once in going  $3\frac{1}{2} \times 5\frac{1}{2}\frac{1}{2}$  feet, it will turn as many times in going  $\frac{13\frac{17}{12} \times 5280}{60}$  feet as  $\frac{13\frac{17}{12} \times 5280}{60} + (3\frac{1}{2} \times 5\frac{1}{2}\frac{1}{2}) = 67\frac{1}{2}$ .

Ans.

70. A can run \$\frac{4}{80}\$ of a mile in \$\frac{2}{3}\$ of a minute, B can run \$\frac{4}{36}\$ of a mile in \$\frac{2}{3}\$ of a minute. Which is the fastest runner? and if he can run a certain distance in 3 min. 10 sec, how much longer will each of the others take to run the same distance?

If A can run  $\frac{4}{35}$  mi. in  $\frac{9}{3}$  min., to run a mile it will take him  $\frac{9}{3}$  min.  $+\frac{4}{35}=8\frac{1}{3}$  min.

If B can run  $\frac{5}{56}$  mi. in  $\frac{3}{4}$  min, to run a mile it will take him  $\frac{3}{4}$  min.  $+\frac{5}{56} = 7\frac{9}{15}$  min.

If C can run \(\frac{1}{13}\) mi. in \(\frac{1}{2}\) min., to run a mile it will take him \(\frac{1}{2}\)

stest runner.

2. = 31 min.

a certain distance in  $3\frac{1}{5}$  min., and a mile in  $6\frac{11}{15}$  listance is that part of a mile which  $3\frac{1}{5}$  is of  $6\frac{11}{15} = \frac{7}{15}$ .

1 a mile in  $8\frac{1}{5}$  min., he can run  $\frac{7}{15}$  mi. in  $\frac{7}{15}$  of  $8\frac{1}{5}$  min. = 3 min. 51 sec.

n it in 3 min 10 sec. ... it takes A 41 sec. longer than C. a mile in  $7\frac{7}{15}$  min., he can run  $\frac{7}{15}$  mi, in  $\frac{7}{15}$  of  $7\frac{7}{15}$   $\frac{18}{15} = 3$  min.  $29\frac{1}{15}$  sec.

ın ıt in 3 mm. 10 sec. ... it takes B 19 1 sec. longer

Find the amount of the	following b	ills:			
75 71	71.		<b>.</b>	37 00 1	
Mr. Richard	•		· ·	Nov. 23, 1	1880
	$T_{0}$	) John	Doe,	Dr.	
To 125 lbs. sugar	@ 10 cts.			.   \$12	50
" 1 bag coffee, 115 lb	_			. 36	80
	@ 62 cts.		• •	. 15	50
" 8 lbs. Japan tea	@ 92 cts.			. 7	36
" 28 lbs. crackers	@ 8 cts.			. 2	24
" 2 bbls. flour	<b>@</b> \$7.50			. 15	00
				\$89	40
•	Received Pag	yment,		•	_ =
			$J_{c}$	ohn Doe.	
	72.				
Mr. James	Hardy,		Boston,	Feb. 29,	<b>L888</b>
	To (	C. H.	Mills,	Dr.	
To 275 bbls. flour @		· · · · · · · · · · · · · · · · · · ·		. \$1856	25
" 324 bbls. flour @	_	• • •	• •	. 2025	00
" 300 bu. potatoes @		• • •		. 144	1
	32 cts	• •	• •	504	96
" 2000 bbls. apples @			• •	2500	00
" 1 car-load oats,	-		hai	.   2000	
	42 cts		•	. 262	50
" 1 car-load corn, 2				. 202	
· _ ·	55 cts		, , , , , , , , , , , , , , , , , , ,	. 280	65
•		• •	• •	<u> </u>	1
	Paginal Pag	um am f		<b>\$7</b> 573	36
•	Received Pag	yment,	C. I	T. Mills.	
	73.		· · -		
James Harl	_		Boston	, Jan. 1, 1	1888
e who like	·	Tohn	Pike,	_	
			<u> </u>	<i>D</i> 1.	
To 12 bales Texas cotton			•	\$532	80
" 7 bales upland cotto		_	•	. 360	19
" 3 bales low middling	7, 1476 lbs.	<b>@</b> 9	§ cts	.   143	91
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Received Payment,

8 bales good ordinary, 9220 lbs. @ 9 cts...

John Pike.

793 | 80

70

**\$**1830

#### EXERCISE LIX.

- 1. What length of board 15 in. wide will contain 11 sq. ft. 36 sq. in.?
- 11 sq. ft. 36 sq. in. =  $11\frac{1}{4}$  sq. ft. 15 in. =  $1\frac{1}{4}$  ft.  $11\frac{1}{4} + 1\frac{1}{4} = 9$  ft. Ans.
- 2. What length of road 44 ft. wide will contain an acre?

1 A. = 160 sq. rds. 44 ft. =  $2\frac{3}{4}$  rds. 160 +  $2\frac{3}{4}$  = 60 rds. Ans.

3. Find the area of a rectangular field 13.12 chains long, 10.35 chains broad.

13.12 ch. × 10.35 ch. 10)135.792 sq. ch. 13 A. 5.792 sq. ch. Ans.

4. A path 216 ft. long measured 72 sq. yds. Find its breadth.

72 sq. yds. = 648 sq. ft. 648 + 216 = 3 ft. Ans.

5. A rectangular field of 21.66 acres is 250.8 yds. broad. Find its length.

1 A. = 4840 sq. yds.  $\frac{4840 \times 21.66}{250.8} = 418 \text{ yds. } Ans.$ 

6. What is the area of a table if length and breadth be 4 ft. 3\frac{3}{2} in. and 2 ft. 9\frac{3}{2} in., respectively?

4 ft. 3\frac{2}{7} in. = 4\frac{2}{7} ft. 2 ft. 9\frac{2}{7} in. = 2\frac{2}{7} ft. 4\frac{2}{7} \times 2\frac{4}{7} = 12 sq. ft. Ans.

7. From each corner of a square, the side of which is 2 ft. 5 in., a square measuring 5 in. on a side is cut out. Find the area of the remainder of the figure.

2 ft. 5 in. =  $2\frac{5}{12}$  ft.  $2\frac{5}{12} \times 2\frac{5}{12} = 5\frac{21}{12}$  sq. ft. = 5 sq. ft. 121 sq. in.  $5 \times 5 = 25$  sq. in. 25 sq. in.  $\times 4 = 100$  sq. in. 5 sq. ft. 121 sq. in. = 100 sq. in. = 5 sq. ft. 21 sq. in. Ans.

8. The length and breadth of a map are  $4\frac{1}{2}$  ft. and  $3\frac{1}{2}$  ft., respectively. If the map represent 77,760 sq. mi. of country, how many miles are there to a square inch?

 $4\frac{1}{4} \times 3\frac{1}{3} = 15$  sq. ft. = 2160 sq. in.  $77,760 \div 2160 = 36$  sq. mi. Ans.

9. In rolling a grass plot 24 yds. long and containing 400 sq. yds., how many times must a roller 3 ft. 4 in. wide be drawn

over it lengthwise so that the whole may be rolled?

$$400 \div 24 = 16\frac{3}{3}$$
 yds.  
3 ft. 4 in. =  $3\frac{1}{3}$  ft. =  $1\frac{1}{3}$  sq. yds.  
 $16\frac{2}{3} \div 1\frac{1}{3} = 15$ . Ans.

10. How many sods, each 2

ft. 3½ in. long and 8½ in. broad, would be required to turf an acre of ground?

2 ft. 
$$3\frac{1}{2}$$
 in. =  $27\frac{1}{2}$  in.  
1 A. =  $6,272,640$  sq. in.  
 $\frac{6272640}{27\frac{1}{2} \times 8\frac{1}{2}} = 27,648$ . Ans.

11. Find the area of a picture-frame 2½ in. broad and having an outside measurement of 4 ft. 6½ in. in length and 2 ft. 8 in. in width.

$$2\frac{1}{2} \text{ in. } \times 2 = 4\frac{1}{2} \text{ in.}$$

$$4 \text{ ft. } 6\frac{1}{2} \text{ in. } -4\frac{1}{2} \text{ in. } = 4 \text{ ft. } 2 \text{ in.}$$

$$4 \text{ ft. } 2 \text{ in. } +2 \text{ ft. } 8 \text{ in. } = 6 \text{ ft. } 10 \text{ in.}$$

$$6 \text{ ft. } 10 \text{ in. } \times 2 = 13 \text{ ft. } 8 \text{ in. } = 13\frac{3}{3} \text{ ft.}$$

$$2\frac{1}{4} \text{ in. } = \frac{3}{16} \text{ ft.}$$

$$13\frac{2}{3} \times \frac{3}{16} = \frac{41}{3} \times \frac{3}{16} = \frac{41}{16} = 2\frac{9}{16} \text{ sq. ft.}$$

$$2\frac{9}{16} \text{ sq. ft. } = 2 \text{ sq. ft. } 81 \text{ sq. in. } Ans.$$

12. Find the expense of glazing four windows, each containing 12 panes, the panes being each a foot long and 10 in. wide, and the price of the glass 38 cents per square foot.

10 in. = 
$$\frac{5}{6}$$
 ft.  
1 ×  $\frac{5}{6}$  =  $\frac{5}{6}$  sq. ft.  
2 12 ×  $\frac{5}{6}$  = 10 sq. ft.  
10 sq. ft. × 4 = 40 sq. ft.  
40 × \$0.38 = \$15.20. Ans.

13. A garden 76 yds. long and 56 yds. broad, enclosed by a wall, has a border 4 ft. wide within the wall, and within this a path 5 ft. wide, the middle being grass. Find the areas of the border, path, and grass, respectively.

4 ft. = 
$$1\frac{1}{3}$$
 yds.  $2 \times 1\frac{1}{3}$  yds. =  $2\frac{2}{3}$  yds.  
76 yds. -  $2\frac{2}{3}$  yds. =  $73\frac{1}{3}$  yds.  
73 $\frac{1}{3}$  yds. + 56 yds. =  $129\frac{1}{3}$  yds.  
129 $\frac{1}{3}$  yds.  $\times 2 = 258\frac{2}{3}$  yds. = perimeter.  
258 $\frac{2}{3} \times 1\frac{1}{3} = \frac{776}{3} \times \frac{4}{3} = \frac{8104}{9} = 341\frac{8}{3}$  sq. yds. (1) Ans.

76 yds.			
17	1	731	
Į	1	70	
F_	[		7
56	53		
	╽┟		- 1
		** ** *	

5 ft. + 4 ft. = 9 ft. = 3 yds.  
76 yds. = 
$$(2 \times 3 \text{ yds.}) = 70 \text{ yds.}$$
  
56 yds. =  $(2 \times 3 \text{ yds.}) = 50 \text{ yds.}$   
 $70 \times 50 = 3500 \text{ sq. yds.}$  (3) Ans.

14. Find the area of a circle which has a radius of 3 ft.

15. What is the area of a curcular field with a radius of 400 vards?

ius of the rotunda n at Rome is 71 ft. s area of the floor.

n. = 
$$71\frac{1}{2}$$
 ft.  
 $1\frac{1}{2}$  =  $5112\frac{1}{2}$  sq. ft.  
 $1416$   
 $5112\frac{1}{2}$  sq. ft.  
 $6446$  sq. ft. Ans.

17. The diameter of a cistern is 13 ft. What is the area of the bottom?

18. The two dials of the clock of St. Paul's, London, are each 184 feet in diameter. What is the area of each in square feet?

18 
$$\frac{1}{1}$$
 ft. + 2 = 9  $\frac{1}{14}$  ft.  
9  $\frac{1}{14}$  × 9  $\frac{1}{14}$  = 82  $\frac{1}{196}$  sq. ft.  
3.1416  
× 82  $\frac{1}{196}$  sq. ft.  
258 5248 sq. ft. Ans.

19. How many square inches on the surface of a ball 3 in. in diameter?

$$3 \times 3 = 9$$
 sq. in.  
 $3.1416$   
 $\times 9$  sq. in.  
 $28.2744$  sq. in. Ans.

20. How many square inches of surface in a spherical black-board 12 in. in diameter?

$$12 \times 12 = 144$$
 sq. in.  
 $3.1416$   
 $\times 144$  sq. in.  
 $452.3994$  sq. in.

21. What is the interior surface of a hemispherical vase 20 in. in diameter?

$$20 \times 20 = 400 \text{ sq. in.}$$
  
 $400 \text{ sq. in.} + 2 = 200 \text{ sq. in.}$   
 $3.1416$   
 $\times 200 \text{ sq. in.}$   
 $628.32 \text{ sq. in.}$   
 $= 4 \text{ sq. ft. } 52.32 \text{ sq. in.}$ 

22. How many yards of carpeting \( \frac{2}{2} \) of a yard wide will be required for a floor 26 ft. long, 15\( \frac{3}{2} \) ft. wide, if the strips run lengthwise? How many if the strips run across the room? How much will be turned under in each case?

23. How many yards  $\frac{7}{8}$  of a yard wide will be required for a room  $8\frac{1}{2}$  yds. long and 17 ft. wide, if the strips run lengthwise, and there is a waste of  $\frac{1}{16}$  of a yard in each strip, in matching patterns?

17 ft. = 
$$5\frac{2}{3}$$
 yds.  
 $5\frac{2}{3} + \frac{7}{8} = 6\frac{1}{2}\frac{9}{1} = 7$  strips.  
 $7 \times \frac{1}{16}$  yd. =  $\frac{7}{16}$  yd.  
 $7 \times 8\frac{1}{2}$  yds. =  $59\frac{1}{2}$  yds.  
 $59\frac{1}{2}$  yds. +  $\frac{7}{16}$  yds.  
=  $59\frac{1}{6}$  yds. Ans.

24. How many square yards of oil-cloth will be required for a hall floor 5½ yds. long and 10 ft. wide?

10 ft. = 
$$3\frac{1}{3}$$
 yds.  
 $5\frac{1}{4} \times 3\frac{1}{3} = 17\frac{1}{2}$  sq. yds. Ans.

25. What will be the cost of carpet \( \frac{5}{4} \) of a yard wide for a room  $28\frac{1}{2}$  ft. by  $18\frac{3}{4}$  ft., if the strips run lengthwise, and the cost per yard is 92 cents?

26. Find the cost of carpet 30 in. wide, at \$1.25 per yd. for a room 18 ft. by 14 ft., if the strips run lengthwise; if the strips run across the room.

30 in. =  $\frac{5}{6}$  yd. 18 ft. = 6 yds. 14 ft. =  $\frac{42}{3}$  yds.  $\frac{42}{3} + \frac{5}{6} = \frac{52}{5} = 6$  strips.  $6 \times 6$  yds. = 36 yds.  $36 \times 11 = 45$ . Ans.  $6 + \frac{5}{6} = 71 = 8$  strips.  $8 \times 4\frac{2}{3} \times 11 = 46\frac{2}{3}$ = 46.67. Ans.

27: Find the cost of carpeting 27 inches wide, at \$1.12½ per yard, for a room 29 ft. 9 in. by 23 ft. 6 in., if the strips run across the room.

27 in. =  $\frac{8}{4}$  yd. 29 ft. 9 in. = 29 $\frac{5}{4}$  ft. =  $9\frac{11}{12}$  yds. 23 ft. 6 in. =  $23\frac{1}{3}$  ft. =  $7\frac{5}{6}$  yds.  $9\frac{11}{12} + \frac{8}{4} = 13\frac{2}{6}$ .  $14 \times 7\frac{5}{6} = 109\frac{2}{3}$  yds. = 14 strips.  $109\frac{2}{3} \times $1.125 = $123.38$ . Ans.

28. Find the cost of carpeting \$\frac{1}{4}\$ of a yard wide, at \$2.75 per yard, for a room 34 ft. 8 in. by 13 ft. 3 in., if the strips run lengthwise, and if there be a waste of \$\frac{1}{4}\$ of a yard on each strip in matching the pattern.

34 ft. 8 in. =  $34\frac{2}{3}$  ft. =  $11\frac{5}{9}$  yds. 13 ft. 3 in. =  $13\frac{1}{4}$  ft. =  $4\frac{5}{12}$  yds.  $4\frac{5}{12} \div \frac{3}{4} = 5\frac{8}{9} = 6$  strips.  $6 \times 11\frac{5}{9} = 69\frac{1}{3}$  yds.  $6 \times \frac{1}{4}$  yd. =  $1\frac{1}{2}$  yds. waste.  $69\frac{1}{3} + 1\frac{1}{2} = 70\frac{5}{6}$  yds.  $70\frac{5}{6} \times \$2.75 = \$194.79$ . Ans.

29. Which way must the strips of carpet 2 of a yard wide

run in order to carpet most economically a room 20 ft. 6 in. long and 19 ft. 6 in. wide, if there be no waste for matching the pattern?

20 ft. 6 in. =  $20\frac{1}{2}$  ft. =  $6\frac{5}{6}$  yds. 19 ft. 6 in. =  $19\frac{1}{2}$  ft. =  $6\frac{1}{2}$  yds.  $6\frac{1}{2} \div \frac{3}{4} = 8\frac{2}{3} = 9$  strips.  $9 \times 6\frac{5}{6} = 61\frac{1}{2}$  yds. lengthwise.  $6\frac{5}{6} \div \frac{3}{4} = 9\frac{1}{9} = 10$  strips.  $10 \times 6\frac{1}{2} = 65$  yds. across.  $\therefore$  the strips must run lengthwise.

30. Find the number of yards of plastering in the walls of a room 21\frac{3}{4} ft. long, 16\frac{1}{2} ft. wide, and 11 ft. high, if 12 sq. yds. be allowed for doors, windows, and base-boards.

 $21\frac{3}{4} + 16\frac{1}{2} = 38\frac{1}{4}$  ft.  $2 \times 38\frac{1}{4}$  ft.  $= 76\frac{1}{2}$  ft.  $76\frac{1}{2} \times 11 = 841\frac{1}{3}$  sq. ft.  $= 93\frac{1}{2}$  sq. yds.  $93\frac{1}{2}$  sq. yds.  $= 81\frac{1}{2}$  sq. yds. Ans.  $= 81\frac{1}{2}$  sq. yds. Ans.

31. How many square yards of plastering in the walls and ceiling of a room 20 ft. 8 in. long, 26 ft. 5 in. wide, 10 ft. 6 in. high, if 24 sq. yds. be allowed for doors, windows, and base-boards?

30 ft. 8 in. =  $30\frac{2}{3}$  ft. 26 ft. 5 in. =  $26\frac{5}{12}$  ft.  $30\frac{2}{3} + 26\frac{5}{12} = 57\frac{1}{12}$  ft.  $2 \times 57\frac{1}{12} = 114\frac{1}{6}$  ft.  $114\frac{1}{6} \times 10\frac{1}{2} = 133\frac{7}{36}$  sq. yds.  $30\frac{2}{3} \times 26\frac{5}{12} = 90\frac{1}{81}$  sq. yds.  $133\frac{7}{36} + 90\frac{1}{81} = 223\frac{67}{324}$ .  $223\frac{67}{324} - 24 = 199\frac{67}{324}$  sq. yds. Ans. 32. What will be the cost of plastering the walls and ceiling of a room 27 ft. 4 in. long, 20 ft. wide, and 12 ft. 6 in. high, at 27 cents per square yard, if 20 sq. yds. be deducted for doors, windows, and base-board?

27 ft. 4 in. = 
$$27\frac{1}{3}$$
 ft. =  $9\frac{1}{9}$  yds.  
20 ft. =  $6\frac{2}{3}$  yds.  
12 ft. 6 in. =  $12\frac{1}{2}$  ft. =  $4\frac{1}{6}$  yds.  
 $9\frac{1}{9} + 6\frac{2}{8} = 15\frac{7}{9}$  yds.  
 $2 \times 15\frac{7}{9} = 31\frac{5}{9}$  yds.  
 $31\frac{5}{9} \times 4\frac{1}{6} = 131\frac{1}{2}\frac{3}{7}$  sq. yds.  
 $9\frac{1}{9} \times 6\frac{2}{3} = 60\frac{2}{9}$  sq. yds.  
 $131\frac{1}{2}\frac{3}{7} \times 60\frac{2}{9} = 192\frac{2}{9}$  sq. yds.  
 $192\frac{2}{9} - 20 = 172\frac{2}{9}$  sq. yds.  
 $172\frac{2}{9} \times 90.27 = 946.50$ . Ans.

33. Find the cost of whitening the ceiling and walls of a room 14 ft. 4 in. wide, 15 ft. 6 in. long, 10 ft. 6 in. high, at 5 cents per square yard, allowing 9 sq. yds. for doors and windows.

14 ft. 4 in. = 
$$14\frac{1}{3}$$
 ft. =  $4\frac{7}{3}$  yds.  
15 ft. 6 in. =  $15\frac{1}{2}$  ft. =  $5\frac{1}{3}$  yds.  
10 ft. 6 in. =  $10\frac{1}{3}$  ft. =  $3\frac{1}{2}$  yds.

$$4\frac{7}{9} + 5\frac{1}{6} = 9\frac{1}{18}$$
 yds.  
 $2 \times 9\frac{1}{18} = 19\frac{8}{9}$  yds.  
 $19\frac{8}{9} \times 3\frac{1}{2} = 69\frac{1}{18}$  sq. yds.  
 $4\frac{7}{9} \times 5\frac{1}{6} = 24\frac{8}{5}\frac{7}{4}$  sq. yds.  
 $69\frac{1}{18} + 24\frac{8}{5}\frac{7}{4} = 94\frac{8}{27}$  sq. yds.  
 $94\frac{8}{27} - 9 = 85\frac{8}{27}$  sq. yds.  
 $85\frac{8}{27} \times \$0.05 = \$4.26$ . Ans.

34. Find the cost of plastering a room 21 ft. long, 15 ft. wide, 12 ft. high, at 40 cents per square yard, allowing for a door 7 ft. high, 3 ft. wide; 3 windows, each 5 ft. high, 3 ft. wide; and a dado 2 ft. 9 in. high around the room.

$$21 + 15 = 36$$
 ft.  
 $2 \times 36$  ft. = 72 ft.  
 $72 \times 12 = 1179$  sq. ft.  
 $3 \times 7 = 21$  sq. ft. door.  
 $5 \times 3 \times 3 = 45$  sq. ft. windows.  
 $2\frac{3}{4} \times 72 = 198$  sq. ft. dado.  
 $21 + 45 + 198 = 264$  sq. ft.  
 $1179 - 264 = 915$  sq. ft.  
 $915$  sq. ft. =  $101\frac{2}{3}$  sq. yds.  
 $101\frac{2}{3} \times 90.40 = 940.67$ . Ans.

35. Find the cost of papering a room 20 ft. 6 in. long, 17 ft. 4 in. wide, 9 ft. high, with paper 18 in. wide, 8 yards in a roll, at 75 cents a roll; allowing for 2 doors, each 7 ft. high, 3 ft. wide, and for 3 windows, each 5 ft. 6 in. high and 3 ft. 3 in. wide.

20 ft. 6 in. = 
$$20\frac{1}{2}$$
 ft. =  $6\frac{5}{6}$  yds.  
17 ft. 4 in. =  $17\frac{1}{3}$  ft. =  $5\frac{7}{6}$  yds.  
9 ft. = 3 yds.  
 $6\frac{5}{6} + 5\frac{7}{6} = 12\frac{1}{18}$  yds.  $2 \times 12\frac{1}{18} = 25\frac{7}{6}$ .  
 $25\frac{7}{6} \times 3 = 75\frac{7}{3}$  sq. yds.  
 $2 \times 7 \times 3 = 42$  sq. ft. =  $4\frac{7}{3}$  sq. yds. doors.

$$3 \times 5\frac{1}{2} \times 3\frac{1}{4} = 53\frac{4}{5}$$
 sq. ft. =  $5\frac{1}{2}\frac{4}{5}$  sq. yds. windows.  
 $4\frac{1}{4} + 5\frac{1}{2}\frac{3}{4} = 10\frac{4}{5}$  sq. yds.  
 $75\frac{1}{3} - 10\frac{4}{5} = 65\frac{1}{2}\frac{1}{4}$  sq. yds.  
 $18$  in. =  $\frac{1}{4}$  yd.  $8 \times \frac{1}{4} = 4$  sq. yds.  
 $65\frac{1}{2}\frac{1}{4} + 4 = 16\frac{1}{2}\frac{1}{5} = 17$  rolls.  
 $17 \times 90.75 = 912.75$ . Ans.

36. Find the cost of papering a room 32 ft. long, 22 ft. wide, 13 ft. high, with paper 18 in. wide, 8 yards in a roll, at \$1.25 a roll, if 50 sq. yds. be allowed for doors, windows, and base-board.

$$32 + 22 = 54$$
 ft.  $2 \times 54 = 108$  ft.  
 $108 \times 13 = 1404$  sq. ft. = 156 sq. yds.  
 $156 - 50 = 106$  sq. yds.  
 $18$  in. =  $\frac{1}{2}$  yd.  $8 \times \frac{1}{2} = 4$  sq. yds.  
 $106 + 4 = 26\frac{1}{2} = 27$  rolls.  
 $27 \times \$1.25 = \$33.75$ . Ans.

87. Find the cost of papering a room 26 ft. long, 21 ft. wide, 12 ft. high, with paper 20 in. wide, 8 yards in a roll, at \$1.50 a roll, and a border at 25 cents per running foot; allowing for a fire-place 5 ft. 3 in. by 4 ft., a door 7 ft. by 4½ ft., and 3 windows, each 6 ft. by 3½ ft.

26 ft. = 
$$8\frac{1}{2}$$
 yds. 21 ft. = 7 yds. 12 ft. = 4 yds.  $8\frac{1}{4} + 7 = 15\frac{2}{3}$  yds.  $2 \times 15\frac{1}{4} = 31\frac{1}{4}$  yds.  $31\frac{1}{2} \times 4 = 125\frac{1}{4}$  sq. yds. 5 ft. 3 in. =  $5\frac{1}{4}$  ft.  $5\frac{1}{4} \times 4 = 21$  sq. ft. =  $2\frac{1}{4}$  sq. yds. fire-place.  $7 \times 4\frac{1}{2} = 31\frac{1}{4}$  sq. ft. =  $3\frac{1}{4}$  sq. yds. door.  $3 \times 6 \times 3\frac{1}{4} = 63$  sq. ft. =  $7$  sq. yds. windows.  $12\frac{1}{4}$  sq. yds. to be deducted.  $125\frac{1}{4} - 12\frac{1}{4} = 112\frac{1}{4}$  sq. yds.  $20$  in. =  $\frac{1}{4}$  yd.  $8 \times \frac{1}{4} = 4\frac{1}{4}$  sq. yds.  $112\frac{1}{4} + 4\frac{1}{4} = 25\frac{1}{16} = 26$  rolls.  $26 \times \frac{1}{4} \cdot 150 = \frac{3}{4} \cdot 39.00$ . Perimeter =  $31\frac{1}{4}$  yds. =  $94$  ft.  $94 \times \frac{1}{4} \cdot 0.25 = \frac{3}{4} \cdot 23.50$ .

39.00 + \$23.50 = \$62.50. Ans.

How many feet board measure in:

38. A board 18 ft. long, 9 in. wide, 7 in. thick?

A board 16 ft. long, 11 in. wide, 1 in. thick?

9 in. = 
$$\frac{3}{4}$$
 ft.  
 $18 \times \frac{3}{4} = 13\frac{1}{2}$  ft. Ans.  
11 in. =  $\frac{1}{12}$  ft.  
 $16 \times \frac{1}{12} = 14\frac{2}{3}$  ft. Ans.

39. Twenty boards averaging 14 ft. long, 10 in. wide, ½ in. thick?

10 in. 
$$= \frac{5}{6}$$
 ft.

$$\frac{\frac{7}{14}}{1} \times \frac{5}{6} \times \frac{20}{1} = \frac{700}{3} = 233\frac{1}{3} \text{ ft. } Ans.$$

40. Three joists 13 ft. long, 8 in. wide, 3 in. thick?

8 in. = 
$$\frac{2}{8}$$
 ft.  
Hence 1 joist = 3 boards 13 by  $\frac{2}{8}$ .  
 $\frac{13}{1} \times \frac{2}{3} \times \frac{3}{1} \times \frac{3}{1} = 78$  ft. Ans.

41. A stick of timber 8 in. by 9 in. and 27 ft. long?

$$8 \text{ in.} = \frac{2}{3} \text{ ft.}$$

Hence 1 stick = 9 boards 27 ft. by 3 ft.

$$\frac{9}{27} \times \frac{2}{3} \times \frac{9}{1} = 162 \text{ ft. } Ans.$$

42. Two beams, each 6 in. by 9 in. and 23 ft. long?

6 in. = 
$$\frac{1}{2}$$
 ft.

Hence 1 beam = 9 boards 23 ft. by  $\frac{1}{2}$  ft.

$$\frac{23}{1} \times \frac{1}{2} \times \frac{9}{1} \times \frac{2}{1} = 207 \text{ ft. Ans.}$$

48. Three joists, each 3 in, by 4 in, and 11 ft. long?

3 in. = 
$$\frac{1}{4}$$
 ft.  
Hence 1 joiét = 4 boards 11 ft. by  $\frac{1}{4}$  ft.  
 $\frac{11}{1} \times \frac{1}{4} \times \frac{4}{1} \times \frac{3}{1} = 33$  ft. Áns.

44. Five joists, each 6 in. by 4 in. and 14 ft. long?

6 in. = 
$$\frac{1}{2}$$
 ft.  
Hence I joint = 4 boards 14 ft. by  $\frac{1}{2}$  ft.  
 $\frac{14}{1} \times \frac{1}{2} \times \frac{4}{1} \times \frac{5}{1} = 140$  ft. Ans.

45. A stick of timber 10 in. square and 36 ft. long?

10 in. = 
$$\frac{5}{6}$$
 ft.  
Hence 1 stick = 10 boards 36 ft. by  $\frac{5}{6}$  ft.  

$$\frac{6}{1} \times \frac{5}{9} \times \frac{10}{1} = 300$$
 ft. Ans.

Ten planks, each 13 ft. long, 15 in. wide, 2 in. thick?

15 in. = 
$$\frac{5}{4}$$
 ft.  
Hence 1 plank = 2 boards 13 ft. by  $\frac{4}{4}$  ft.  
 $\frac{13}{1} \times \frac{5}{4} \times \frac{2}{1} \times \frac{10}{1} = 325$  ft. Ans.

d the cost of:

Nine joists, each 15 ft. long, 31 in. by 5 in., at \$12 per M.

5 in. = 
$$\frac{4}{12}$$
 ft. \$12 per M. =  $\frac{$12}{1000}$  per sq. ft.  
Hence 1 joist =  $3\frac{1}{2}$  boards 15 ft. by  $\frac{4}{12}$  ft.  
 $15 \times \frac{7}{2} \times \frac{5}{12} \times 9 \times \frac{$12}{1000} = \frac{$169}{80} = $2.36$ . Ans.

48. Thirty planks, each 12 ft. long, 11 in. wide, 3 in. thick, at \$15 per M.

11 in. = 
$$\frac{11}{12}$$
 ft. \$15 per M. =  $\frac{$15}{1000}$  per sq. ft.  
Hence 1 plank = 3 boards 12 ft. by  $\frac{11}{12}$  ft.  
 $12 \times \frac{11}{12} \times 3 \times 30 \times \frac{$15}{1000} = \frac{$297}{20} = $14.85$ . Ans.

49. Four sticks of timber, each 8 in. by 9 in. and 23 ft. long, at \$18 per M.

9 in. = 
$$\frac{2}{4}$$
 ft. \$18 per M. =  $\frac{\$18}{1000}$  per sq. ft.  
Hence 1 stick = 8 boards 23 ft. by  $\frac{2}{4}$  ft.  
 $\frac{23}{1} \times \frac{3}{4} \times \frac{8}{1} \times \frac{4}{1} \times \frac{\$18}{1000} = \frac{\$1242}{125} = \$9.94$ . Ans.

50. A board 24 ft. long, 23 in. wide at one end and 17 in. at the other, and 11 in. thick, at \$30 per M.

$$\frac{23 + 17}{2} = 20 \text{ in. average width.}$$

$$20 \text{ in.} = 1\frac{2}{3} \text{ ft}$$

$$30 \text{ per M.} = \frac{\$30}{1000} \text{ per sq. ft.}$$
Hence the board =  $1\frac{1}{2}$  boards 24 ft. by  $1\frac{2}{3}$  ft.
$$24 \times \frac{5}{3} \times \frac{3}{2} \times \frac{\$30}{1000} = \frac{\$9}{5} = \$1.80. \text{ Ans.}$$

51. A stick of timber 29 ft. long, 10 in. by 12 in. at \$13.50 per M.

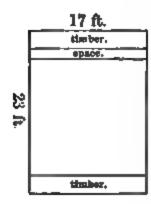
12 in. = 1 ft. \$13.50 per M. = 
$$\frac{\$13\frac{1}{2}}{1000} = \frac{\$27}{2000}$$
 per ft.  
Hence 1 stick = 10 boards 29 ft. by 1 ft.  
 $29 \times 10 \times 1 \times \frac{\$27}{2000} = \frac{\$783}{200} = \$3.92$ . Ans.

52. The flooring for two floors, each 23 ft. by 17 ft., each floor double, and of boards  $\frac{7}{4}$  in thick; the lower floor at \$18, and the upper at \$24, per M.

Boards ? in thick are reckoned as 1 in.

Hence each floor, being double, will require  $2 \times 23 \times 17 = 782$  sq. ft. Average cost per floor = \$21 per M.

- .. Average cost both floors \$42 per M.
- .. Whole cost =  $782 \times \frac{\$42}{1000} = \$32.84$ . Ans.
- 53. The flooring timbers for a room 23 ft. by 17 ft. at \$18 per M, if they are 2 in. by 10 in., 17 ft. long, and are placed on edge, two close to the walls, and the others with spaces of \$2 of a foot between them.



The room being 17 ft. wide and the timbers 17 ft. long, the timbers must run across the room. After a timber is placed against the wall at one end, the remaining distance to be occupied with timbers and spaces = 23 ft. -2 in. =  $22\frac{\pi}{2}$  ft. The distance occupied by a timber and a space  $-\frac{\pi}{4} + \frac{\pi}{4}\frac{\pi}{6} = \frac{1}{1}\frac{\pi}{10}$  ft.

 $\therefore$  22% +  $\frac{1}{1}$ % = number of timbers required for remaining space.

$$22\frac{5}{4} + \frac{137}{120} = \frac{137}{6} \times \frac{129}{137} = 20.$$

1 timber is supposed to have been placed.

 $\therefore$  20 + 1 = 21, the whole number of timbers required.

$$19 \times \frac{1}{9} \times 17 \times \frac{$19}{1009} = \frac{$51}{100} = $0.51$$
, cost of one timber.

- $\therefore$  21 × \$0.51 \$10.71, whole cost.
- A log 14 ft. long, 17 in. in diameter.

$$17^{2} - 2 \times 17 = 289 - 34 = 255$$
.  
21 of 14 of 255 = 187 ft. Ans.

. A log 11 ft, long, 13 in. in diameter.

$$13^{2} - 2 \times 13 = 169 - 26 = 143$$
.  
21 of 11 of 143 = 83 ft. Ans.

56. A log 16 ft. long, 20 in. in diameter.

$$20^{2}-2\times 20=400-40=360$$
.  
 $\frac{21}{16}$  of  $\frac{1}{16}$  of  $360=302$  ft. Ans.

57. A log 12 ft. long, 15 in. in diameter.

$$15^{2} - 2 \times 15 = 225 - 30 = 195$$
.  
 $\frac{21}{10}$  of  $\frac{12}{10}$  of  $195 = 123$  ft. Ans.

Find the value, at \$9 per M. of:

58. A log 17 ft. long, averaging 11 in. in diameter.

$$11^{2}-2\times 11=121-22=99.$$
  
 $\frac{21}{10}$  of  $\frac{17}{10}$  of  $99=88.3575$  ft.  
 $88.3575\times \$0.009=\$0.80$ . Ans.

59. A log 18 ft. long, averaging 13 in. in diameter.

$$13^2 - 2 \times 13 = 169 - 26 = 143$$
.  
 $\frac{21}{10}$  of  $\frac{18}{10}$  of  $143 = 135.135$  ft.  
 $135.135 \times \$0.009 = \$1.22$ . Ans.

60. A log 13 ft. long, 16 in. in diameter.

$$16^2 - 2 \times 16 = 256 - 32 = 224$$
.  
 $\frac{21}{10}$  of  $\frac{18}{10}$  of  $224 = 153$  ft.  
 $153 \times \$0.009 = \$1.38$ . Ans.

61. A log 14 ft. long, 12 in. in diameter.

1

$$12^{2}-2\times 12=144-24=120.$$
  
 $\frac{21}{10}$  of  $\frac{1}{10}$  of  $120=88$  ft.  
 $88\times \$0.009=\$0.79$ . Ans.

62. How many clapboards will be required to cover the front of a house 60 ft. long and 20 ft. high, if they are laid 4 in. to the weather, and if 120 sq. ft. be deducted for doors and windows?

$$60 \times 20 = 1200.$$
 $1200 - 120 = 1080.$ 
 $4 \times \frac{1}{3} = 1\frac{1}{3} \text{ sq. ft.}$ 
 $1080 + 1\frac{1}{3} = \frac{3}{4} \text{ of } 1080.$ 
 $= 810. \text{ Ans.}$ 

63. If one thousand shingles cover 120 sq. ft. of roof, what is the average width of a shingle?

$$\frac{130}{1605} = \frac{1}{25}$$
 sq. ft. =  $17\frac{7}{35}$  sq. in.  
 $\frac{1}{3}$  of 16 in =  $5\frac{1}{3}$  in.  
 $17\frac{7}{25} + 5\frac{1}{3} = 3\frac{7}{25}$  in. Ans.

64. Allowing one thousand shingles for 120 sq. ft., how many thousand will be required to cover the pitched roof of a house 60 ft. long, if the width of each side of the roof be 24½ ft.?

$$24\frac{1}{2} \times 60 = 1470$$
 sq. ft.  
 $1470 + 120 = 24\frac{1}{4}$ .  
 $24\frac{1}{4}$  thousand. Ans.

#### EXERCISE LX.

1. Find the volume of a rectangular solid whose length, breadth, and thickness are 7 ft., 2 ft. 6 m., and 11 in. respectively.

$$7 \times 2\frac{1}{2} \times \frac{11}{12} = 16\frac{1}{14}$$
 cu. ft.  
= 16 cu. ft. 72 cu. in. Ans.

2. How many cubic feet of air in a hall 54 ft. long, 33 ft. wide, 21 ft. 4 in. high?

$$54 \times 33 \times 21\frac{1}{3} = 38,016$$
 cu. ft.

Ans

3. Find the volume of a cube whose edge is 2½ yds.

2½ × 2½ = 15½ cu. yds. = 15 cu. yds. 16 cu. ft. .512 cu. m. Ans.

cellar is dug 21 ft. long, in. wide, 9 ft. deep. How ubic yards of earth are ut?

$$\frac{1 \times 9}{1} = 1204$$
 cu. yds. Ans.

5. How many cubic feet of water does a cistern hold whose length, breadth, and height are 5 ft. 4 in., 3 ft. 6 in., 2 ft. 10 m., respectively?

$$5\frac{1}{4} \times 3\frac{1}{4} \times 2\frac{5}{2} = 52\frac{5}{4}$$
 cu. ft. Am.

6. If the dimensions of a brick be 8 in by 3½ in. by 2½ in., find its volume.

$$8 \times 31 \times 21 = 63$$
 cu. in. Ans.

7. In a bar of iron 21 ft long, 3 in. wide, 2 in. thick, how many cubic inches are there?

21 ft. = 252 in.  

$$252 \times 3 \times 2 = 1512$$
 cu. in Ans.

8. What is the value of a bar of gold 8 in. long and 4 of an inch square, at \$190 a cubic inch?

9. A reservoir whose length and breadth are 15 yds. and 12 yds., respectively, holds 330 cu. yds. of water. What is its depth?

$$\frac{330}{15 \times 12} = 1\frac{5}{8}$$
 yds. Ans.

10. What length must be cut off a beam 9 in. by 15 in. to contain  $2\frac{1}{2}$  cu. ft.?

$$\frac{\frac{2\frac{1}{2}}{\frac{3}{4} \text{ of } \frac{5}{4}}}{= 2 \text{ ft. 8 in. } Ans.}$$

11. How high should a room be made, if its length be 31 ft. 3 in. and breadth 24 ft., in order that it may contain 10,000 cu. ft. of air?

$$\frac{10000}{31\frac{1}{4}\times24}=13\frac{1}{3} \text{ ft. } Ans.$$

12. A piece of wood 5 ft. long, 1 ft. broad, and 9 in. thick, is cut up into matches 2½ in. long and 0.1 of an inch square. How many will there be if no allowance be made for waste in cutting?

5 ft. = 60 in.; 1 ft. = 12 in.  

$$\frac{60 \times 12 \times 9}{2\frac{1}{4} \times \frac{1}{10} \times \frac{1}{10}} = 259,200. \text{ Ans.}$$

13. How long a wall 6 ft. high, 12\frac{3}{4} in. thick, could be built with the bricks forming a pile 17 ft. 6 in. long, 5 ft. wide, 4 ft. 3 in. high?

$$\frac{12\frac{3}{4} \text{ in.} = 1\frac{1}{16} \text{ ft.}}{\frac{17\frac{1}{2} \times 5 \times 4\frac{1}{2}}{6 \times 1\frac{1}{16}} = 58\frac{1}{3} \text{ ft. } Ans.}$$

14. Find the surface of a cube whose edge is 3 ft. 53 in.

$$5\frac{2}{3}$$
 in.  $=\frac{17}{36}$  ft.  
 $3\frac{17}{36} \times 3\frac{17}{36} \times 6 = 72\frac{78}{216}$  sq. ft.  
 $= 72$  sq. ft.  $48\frac{2}{3}$  sq. in. Ans.

15. Find the surface of a rectangular block of stone 4 ft. long, 2½ ft. broad, 1½ ft. thick.

$$4 \times 2\frac{1}{2} \times 2 = 20.$$
 $2\frac{1}{2} \times 1\frac{1}{4} \times 2 = 6\frac{1}{4}.$ 
 $4 \times 1\frac{1}{4} \times 2 = 10.$ 
 $20 + 6\frac{1}{4} + 10 = 36\frac{1}{4} \text{ sq. ft.}$ 
 $= 36 \text{ sq. ft. } 36 \text{ sq. in. } Ans.$ 

16. A lake whose area is 45 A. is covered with ice 3 in. thick. Find the weight of the ice in tons, if a cubic foot weigh 920 oz. avoirdupois.

1 A. = 43,560 sq. ft.  
43560  

$$\times$$
 45  
1960200 sq. ft.  
3 in. =  $\frac{1}{4}$  ft.  
4)1960200  
490050 cu. ft.  
 $\times$  920  
 $\overline{450846000}$   
32,000 oz. = 1 t.  
14088 $\frac{1}{8}$  t. Ans.  
32)450846

17. How many bricks will be required to build a wall 75 ft. long, 8 ft. high, and 16 in. thick, each brick being 8 in. long, 4 in. wide, 2} in. thick?

$$\frac{75\times6\times11}{1\times1\times1}=14,400. \text{ Ans.}$$

18. Find the cost of making a road 110 yds. in length and 18 ft. wide, the soil being first removed to the depth of 1 ft. at a cost of 25 cents a cubic yard; rubble being then laid 8 in. deep, at 25 cents a cubic yard, and gravel placed on top 9 in. thick, at 62 cents a cubic yard.

18 ft. = 6 yds.  

$$\frac{110}{1} \times \frac{6}{1} \times \frac{1}{3} \times \frac{$25}{100} = $55.$$
8 in. =  $\frac{1}{3}$  yd.  

$$\times \frac{2}{9} \times \frac{$25}{100} = $36\frac{1}{3}.$$
9 in. =  $\frac{1}{4}$  yd.  

$$\times \frac{1}{4} \times \frac{$625}{1000} = $103\frac{1}{3}.$$
Whole cost =  $$194.79$ .

room whose length is eadth 24 ft., height 10 ave its ceiling raised so ease the space by 84 cu. nat will then be its

27 ft. = 9 yds.  
24 ft. = 8 yds.  
$$\frac{84}{9 \times 8} = 1\frac{1}{8} \text{ yds.} = 3\frac{1}{4} \text{ ft.}$$

$$10 + 3\frac{1}{2} = 13\frac{1}{2}$$
 ft. Ans.

20. A block of wood 5 ft. 4.8 m. long, 1 ft. 9 in. wide and thick, weighs 7.56 cwt. Determine the weight, in pounds, of a cubic foot.

5 ft. 4.8 in. = 5
$$\frac{1}{5}$$
 ft.  
7.56 cwt. = 756 lbs.  
$$\frac{756}{54 \times 14 \times 14} = 454$$
 lbs. Ans.

21. How many cords in a pile of wood 40 ft. long, 4 ft. wide, 5 ft. 4 m. high?

$$\frac{40\times4\times51}{8\times4\times4}=61. \text{ Ans.}$$

22. A pile of wood containing 67} cords is 270 ft. long and 4 ft. wide. How high is it?

$$\frac{671 \times 128}{270 \times 4} = 8 \text{ ft. Are.}$$

23. What will be the cost of a pile of wood 25 ft. long, 4 ft. wide, 4 ft. 8 in. high, at \$3.75 a cord?

$$\frac{25 \times 4 \times 43 \times 833}{128} = $13.67. Ans.$$

24. What must be the length of a load of wood 3½ ft. high and 5 ft. wide, to contain a cord?

$$\frac{128}{5 \times 3\frac{1}{2}} = \frac{128 \times 2}{5 \times 7} = 7\frac{11}{85} \text{ ft. } Ans.$$

25. How high must manure be in a cart 6 ft. by 4 ft., in order to be \(\frac{1}{2}\) a cord.

$$\frac{\frac{1}{2} \times 128}{6 \times 4} = 2\frac{2}{3} \text{ ft. } Ans.$$

26. Find the number of bushels in a bin that is 8 ft. long, 4 ft. wide, 3 ft. deep.

$$8 \times 4 \times 3 = 96$$
.  
 $96 - \frac{1}{5}$  of  $96 = 96 - 19\frac{1}{5} = 76\frac{1}{5}$  bu.  
Ans.

27. Find the number of bushels in a bin 9 ft. long, 6 ft. 6 in. wide, 3 ft. 4 in. deep.

$$9 \times 6\frac{1}{2} \times 3\frac{1}{3} = 195.$$
  
 $195 - \frac{1}{5}$  of  $195 = 195 - 39$   
= 156 bu. Ans.

28. Find the depth of a bin to hold 360 bu., if its length be 12 ft. and its width 6 ft.

$$360 - \frac{1}{4}$$
 of  $360 = 450$  cu. ft.  $\frac{450}{12 \times 6} = 6\frac{1}{4}$  ft. Ans.

29. Find the length of a bin that is 6 ft. wide and 5 ft. deep, if it hold 400 bu.

$$400 + \frac{1}{4}$$
 of  $400 = 500$  cu. ft.  
 $\frac{500}{6 \times 5} = \frac{500}{30} = \frac{50}{3} = 16\frac{2}{3}$  ft. Ans.

30. Find the number of bushels that will fill a bin 8.5 ft. long, 4.5 ft. wide, 3.5 ft. deep.

$$8.5 \times 4.5 \times 3.5 = 133.875$$
 cu. ft.  
 $133.875 - \frac{1}{5}$  of  $133.875$   
 $= 107.1$  bu. Ans.

31. A bin 20 ft. long, 12 ft. wide, and 6 ft. deep, is full of wheat. What is its value, at \$1.25 a bushel?

$$20 \times 12 \times 6 = 1440$$
 cu. ft.  
 $1440 - \frac{1}{5}$  of  $1440 = 1152$  bu.  
 $1152 \times \$1\frac{1}{4} = \$1440$ . Ans.

32. If a ton of coal occupy 40 cu. ft., how many tons will a bin hold that is 21 ft. long, 10 ft. wide, 5 ft. deep?

$$\frac{21 \times 10 \times 5}{40} = 26\frac{1}{4}$$
 t. Ans.

33. If a ton of Lehigh coal occupy 35 cu. ft., how many tons will a bin hold that is 8 ft. long, 5 ft. 9 in. wide, 4 ft. 6 in. deep?

$$\frac{8 \times 5\frac{3}{4} \times 4\frac{1}{2}}{35} = 5\frac{33}{35} \text{ t. Ans.}$$

84. Find the number of gallons that a cistern will hold that is 13 ft. long, 6 ft. wide, 7 ft. 4 in. deep.

$$13 \times 6 \times 7\frac{1}{8} = 572$$
 cu. ft.  
- 988,416 cu. in.

4278\$ gals. Ans. 231)988416

35. Find the number of gallons that a tank will hold that is 4 ft. long, 2 ft. 8 in. wide, 1 ft. 8 in. deep.

$$4 \times 2\frac{2}{8} \times 1\frac{2}{8} = 17\frac{7}{5}$$
 cu. ft.  
 $1728$   
 $\times 17\frac{7}{5}$   
 $231)30720(1327\frac{4}{5})$  gals. Ans.

36. Find the number of gallons in a cubic foot.

$$\frac{7_{77}^{87}}{231}$$
 gals. Ans.

37. Find the capacity of a cistern, in cubic feet, that will hold 200 barrels of water.

$$\frac{200 \times 31\frac{1}{2}}{7\frac{1}{2}} = 840 \text{ cu. ft. } Ans.$$

38. Find the number of gallons that a round cistern will hold that is 6 ft. in diameter and 7 ft. deep.

$$3^2 = 9.$$
 $3.1416 \times 9 \times 7 \times 7\frac{1}{2}$ 
= 1484.41 gals. Ans.

39. Find the number of gallons that a vessel will hold that is 12 in. in diameter and 10 in. deep.

6 in. = 
$$\frac{1}{2}$$
 ft.  $(\frac{1}{2})^2 = \frac{1}{4}$ .  
10 in. =  $\frac{3}{6}$  ft.  
 $\frac{1}{4} \times \frac{5}{6} \times 3.1416 \times 7\frac{1}{4} = 4.91$  gals.  
Ans.

40. How many quarts will a round vessel hold 51 in. in diameter and 6 in. deep?

$$(5\frac{1}{6})^{2} = 26\frac{25}{36}.$$

$$0.7854$$

$$\times 26\frac{25}{36}$$

$$20.9658$$

$$\times 6$$

$$125.7948 \text{ cu. in.}$$

30 qts. = 1 cu. ft.  

$$\therefore$$
 1 qt. =  $\frac{1}{30}$  of 1728 cu. in.  
= 57.6 cu. in.

41. Find the number of cubic inches in a sphere 11 in. in diameter.

$$11 \times 11 \times 11 \times 0.5236$$
  
= 696.9 cu. in. Ans

42. How many quarts will a sphere hold that is 12 in. in diameter?

$$1^8 = 1.$$
 $0.5236 \times 1 = 0.5236$  cu. ft.
 $30 \text{ qts.} = 1 \text{ cu. ft.}$ 
 $0.5236 \times 30 = 15,708 \text{ qts.}$  Ans.

43. What part of a bushel will a hemispherical bowl hold that is 13 in. in diameter?

$$13^{3} = 13 \times 13 \times 13 = 2197.$$

$$0.5236 \times 2197$$

$$2)1150.3492 \text{ cu. in.}$$

$$575.1746 \text{ cu. in.}$$

$$1 \text{ bu.} = 2150.42 \text{ cu. in.}$$

$$0.267. \text{ Ans.}$$

44. If a cubical box 2 ft. on an edge contain a solid sphere 2 ft. in diameter, how many gallons of water can be poured into the box?

215042)57517.460

$$2 \times 2 \times 2 = 8.$$
 $8 \times 0.5236 = 4.1888.$ 
 $8.0000$ 
 $4.1888$ 
 $3.8112$  cu. ft.
 $\times 1728$ 
 $6585.5536$  cu. in.
 $28.51$  gals. Ans.
 $231)6585.55$ 

45. If 64 qts. of water be poured into a vessel that will hold 2 bu. of wheat, what part of the vessel will be filled?

2 bu. = 64 dry qts.  
64 dry qts. = 
$$64 \times 67\frac{1}{5}$$
 cu. in.  
64 liquid qts. =  $64 \times 57\frac{3}{4}$  cu. in.  

$$\frac{64 \times 57\frac{3}{4}}{64 \times 67\frac{1}{5}} = \frac{55}{64} = 0.859$$
. Ans.

46. Find the number of cubic inches in 1 oz. (av.) of water.

47. Find the weight in ounces (av.) of 1 cu. in. of water.

$$\frac{1000}{728} = \frac{125}{215}$$
 oz. Ans.

48. Find the weight in ounces (av.) of 1 pt. of water.

$$\frac{1000}{7\frac{1}{2} \times 8} = 16\frac{2}{8} \text{ oz. } Ans.$$

49. Find the number of pints in 1 lb. of water.

1 pt. of water weighs  $16\frac{2}{3}$  oz. 1 lb. = 16 oz.  $\frac{16}{162} = \frac{24}{25}$  pts. Ans. 50. Find the weight, in grains, of 1 cu. in. of water.

1 cu, in. of water weighs 
$$\frac{1000}{1728}$$
 os. or  $\frac{1000}{1728 \times 16}$  lbs. or  $\frac{1000 \times 7000}{1728 \times 16}$  grs. =  $253\frac{79}{432}$  grs. Ans.

51. Find the specific gravity of a bar of iron 5 in. long, and 2 in. square, if it weigh 5 lbs.

 $5 \times 2 \times 2 = 20$  cu in.; if 20 cu. in. weigh 5 lbs., 4 cu. in. weigh 1 lb, and 1 cu. in. weighs 4 cz. 1 cu. in. of water weight  $\frac{1}{2}$  cs.

$$\frac{4}{178} = 6\frac{14}{125} = 6.912$$
. Ans.

52. Find the specific gravity of a bar of iron 18 in. long, 24 in wide, 15 in. thick, if it weigh 18 lbs. 9 os.

 $18 \times 2\frac{1}{4} \times 1\frac{3}{4} = 73\frac{1}{4}$ ; if  $73\frac{1}{4}$  cu, in. weigh 18 lbs. 9 cz. or 297 cz., 1 cu. in. weighs  $\frac{297}{73\frac{1}{4}}$ .

$$\frac{297}{73\frac{1}{2}} + \frac{125}{216} = 6\frac{4028}{3126} = 6.983. \ Ans.$$

53. Find the number of cubic inches to the pound of iron, if its specific gravity be 7.48.

1 os. of water = 
$$\frac{216}{125}$$
 cu. in.  
1 lb. of water =  $\frac{216 \times 16}{125}$  cu. in.

of iron (specific gravity 7.48) =  $\frac{216 \times 16}{7.48 \times 125} = 3\frac{451}{525}$  cu. in. Ass.

Find the number of cubic inches in 2 lbs. 6½ oz. of gold, if its gravity be 19.36.

1 oz. (av.) of water = 
$$\frac{216}{125}$$
 cu. in.

1 lb. (av.) of water = 
$$\frac{216 \times 16}{125}$$
 cu. in.

1 lb. (troy) of water = 
$$\frac{216 \times 16 \times 5760}{125 \times 7000}$$
 cu. in.  
 $2\frac{18}{22}$  lbs. (troy) of water =  $\frac{216 \times 16 \times 5760 \times 2\frac{18}{22}}{125 \times 7000}$   
 $2\frac{18}{22}$  lbs. of gold (specific gravity 19.36 or  $19\frac{9}{25}$ )  
=  $\frac{216 \times 16 \times 5760 \times 2\frac{18}{22}}{125 \times 7000 \times 19\frac{9}{25}}$   
=  $\frac{316224}{105875}$  cu. in. = 2.987 cu. in. Ans.

55. How many pounds does a boy lift in raising a cubic foot of stone under water, if its specific gravity be  $2\frac{1}{2}$ ?

Specific gravity of stone =  $2\frac{1}{2}$ . Specific gravity of water =  $\frac{1}{2}$ . Difference =  $\frac{1}{2}$ . 1 cu. ft. of water weighs 62.5 lbs.  $\frac{1}{2} \times 62.5$  lbs. = 93.75 lbs. Ans.

56. A square-built scow 12 ft. long, 61 ft. wide, sinks 5 in. in water. What does it weigh, and how many pounds will be required to sink it 7 in. deeper?

57. A square-built scow 11 ft. long, 5½ ft. wide, weighs 320 lbs. and is loaded with 750 lbs. of stone. How deep will it sink in the water?

$$11 \times 5\frac{1}{4} \times \frac{1}{12} = 4\frac{18}{16}$$
 cu. ft.  
 $4\frac{18}{16} \times 62.5$  lbs. = 300.78125 lbs.  
 $320 + 750 = 1070$  lbs.  
 $3.557$  in. Ans.  
 $30078125)107000000.000$ 

58. How many tons of ice, specific gravity 0.93, can be packed in a building 50 ft. long, 40 ft. wide, 20 ft. high?

$$\frac{50 \times 40 \times 20 \times 62\frac{1}{2} \times 0.93}{2000} = 1162\frac{1}{2} \text{ t. Ans.}$$

59. If an iceberg weigh 0.9 of an equal bulk of sea-water, how many cubic yards in an iceberg 40 rds. long, 6 yds. wide, and rising 160 ft. out of the sea?

$$40 \text{ rds.} = 660 \text{ ft.}$$
  
 $6 \text{ yds.} = 18 \text{ ft.}$   
 $660 \times 18 \times 160 = 1900800 \text{ cu. ft.} = 70,400 \text{ cu. yds.}$ 

Now, if the iceberg weighs 0.9 of the weight of an equal bulk of sea-water, only  $\frac{1}{10}$  of the iceberg is above the water.

$$10 \times 70,400 = 704,000$$
 cu. yds. Ans.

60. If a cubic foot of brick wall weigh 90 lbs. and contain 22 bricks, with the mortar, what is the weight and specific gravity of a brick and its share of mortar?

90 + 22 = 
$$4\frac{1}{11}$$
 lbs. (1) Ans.  
62 $\frac{1}{2}$  + 22 =  $2\frac{3}{4}\frac{7}{4}$  lbs.  
 $4\frac{1}{11}$  +  $2\frac{37}{4}$  =  $\frac{36}{25}$  = 1.444. (2) Ans.

61. What is the weight of a brick wall 40 ft. long, 20 ft. high, and 1 ft. thick, if the specific gravity of a brick with its mortar be 1.46; and how many thousand bricks will be required for the wall, allowing 22 for a cubic foot?

$$40 \times 20 \times = 1800$$
 cu. ft.  
 $800 \times 1.46 \times 62.5$  lbs. = 73000 lbs.  
=  $36\frac{1}{2}$  t. (1) Ans.  
 $800 \times 22 = 17,600$ . (2) Ans.

## Exercise LXI.

1. Reduce 24 gals. to liters.

24 gals. = 96 qts.  

$$96 \times 0.946^1 = 90.816^1$$
. Ans.

2. Reduce 10 lbs. troy to kilograms.

$$10 \text{ lbs.} = 120 \text{ oz.}$$
 $120 \times 31.104^{\text{g}} = 3732.480^{\text{g}}$ 
 $= 3.73248^{\text{ks.}}$  Ans.

3. Reduce 50.5 cu. yds. to cu. meters.

 $50.5 \times 0.765^{\text{obm}} = 38.63^{\text{obm}}$ . Ans.

4. Reduce 6917 mi. to kilometers.

$$69.17 \times 1.609^{km} = 111.2945^{km}$$
.

5. Reduce 12 A. 12 rds. to hektars.

12 sq. rds. = 0.075 A.  $12.075 \times 0.405^{\text{hs}} = 4.89^{\text{hs}}$ . Ans.

6. Reduce 10 cords to sters.

$$10 \times 3.624^{st} = 36.24^{st}$$
. Ans.

7. Reduce 4 cwt. 24 lbs. to kilograms.

4 cwt. 24 lbs. = 424 lbs.  $424 \times 0.454$  kg = 192.496 kg. Ans.

8. Reduce 25 bu. 2 pks. to hektoliters.

25 bu. 2 pks. = 816 qts.  

$$816 \times 1.101$$
 qts. =  $898.416^{1}$   
=  $8.98416^{11}$ . Ans.

9. Reduce to the common system 15<sup>km</sup>.

0.621  

$$\times 15$$
  
9.315 mi.  
 $\times 320$   
100.8 rds.  
 $\times 5\frac{1}{2}$   
4 yds. nearly.

9 mi. 100 rds. 4 yds. nearly. Ans.

10. Reduce to the common system 3<sup>ha</sup>.

2.471 A.  

$$\frac{\times 3}{7.413}$$
 A.  
 $\frac{\times 160}{66.08}$  sq. rds.  
 $\frac{\times 30\frac{1}{4}}{2}$  sq. yds. nearly.

7 A. 66 sq. rds. 2 sq. yds. nearly.

Ans.

11. Reduce to the common system 12.125° m.

1.308 cu. yds.  

$$\frac{\times 12\frac{1}{8}}{15.8295}$$
 cu. yds.  
 $\frac{\times 27}{23.3965} = 23.4$  cu. ft.

15 cu. yds. 23.4 cu. ft. Ans.

12. Reduce to the common system 101.251.

1.0567 liquid qts.  

$$\times 101\frac{1}{4}$$

$$106.9908$$
= 107 liquid qts. nearly. Ans.
$$0.908 \text{ dry qts.}$$
 $\times 101\frac{1}{4}$ 

$$91.935$$

= 92 dry qts. nearly. Ans.

13. Reduce to the common system 20.25<sup>hl</sup>.

$$20.25^{\text{hl}} = 2025^{\text{l}}$$
 $1.0567 \text{ liquid qts.}$ 
 $\times 2025$ 
 $4)2139.8175 \text{ qts.}$ 
 $535 \text{ gals. nearly. } Ans.$ 

14. Reduce to the common system (troy weight) 514.

13 lbs. 4 oz. 15 dwt. Ans.

15. Reduce to the common system 24st.

$$0.276^{\circ}$$
 $\times 24$ 
 $\overline{6.624}$ 
 $\times 128$ 
 $\overline{79.872}$ 

= 80 cu. ft. nearly.

6 c. 80 cu. ft. nearly. Ans.

16. Reduce to the common system 62.5<sup>qm</sup>.

17. Reduce to the common system (avoirdupois weight) 10014.

- 1 t. 2 cwt. 7 lbs. nearly. Ans.
- 18. Find in acres, etc., the area of a field if its length be 100<sup>m</sup> and breadth 75<sup>m</sup>.

1 A. 136 sq. rds. 16 sq. yds. Ans.

19. Determine the number of cubic meters in a box 2 yds. long, 3 ft. wide,  $2\frac{1}{2}$  ft. deep.

2 yds. = 6 ft.  

$$6 \times 3 \times 2\frac{1}{2} = 45$$
 cu. ft.  
=  $1\frac{2}{3}$  cu. yds.  
 $1\frac{2}{3} \times 0.765^{\text{cbm}} = 1.275^{\text{cbm}}$ .

20. Determine the number of cubic yards in a box 2<sup>m</sup> long, 75<sup>cm</sup> wide, 50<sup>cm</sup> deep.

$$2 \times 0.75 \times 0.50 = 0.75^{\text{obm}}$$
.  
 $0.75 \times 1.308 \text{ cu. yds.}$   
 $= 0.981 \text{ cu. yds.}$  Ans.

21. If a man walk 75<sup>m</sup> a minute, what is his rate in miles per hour?

$$75 \times 60 = 4500^{m} = 4.5^{km}$$
.  
 $4.5 \times 0.621 \text{ mi.} = 2.795 \text{ mi.}$  Ans.

22. If cast-iron weigh 7.113s per cubic centimeter, how many pounds does a cubic foot weigh?

As the weight of the iron is 7.113s per cubic centimeter, the specific gravity is 7.113. 7.113 × 62.5 lbs. = 444.5625 lbs.

Ans.

23. How many steps 2 ft. 6 in. long will a man take in walking a kilometer?

$$0.621 \text{ mi.}$$
 $\times 5280$ 
 $32788.8 \text{ ft.}$ 

1311.5 steps = 1312 steps. Ans.

24. Find the value of a carboy (17 qts.) of sulphuric acid, of 1.841 specific gravity, at 2½ cents a pound.

$$0.946^{1}$$
 $\times 17$ 
 $16.082^{1}$ 
 $16.082^{1}$ 
 $16.082^{1}$ 
 $\times 2.205 \text{ lbs.}$ 
 $35.461 \text{ lbs.}$ 
 $\times 1.841$ 
 $65.284 \text{ lbs.}$ 
 $65.284$ 
 $\times \$ 0.02\frac{1}{2}$ 
 $\$ 1.47. Ans.$ 

25. Find the value of a carboy  $(17\frac{1}{2}1)$  of nitric acid, of 1.451 specific gravity, at 15 cents a pound.

2.205 lbs.  

$$\times 17\frac{1}{2}$$
  
38.588 lbs.  
 $\times 1.451$   
55.971 lbs.  
 $\times $0.15$   
 $\$ 8.40$ . Ans.

26. Find the weight in pounds and in kilograms of 31½ gals. of the best alcohol, specific gravity 0.792.

31
$$\frac{1}{6}$$
 gals. = 124 $\frac{2}{3}$  qts.  
0.946 $\frac{1}{24\frac{2}{3}}$   
117.935 $\frac{1}{2}$  of water.

117.935kg × 0.792 93.405kg. (1) Ans. 93.405 2.205 lbs. 205.958 lbs. (2) Ans.

27. If the specific gravity of sea-water be 1.026, and that of olive-oil be 0.915, what will be the weight of a hektoliter of each in pounds and in kilograms?

$$1^{hl} = 100^{l} = 100^{kg}$$
.  
 $1.026$   
 $\times 100^{kg}$   
 $102.6^{kg}$ . (1) Ans.  
 $\times 2.205$  lbs.  
 $226.233$  lbs. (2) Ans.  
 $0.915$   
 $\times 100^{kg}$   
 $91.5^{kg}$ . (3) Ans.  
 $\times 2.205$  lbs.  
 $201.76$  lbs. (4) Ans.

28. Find the weight in pounds and in kilograms of the air, specific gravity 0.00129206, in a room 7<sup>m</sup> by 5<sup>m</sup>, and 3.5<sup>m</sup> high.

$$7 \times 5 \times 3\frac{1}{2} = 122\frac{1}{2}^{\text{obm}}$$
.  
 $122\frac{1}{2}^{\text{cbm}}$  of water =  $122,500^{\text{kg}}$ .  
 $0.00129206$   
 $\times 122500^{\text{kg}}$   
 $158.27735^{\text{kg}}$ . (1) Ans.

29. Find the weight in pounds and in kilograms of the air, specific gravity 0.00129206, in a room 23 ft. long, 16 ft. wide, and 10 ft. high.

30. If a balloon weigh 2<sup>kg</sup>, and contain 10,000<sup>1</sup> of hydrogen gas, specific gravity 0.00008929, what is its lifting force in kilograms and in pounds when the air has a specific gravity of 0.00129206?

0.00129206 0.00008929 0.00120277 × 10000ks 12.0277ks 2. 10.0277ks. (1) Ans. 10.0277 × 2.205 lbs. 22.111 lbs. (2) Ans.

31. If a pile of wood be 1.2<sup>m</sup> wide, 7<sup>m</sup> long, and 2<sup>m</sup> high, how much is it worth, at \$4.50 a cord?

 $1.2 \times 7 \times 2 = 16.8^{st}$ .  $16.8 \times 0.276^{o} = 4.6368^{o}$ .  $4.6368 \times $4\frac{1}{2} = $20.87$ . Ans.

32. How many miles will be travelled in 1 hr. 28 min. 21 sec., at the rate of 50km an hour?

1 hr. 28 min. 21 sec. = 1.4725 hr.  $50^{km} = 50 \times 0.621$  mi. = 31.05 mi.  $1.4725 \times 31.05$  mi. = 45.721 mi.

Ans.

33. Find the time of travelling 31 mi. 180 yds. at 1 min. 25 sec. per kilometer.

 $1^{km} = 0.621 \text{ mi.}$   $1 \text{ min. } 25 \text{ sec.} = 1_{\frac{5}{12}}^{\frac{5}{12}} \text{ min.}$  31 mi. 180 yds. = 31.1023 mi. 31102.3 + 621 = 50.08  $50.08 \times 1_{\frac{5}{12}}^{\frac{5}{12}} \text{ min.} = 70.95 \text{ min.}$  = 1 hr. 11 min., nearly. Ans.

34. What is the weight of 12 cu. yds. 16 cu. ft. 720 cu. in. of earth of which a cubic meter weighs 1 t. 17 cwt.?

12 cu. yds. 16 cu. ft. 720 cu. in. = 12.608 cu. yds.  $1^{\text{obm}} = 1.308 \text{ cu. yds.}$  12608 + 1308 = 9.639. 1 t. 17 cwt. = 37 cwt.  $9.639 \times 37 \text{ cwt.} = 356.643 \text{ cwt.}$  = 17 t. 16 cwt. 64 lbs. Ans.

35. Find the weight in grams of a liter of mercury, of which a cubic inch weighs 0.4925 of a pound avoirdupois.

 $1^1 = 61.03$  cu. in. 0.4925 lbs.  $\times 61.03 = 30.057$  lbs.  $30.057 \times 453.59s = 13633.55s$ .

36. How many yards of cloth, at \$3.12½ a meter, should be given in exchange for 15<sup>m</sup> at \$2.75 a yard?

1 yd. = 0.914<sup>m</sup>. 0.914 × \$3 $\frac{1}{8}$  = \$2.856 per yd. 15 × 1.0936 yds. = 16.404 yds. 16.404 × \$2 $\frac{3}{4}$  = \$45.111. 45111 ÷ 2856 = 15.79 yds. Ans.

37. If a wine merchant buy 3<sup>hl</sup> of wine for 1600 francs, at what rate, United States money, does he pay a gallon, reckoning 25 francs equal to \$4.85?

 $3^{hl} = 300^{l}$ .  $1600 \text{ francs} \div 300 = 5\frac{1}{3} \text{ francs}$ .  $$4.850 \div 25 = $0.194$ .  $$0.194 \times 5\frac{1}{3} = $1.035 \text{ per l.}$   $1^{l} = 1.0567 \text{ qts.}$  = 0.264 gals. $1035 \div 264 = $3.92$ . Ans. 38. A mill-wheel is turned by a stream of water running at the rate of a yard per second in a channel 5 ft. wide and 9 in. deep. Determine the weight of water in metric tons, supplied in 12 hrs., if a cubic foot of water weigh 1000 oz.

$$3 \times 5 \times \frac{3}{4} = 11\frac{1}{4}$$
 cu. ft.  
12 hrs. = 43,200 sec.

 $43200 \times 111$  cu. ft.

=486000 cu. ft.

 $486000 \times 1000 \text{ oz.}$ 

- 486000000 os.

= 30375000 lbs.

 $0.00045359 \text{ m. t.} \times 30375000$ 

= 13777.796 m. t.

Ans.

## EXERCISE LXII.

1. Which is the greater ratio, 5:8 or 6:9?

5:8=
$$\frac{5}{8}=\frac{15}{24}$$
.  
6:9= $\frac{6}{9}=\frac{2}{3}=\frac{16}{24}$ .  
.. 6:9 is greater.

2. Which is the greater ratio, 7:10 or 9:12?

7: 
$$10 = \frac{7}{10} = \frac{14}{20}$$
.  
9:  $12 = \frac{9}{12} = \frac{3}{4} = \frac{15}{20}$ .  
 $\therefore$  9: 12 is greater.

3. Which is the greater ratio, 8:9 or 10:12?

8:9 = 
$$\frac{8}{9}$$
 =  $\frac{16}{18}$ .  
10:12 =  $\frac{10}{12}$  =  $\frac{5}{6}$  =  $\frac{15}{18}$ .  
 $\therefore$  8:9 is greater.

4. Which is the greater ratio, 6:12 or 8:14?

6: 
$$12 = \frac{6}{12} = \frac{1}{2} = \frac{7}{14}$$
.  
8:  $14 = \frac{8}{14}$ .  
... 8: 14 is greater.

5. Which is the greater ratio, 10 cwt.: 15 cwt. or \$7:\$9?

10 cwt.: 15 cwt. = 
$$\frac{10 \text{ cwt.}}{15 \text{ cwt.}} = \frac{2}{3} = \frac{6}{3}$$
.  
\$7:\$9 =  $\frac{\$7}{\$9} = \frac{7}{3}$ . \this \\$7:\$9 is greater.

6. Which is the greater ratio, 5 dys.: 7 dys. or 8 ft.: 11 ft.?

5 dys. : 7 dys. = 
$$\frac{5 \text{ dys.}}{7 \text{ dys.}} = \frac{5}{7} = \frac{55}{77}$$
.

8 ft.: 11 ft. = 
$$\frac{8 \text{ ft.}}{11 \text{ ft.}} = \frac{8}{11} = \frac{56}{77}$$
.  $\therefore$  8 ft.: 11 ft. is greater.

7. Which is the greater ratio, 9 yds.: 6 yds. or 5:3?

9 yds.: 6 yds. = 
$$\frac{9 \text{ yds.}}{6 \text{ yds.}} = \frac{9}{6}$$
.

$$5:3=\frac{5}{8}=\frac{10}{8}$$
.

∴ 5:3 is greater.

8. Which is the greater ratio, 2 lb.: 1 lb. or 5 yd.: 2 yd.?

$$\frac{3}{4}$$
 lb.:  $\frac{1}{2}$  lb.  $=\frac{\frac{3}{4}}{\frac{1}{2}}$  lb.  $=\frac{4}{5}$ .

$$\frac{1}{8}$$
 yd. :  $\frac{1}{8}$  yd. =  $\frac{1}{8}$  yd. :  $\frac{1}{8}$  yd. :  $\frac{1}{8}$  yd. :  $\frac{1}{8}$  yd. is greater.

#### EXERCISE LXIII.

1. If 24 men can finish some work in 14 days, how long will it take 21 men to do it?

$$\frac{\frac{8}{24} \times 14}{21} \text{ dys.} = 16 \text{ dys.} \text{ Ans.}$$

2. A well is dug in 13 days of 9 hours each. How many days of 10 hours each would it have taken?

$$\frac{9\times13}{10}$$
 dys.  $=\frac{117}{10}=11\frac{7}{10}$  dys. Ans.

3. A man who steps 2 ft. 5 in. takes 2480 steps in walking a cer-How many steps of 2 ft. 7 in. will be required for the tain distance. same distance?

$$2 \text{ ft. } 5 \text{ in.} = 29 \text{ in.}$$

$$2 \text{ ft. } 7 \text{ in.} = 31 \text{ in.}$$

31:29::2480: what?

$$\frac{29 \times \cancel{2489}}{\cancel{21}} = 2320.$$

2320 steps. Ans.

4. If A ton cost \$6, what will 78 cwt. cost, at the same rate?

$$7\frac{4}{9}$$
 cwt. =  $\frac{7\frac{4}{9}}{20}$  t. =  $\frac{17}{48}$  t.

$$\frac{1}{15}: \frac{17}{15}:: \$6 \text{ what?}$$

$$\frac{17 \times 6}{15} = \frac{17 \times 13 \times \$6}{45 \times 5} = \frac{\$442}{75} = \$5.89, Ans.$$

5. If 42 yds, of carpet 2 ft. 3 in. wide are required for a room, bow many yards 2 ft. 4 in. wide will be required?

2 ft. 4 in. = 28 in.

28: 27:: 42 yds.: what?

$$\frac{27 \times 42}{23} = \frac{81}{2} \text{ yds.} = 40\frac{1}{2} \text{ yds.} \text{ Ans.}$$

6. A court was gaved with 950 stones, each 18 sq. ft., and is repaved with 836 stones of a uniform size. Find the size of each.

$$\frac{950 \times 1\frac{5}{5}}{836} = \frac{\frac{25}{950 \times 11}}{\frac{826}{22} \times 6} = 2\frac{1}{11} \text{ aq. ft. } Ans.$$

If a train, at the rate of 👫 of a mile per minute, take 31 hrs. ch a station, how long will it take at the rate of 7 of a mile a æ?

$$\frac{7}{16}: \frac{6}{18}:: 5\frac{1}{1}$$
 hrs. what?  
 $\frac{15}{18} \times \frac{3\frac{1}{4}}{7} = \frac{15}{7} \times \frac{5}{13} \times \frac{13}{4} = \frac{75}{28} = 2\frac{13}{38}$  hrs. Ans.

If a post 4 ft. 8 in. high cast a shadow 7 ft. 3 in. long, how long low will a post 11 ft. high cast?

$$\frac{11 \times 7\frac{1}{4}}{4\frac{3}{4}} = \frac{3 \times 11 \times 29}{14 \times 4} = 17\frac{5}{54} \text{ ft.} = 17 \text{ ft. } 1\frac{1}{12} \text{ in. } Ans.$$

9. When a shadow 8 ft. 5 in. long is cast by a post 5 ft. 7 in. high, how high is a steeple that casts a shadow of 211 ft. at the same time?

$$8\frac{5}{13}$$
: 211:: $5\frac{7}{13}$  ft.: what?  

$$\frac{211 \times 5\frac{7}{13}}{8\frac{5}{13}} = \frac{12 \times 211 \times 67}{101 \times 12} = 139\frac{95}{101}$$
 ft. = 139 ft.  $11\frac{65}{101}$  in.

10. If 4 men can mow a certain field in 10 hrs., how many men will it take to mow it in 5 hrs.?

5:10::4 men: what? 
$$\frac{2}{19 \times 4}$$
 men = 8 men. Ans.

11. A tap discharging 4 gals. a minute empties a cistern in 3 hrs. How long will it take a tap discharging 7 gals. a minute to empty it?

7:4::3 hrs.: what? 
$$\frac{4 \times 3}{7}$$
 hrs. = 15 hrs. Ans.

12. A pipe discharging 3 gals. 1 pt. a minute fills a tub in 4 min. 20 sec. How long will it take a pipe discharging 83 qts. a minute to fill it?

3 gals. 1 pt. = 25 pts. 83 qts. = 166 pts.  
4 min. 20 sec. = 260 sec.  
130  
166: 25:: 260 sec.: what? 
$$\frac{25 \times 269}{166} = 39\frac{13}{15} \text{ sec. } Ans.$$

13. If both pipes of Ex. 12 discharge at the same time into the tub, how long will it take to fill it?

4½ min. = 260 sec.  
95½: 12½:: 260 sec.: what?  

$$\frac{12½ \times 260}{95½} = \frac{2}{191} \times \frac{25}{2} \times \frac{260}{1} = \frac{6500}{191} \text{ sec.} = 34\frac{6}{191} \text{ sec.} Ans.$$

14. How long will it take to fill a cistern of 165 gals. by a pipe that fills one of 120 gals. in 7 min. 16 sec.?

16 sec. = 
$$\frac{4}{15}$$
 min.  
120: 165::  $7\frac{4}{15}$  min.: what?  

$$\frac{11}{120} = \frac{165 \times 7\frac{4}{15}}{120 \times 15} = 9\frac{1}{120}$$
 min. = 9 min. 59 $\frac{1}{2}$  sec. Ans.

15. A ship has sailed 1800 mi. m a formight. How long, at the same rate, will it take for a voyage of 5000 mi. ?

$$\frac{25}{1809} \times \frac{2}{2} = \frac{50}{9} = 5\frac{1}{9}$$
 where

54 wks. = 5 wks. 4 dys. nearly. Ans.

16. The wheels of a carriage are 6 ft. 9 in. and 9 ft. 6 in. in circumserence. How many times will the larger turn while the smaller turns 3762 times?

$$\frac{64 \times 3762}{94} = \frac{2 \times 27 \times 3362}{19 \times 4} = 2673. Ans.$$

17. If A of a ship be worth \$2167, what is the value of A of it?

$$\frac{\frac{2}{15}:\frac{7}{17}::\$2167:\text{what?}}{\frac{7}{15}\times\$2167} = \frac{25\times7\times2167}{3\times17} = \frac{\$379225}{51} = \$7435.78. \text{ Ans.}$$

eat will be the weight of 18 cu. ft. 432 cu. in. of stone of cu. ft. 864 cu. in. weigh 14 cwt. 7 lbs.?

$$\frac{18\frac{1}{2} \times 1407}{10\frac{1}{2}} = \frac{2 \times 73 \times 1497}{21 \times 4} = \frac{4891}{2} \text{ lbs.} = 2445\frac{1}{2} \text{ lbs.}$$

$$= 1 \text{ t. 4 cwt. } 45\frac{1}{2} \text{ lbs.} \text{ Ans.}$$

280 lbs. of flour make 360 lbs. of bread, how many four ves can be made from 1 cwt. of flour?

$$\frac{100 \times \frac{9}{569}}{\frac{289}{7}} = \frac{900}{7} = 1284 \text{ lbe.} \qquad 1284 + 4 = 324. Ans$$

20. If a column of mercury 27.93 in. high weigh 0.76 of a pound, what will be the weight of a column of the same diameter 29.4 in. high?

27.93: 29.4:: 0.76 lb.: what?  
0.2 4  

$$\frac{29.4 \times 0.76}{27.93}$$
 lb. = 0.8 lb. Ans.  
0.19

21. How many francs will pay a bill of £100, when £42 10 s. 8 d. is equivalent to 1090.98 francs?

£42 10 s. 8 d. = £42 
$$\frac{8}{15}$$
.  
42  $\frac{8}{15}$ : 100:: 1090.98 francs: what?  

$$\frac{1090.98 \times 100}{42 \frac{8}{15}} \text{ francs} = \frac{15}{638} \times \frac{199998}{199} \times \frac{199}{1} = 2565 \text{ francs.}$$

22. What will be the weight of a cube whose edge is 2 ft. 2 in., when a cube of the same material whose edge is 1 ft. 4 in. weighs 537.6 lbs.?

2 ft. 2 in. = 
$$2\frac{1}{6}$$
 ft. 1 ft. 4 in. =  $1\frac{1}{3}$  ft. ( $1\frac{1}{3}$ )<sup>3</sup>: ( $2\frac{1}{6}$ )<sup>3</sup>: 537.6 lbs.: what?  $\frac{21}{27}$ :  $\frac{2197}{216}$ : 537.6 lbs.: what?  $\frac{21}{672}$   $\frac{27}{64} \times \frac{2197}{216} \times \frac{5376}{10} = \frac{46137}{20}$  lbs. = 2306.85 lbs. Ans.  $\frac{2}{2}$ 

23. If a square field measuring 50 yds. 10% in. on each side be worth \$2710\frac{1}{2}, what is the value of a square field 62 yds. 1 ft. each way?

50 yds. 
$$10^{2}_{7}$$
 in.  $= 50^{2}_{7}$  yds. 52 yds. 1 ft.  $= 62^{1}_{8}$  yds.  $(50^{2}_{7})^{2}$ :  $(62^{1}_{8})^{2}$ : \$2710 $^{1}_{1}$ ? what?  $\frac{123904}{49}$ :  $\frac{34969}{9}$ :  $\frac{$46080}{17}$ : what?  $\frac{17}{2957}$  \$129  $\frac{5}{173994}$  ×  $\frac{34969}{9}$  ×  $\frac{46989}{17}$  = \$4165. Ans.

24. A gains 4 yds. on B in running 30 yds. How much will be gain while B is running 97 g yds.?

30: 
$$97\frac{1}{2}$$
: 4 yds.; what?  
 $13$  2  
 $195 \times 4$   
 $2 \times 39$   
 $2 \times 39$   
 $15$   
 $2 \times 39$ 

25. If 10 cu. in, of gold weigh as much as 193 cu. in, of water, what is the size of a nugget weighing as much as a cubic foot of water?

193 . 1728 : . 10 cu. in. : what?  

$$\frac{1728 \times 10}{193} = \frac{17280}{193} = 89\frac{1}{1}\frac{2}{3}$$
 cu. in. Ans.

26. If a garrison of 1500 men have provisions for 13 months, how long will the provisions last if it be increased by 700 men?

1500 + 700 = 2200.  
2200 . 1500 : : 13 mo. : what?  
15  

$$\frac{1599 \times 13}{2299}$$
 mo. =  $\frac{198}{23}$  mo. =  $8\frac{19}{23}$  mo. Ans.

ree 38 ft. high be represented by a drawing 14 in. high, same scale, will represent the height of a house 45 ft.

38: 45:: 1½ in.: what?  

$$\frac{45 \times 3}{38 \times 2}$$
 in. = 1½ in. = 1‡‡ in. Ans.

untry 630 mi. long be represented on a raised map by a ft., by what height ought a mountain of 15,750 ft. be in the map?

29. A train travels \(\frac{1}{2}\) of a mile in 18 sec. How many miles an hour does it travel?

1 hr. = 3600 sec. 18: 3600:: 
$$\frac{1}{4}$$
 mi.: what?  
200  
 $\frac{3699 \times \frac{1}{4}}{18} = 50$  mi. Ans.

30. If 4½ tons of coal fill a bin 9 ft. long, 5 ft. broad, 5 ft. high, how many cubic feet will be required for the coal of a steamer carrying 3 weeks' consumption at 20 tons a day?

$$9 \times 5 \times 5 = 225$$
 cu. ft. 3 wks. = 21 dys.  
 $21 \times 20$  t. = 420 t.  $4\frac{1}{2}$ : 420: : 225 cu. ft. : what?  
 $\frac{25}{9}$  cu ft. = 21,000 cu. ft. Ans.

31. If 2 lbs. of rosin be melted with 5 oz. of mutton tallow, to make a grafting wax, how many ounces of tallow will 20 oz. of the wax contain?

2 lbs. + 5 oz. = 2 lbs. 5 oz. = 37 oz.  

$$37: 20: 5 \text{ oz.} : \text{ what ?}$$
  
 $\frac{20 \times 5}{37} = \frac{100}{37} \text{ oz.} = 2\frac{26}{37} \text{ oz.} \text{ Ans.}$ 

# EXERCISE LXIV.

1. How many days 8 hours long will 60 men take to finish some work which 24 men can do in 15 days, working 10 hours a day?

$$\begin{array}{c|c}
8 & 10 \\
60 & 24 \\
\hline
5 & 3 \\
\cancel{19 \times 24 \times 15} \\
\cancel{5} & \cancel{4} \\
2
\end{array}$$
dys. =  $\frac{15}{2}$  dys. =  $7\frac{1}{2}$  dys. Ans.

2. What will be the expense of covering a room with drugget 4 ft. wide, at 913 cts. a yard, when carpet 2 ft. 3 in. wide for the room costs \$70.50, at \$1.371 a yard?

3. If 4418 tons of iron ore produce \$36,190 worth of metal, when iron is at \$37.50 a ton, what will be the value of the iron from 2275 tons of ore, at \$47 a ton?

4. If a bar of iron 3\frac{1}{2} ft. long, 3 in. wide, 2\frac{3}{2} in. thick weigh 93 lbs., what will be the weight of a bar 3\frac{2}{2} ft. long, 4 in. wide, and 2\frac{1}{2} in. thick?

$$\begin{array}{c|c}
3\frac{1}{3} & 3\frac{2}{3} \\
3 & 4 :: 93 \text{ lbs.} : \text{ what?} \\
2\frac{3}{4} & 2\frac{1}{2}
\end{array}$$

$$\frac{2}{2} \times \frac{31}{2} \times \frac{3}{2} \times \frac{5}{2} \times \frac{5}{2} \times \frac{31}{1} \times \frac{3}{10} \times \frac{4}{11} = 124 \text{ lbs.} \quad Ans.$$

5. If 40 bu. of wheat can be grown on the same area as 48 bu. of barley, and 28 acres produce 840 bu. of wheat, how much barley will be obtained from 38 acres?

$$\begin{array}{c|c}
40 & 48 \\
28 & 38 \\
\end{array} :: 840 \text{ bu.} : \text{ what?} \qquad \begin{array}{c|c}
6 & 39 \\
48 \times 38 \times 849 \\
\hline
49 \times 28 \\
\hline
5 & 39
\end{array} = 1368 \text{ bu.}$$

6. If 18 men can dig a trench 150 ft. long, 6 ft. broad, and 4 ft. 6 in. deep in 12 days, how long will 16 men take for a trench 210 ft. long, 5 ft. broad, and 4 ft. deep?

7. In the reprint of a book consisting of 810 pages, 50 lines are contained in a page, instead of 40, and 72 letters in a line, instead of 60. Of how many pages will the new edition consist?

$$\begin{array}{c|c}
50 & 40 \\
72 & 60
\end{array} : 810 : \text{what?} \qquad \begin{array}{c}
10 & 6 & 45 \\
49 \times 99 \times $19 \\
\hline
59 \times 72 \\
\hline
5 & 4
\end{array} = 540. Ans.$$

8. If 3280 42-lb. shot cost \$3000, how many 32-lb. shot can be bought for \$4200?

$$\begin{array}{c|c}
3000 & 4200 \\
32 & 42
\end{array} :: 3280 : \text{ what?} \qquad \begin{array}{c}
7 & 21 & 295 \\
4299 \times 42 \times 3289 \\
\hline
3999 \times 32 \\
\hline
5 & 2
\end{array} = 6027.$$

9. What must be the rate of wages, that 12 men may earn in 10 days the same amount that 9 men earn in 14 days, at \$1.50 a day?

10. A reservoir 15 yds. long and 4 ft. deep holds 32,500 gals. Determine the quantity of water it will hold when it has been increased in length by 18 ft. and in depth 1 ft.

$$\begin{array}{c|c}
15 & 21 \\
4 & 5
\end{array}$$
: 32,500 gals.: what?
$$7 & 8125 \\
\hline
21 \times 5 \times 22500 \\
\hline
15 \times 4
\end{array}$$
gals. = 56,875 gals. Ans.

11. How far can A, who takes 3.1 ft. each step, run, while B, who takes 2.3 ft. each step, runs 220 yds., if A takes 7 steps while B takes 11?

$$\begin{array}{c|c} 2.3 & 3.1 \\ 11 & 7 \end{array} : \cdot 220 \text{ yds.} \cdot \text{what?} \\ \hline & 20 \\ \hline & 3.1 \times 7 \times 229 \\ \hline & 2.3 \times II \end{array} \text{yds.} = \frac{434}{2.3} \text{ yds.} = 188\frac{14}{2} \text{ yds.} \text{ Ans.} \end{array}$$

12. If 6 hours be required for travelling a given distance at a given rate, how long will be required when the distance is diminished by one-fourth and the rate is increased by one-half?

$$\frac{1}{1\frac{1}{2}} \begin{bmatrix} \frac{1}{4} & 0 \text{ hrs. : what?} \\ \frac{3}{2} & \frac{3}{2} \times \frac{2}{3} \text{ hrs.} = 3 \text{ hrs. } Ans.$$

13. How many hours a day must 5 men work to mow the same quantity of grass in 8 days that 7 men can mow in 6 days, working 10 hours a day?

14. If a bar 10 ft. 6½ in. long, 3½ in. broad, 3½ in. thick weigh 5 cwt. 8.23 lbs., what length must be taken to weigh a long ton when the breadth and thickness are 4½ in. and 4½ in. respectively?

1 l. t. = 2240 lbs. 4 cwt. 8.23 lbs. = 408.23 lbs.

40823 | 224000 | 
$$3\frac{5}{8}$$
 ::  $10\frac{13}{24}$  ft.: what?

4\frac{1}{4} |  $3\frac{1}{2}$ 

7000

14999

28999

23

274999 \times \frac{3}{8} \times \frac{8}{8} \times \frac{2}{8} \times \frac{1}{8} \frac{1}{8} \frac{1}{12} \frac{1}{2} \frac{1}{8} \frac{1}{8} = 38 \frac{1}{122469} = 38 \text{ ft. 1.5 in.}

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3

15. If 27 men, in 28 days of 10 hours each, dig a trench 126 yds. long, 2½ yds. broad, 1½ yds. deep, how long a trench 2¾ yds. broad, 1¾ yds. deep, will 56 men dig in 25 days of 8¼ hours?

27 | 56  
10 | 8½  
28 | 25 :: 126 yds. : what?  
2½ | 2½  
1½ | 1½ | 6  

$$\frac{2}{4 \times 4 \times 56 \times 33 \times 25 \times 5 \times 3 \times 126}}{4 \times 4 \times 56 \times 33 \times 25 \times 5 \times 3 \times 126}}$$
 yds. = 150 yds. Ans.  
 $\frac{11}{11 \times 7 \times 27 \times 19 \times 4 \times 28 \times 2 \times 2}$ 

16. What must be the length of a bar of silver \(\frac{3}{4}\) in. square, that it may weigh the same as a bar of gold \(\frac{1}{2}\) in. square and  $6\frac{3}{4}$  in. long, if the weight of a cubic inch of silver have to that of a cubic inch of gold the ratio 47:88?

$$\begin{array}{c|c}
\frac{\binom{3}{4})^2}{47} & \binom{\binom{1}{2})^3}{88} :: 6\frac{3}{4} \text{ in.} : \text{ what?} \\
\frac{4}{16} & \frac{22}{88} :: 6\frac{3}{4} \text{ in.} : \text{ what?} \\
\frac{16 \times 88 \times 27}{9 \times 47 \times 4 \times 4} \text{ in.} = 5\frac{29}{47} \text{ in.} \quad Ans.
\end{array}$$

17. If it take 34kg of wool to make 25m of cloth 0.6m wide, how long a piece of cloth 0.8m wide can be made from 108.8kg of wool?

$$\begin{array}{c|c}
34 & 108.8 \\
0.8 & 0.6
\end{array} : 25^{m} : \text{what?} \qquad \begin{array}{c}
4 \\
136 \\
198.8 \times 0.6 \times 25 \\
34 \times 0.8
\end{array} = 60^{m}. Ans.$$

18. An oak beam 5.40<sup>m</sup> long, 0.63<sup>m</sup> thick, and 0.57<sup>m</sup> wide weighs 1469.25<sup>ks</sup>; find the weight of a beam whose dimensions are 4.87<sup>m</sup>, 0.58<sup>m</sup>, 0.53<sup>m</sup>.

19. A certain quantity of air has a volume of 195.5 cu, ft. at 27.8°. What will be its volume at 100°?

$$100^{\circ} - 27.8^{\circ} = 72.2^{\circ}$$
.  $72.2 \times 0.00367 = 0.264974$ .   
1: 1.264974:: 195½ cu. ft.: what?  
 $\frac{1.264974 \times 195}{1}$  cu. ft. = 247.3 cu. ft. Ans.

20. A quantity of air at a temperature of 15.6° C. has a volume of 4 cu. ft. under a pressure of 12 lbs. to the square inch. What will be its volume at a temperature of 48.7° C., and under a pressure of 14 lbs. the square inch?

$$48.7^{\circ} - 15.6^{\circ} = 33.1^{\circ}$$
.  $33.1 \times 0.00367 = 0.121477$ .   
 $14 \mid 12 \atop 1 \mid 1.121477 :: 4 \text{ cu. ft. : what?}$ 

$$\frac{3}{12 \times 1121477 \times 4} \quad \text{cu. ft.} = \frac{3364431}{875000} \text{ cu. ft.} = 3.8 \text{ cu. ft. } Ans.$$

$$\frac{7}{125000} \quad \frac{5999999}{125000} \quad \frac{125000}{125000}$$

# EXERCISE LXV.

1. Divide \$12,000 proportionally to the numbers 3, 4, 5.
$$3 + 4 + 5 = 12.$$

$$1000$$

$$\frac{3}{12} \times \frac{\$12000}{1} = \$3000.$$

$$\frac{5}{12} \times \frac{\$12000}{1} = \$5000.$$

2. Divide 815 tons proportionally to  $\frac{1}{2}$ ,  $\frac{3}{4}$ ,  $\frac{4}{5}$ .

$$(\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}) \times 60 = 30, 40, 45, 48.$$
  
  $30 + 40 + 45 + 48 = 163.$ 

$$\frac{30}{163} \times \frac{815}{1} = 150 \text{ t.}$$

$$\frac{40}{163} \times \frac{815}{1} = 200 \text{ t.}$$

$$\frac{45}{163} \times \frac{815}{1} = 225 \text{ t.}$$

$$\frac{48}{163} \times \frac{815}{1} = 240 \text{ t.}$$

3. Divide 6853 lbs. of wool proportionally to 1½, 2½, 5½; and also proportionally to the reciprocals of these numbers.

$$(\frac{7}{4}, \frac{14}{5}, \frac{35}{5}) \times 60 = 105, 168, 350.$$
  
 $105 + 168 + 350 = 623.$ 

$$\frac{105}{623} \times \frac{6853}{1} = 1155 \text{ lbs.}$$

$$\frac{168}{623} \times \frac{11}{6853} = 1848 \text{ lbs.}$$

$$\frac{11}{6823} \times \frac{11}{1} = 1848 \text{ lbs.}$$

$$\frac{11}{6833} \times \frac{11}{6853} = 3850 \text{ lbs.}$$

The reciprocals of

$$1\frac{8}{4}$$
,  $2\frac{4}{5}$ ,  $5\frac{5}{6} = \frac{4}{7}$ ,  $\frac{5}{14}$ ,  $\frac{6}{85}$ .  
 $(\frac{4}{7}, \frac{5}{14}, \frac{6}{85}) \times 70 = 40$ , 25, 12,  $40 + 25 + 12 = 77$ .

$$\frac{40}{77} \times \frac{355}{1} = 3560 \text{ lbs.}$$

$$\frac{25}{77} \times \frac{655}{1} = 2225 \text{ lbs.}$$

$$\frac{12}{77} \times \frac{655}{1} = 1068 \text{ lbs.}$$

4. Two persons join in purchasing some property, one paying \$1250, and the other \$1000. If the property rise in value to \$3600, what will be the value of each one's share?

\$ 1000 + \$ 1250 = \$ 2250.  

$$\frac{200}{2230} \times \frac{8}{3600} = $ 1600.$$

$$\frac{250}{2230} \times \frac{8}{3600} = $ 2000.$$

5. Gun-metal is composed of 3 parts (by weight) of tin to 100 parts of copper. What weight of each of these metals will there be in cannon weighing 721 lbs.?

$$3 + 100 = 103.$$

$$\frac{3}{103} \times \frac{721}{1} = 21 \text{ lbs. tin.}$$

$$\frac{100}{103} \times \frac{721}{1} = 700 \text{ lbs. cop.}$$

6. Bell-metal contains 78 parts copper and 22 parts tin. What weight of each of these metals will there be in a bell weighing 937 lbs.?

$$78 + 22 = 100$$
.  
 $\frac{78}{100} \times 937 = 730.86$  lbs. copper.  
 $\frac{78}{100} \times 937 = 206.14$  lbs. tin.

7. It takes 75% of saltpetre, 12.5% of charcoal, and 12.5% of sulphur to make 100% of powder. How much of each of these substances will be required to make 10,000,000 cartridges, each containing 5% of powder?

$$75 + 12\frac{1}{3} + 12\frac{1}{3} = 100.$$

$$10,000,000 \times 5^{g} = 50,000,000^{g} = 50,000^{kg}.$$

$$\frac{75}{199} \times \frac{500}{1} = 37,500^{kg} \text{ saltpetre.}$$

$$\frac{125}{1999} \times \frac{50}{1} = 6250^{kg} \left\{ \begin{array}{l} \text{charcoal.} \\ \text{sulphur.} \end{array} \right.$$

opper contains 2 parts of red copper and 1 part sinc. notes of red copper are there in an article weighing 1 lb. r copper?

1 lb. = 16 oz,  

$$2 + 1 = 3$$
.  
 $2 \times \frac{14}{3} = \frac{3}{3} = 10 \frac{1}{3}$  os. Ans.

tal is made of an alloy containing 39 parts of lead to ony. How many pounds of each will be required to of type?

$$39 + 11 = 50$$
,  
 $\frac{28}{15} \times \frac{257}{1} = \frac{27832}{50} = 748.46$  lbs. lead.  
 $\frac{11}{10} \times \frac{257}{10} = \frac{10527}{10527} = 210.54$  lbs. antimony.

10. Plumber's solder contains 2 parts lead and 1 part tin. How much of each of these in 100 lbs. of solder?

$$2 + 1 = 3$$
.  $\frac{2}{3} \times 100 = 66\frac{2}{3}$  lbs. lead.  $\frac{1}{3} \times 100 = 33\frac{1}{3}$  lbs. tin.

11. The air is composed of oxygen and nitrogen. In 100 volumes of air there are 21 volumes of oxygen and 79 of nitrogen. Reckoning the weight of a liter of oxygen to be 1.4295s, that of a liter of nitrogen 1.2577s, find the number of grams of each gas in 100s of air.

$$21 \times 1.4295 = 30.0195.$$
 $79 \times 1.2577 = 99.3583.$ 
 $30.0195 + 99.3583 = 129.3778.$ 

$$\frac{300195}{1293778} \text{ of } 100^{\circ} = \frac{30019500^{\circ}}{1293778} = 23.203^{\circ} \text{ O.}$$

$$100^{\circ} - 23.203^{\circ} = 76.797^{\circ} \text{ H.}$$

12. What is the value of the gold in a chain weighing 3 oz. 4 dwt., supposing it to be 18 carats fine (that is, 18 parts of pure gold out of 24), at \$19 an ounce?

3 oz. 4 dwt. = 
$$3\frac{1}{5}$$
 oz.  
 $3\frac{1}{5} \times $19 = $60\frac{2}{5}$ .  
 $\frac{18}{10}$  of  $$60\frac{2}{5} = $45.60$ . Ans.

#### EXERCISE LXVI.

1. Arnold and Baker enter into partnership. Arnold puts in \$6000 for 8 months, and Baker \$4000 for 6 months. Their profits are \$2000. What is each man's share?

$$8 \times \$6000 = \$48,000.$$
 $6 \times \$4000 = \$24,000.$ 
 $48,000 + 24,000 = 72,000.$ 

$$\frac{2}{72999} \times \frac{\$2000}{1} = \$1333.33, A's.$$

$$\frac{24999}{72999} \times \frac{\$2000}{1} = \$666.67, B's.$$

2. Dobson furnishes the firm of Dobson & Fogg with \$5000 for 13 months; Fogg furnishes \$7000 for 9 months. Their profits are \$1700. What is the share of each?

$$13 \times $5000 = $65,000$$
,  $9 \times $7000 = $63,000$ ,  $65,000 + 63,000 = 128,000$ ,  $\frac{65}{425} = \frac{425}{129999} \times \frac{$1199}{1} = \frac{$37625}{32} = $863.28$ , Dobson's,  $\frac{128}{32}$   $\frac{32}{32}$ 

\$. In a business speculation, A furnishes \$800, and after 3 months \$250 more; B furnishes \$950, and at the end of 2 months withdraws \$200; C furnishes \$650, and at the end of 6 months \$400 more. At the end of a year they realize a profit of \$2516. How shall it be divided among them?

A B. C.
$$12 \times \$800 = \$9600 \qquad 12 \times \$950 = \$11400 \qquad 12 \times \$650 = \$7800$$

$$9 \times 250 = 2250 \qquad 10 \times 200 = 2000 \qquad 6 \times 400 = 2400$$

$$\$11,850 + \$9400 + \$10,200 = \$31,450.$$

$$\frac{\$}{1} = \$948, A's. \qquad \frac{9499}{81459} \times \frac{\$2516}{1} = \$752, B's.$$

$$\frac{204}{19299} \times \frac{\$2516}{81459} \times \frac{\$2516}{1} = \$752, B's.$$

$$\frac{204}{19299} \times \frac{\$2516}{81459} \times \frac{\$2516}{1} = \$816, C's.$$

hers, A and B, begin business with capitals of \$3500 A is to have 0.12 of the profits for managing the shall a profit of \$1906.25 be divided between them?

$$25 = $228.75$$
.  $$1906.25 - $228.75 = $1677.50$ .  $3500 + 8700 = 12200$ .

$$\begin{array}{c} 35 \\ \frac{$\$\$99}{12299} \times \frac{$2355}{2} = $481.25, \\ 122 \end{array}$$

5. A puts \$2100 into a business, and B \$1750. At the end of a year each puts in \$700 more, and C joins them with \$2500. At the end of 18 months from this time how shall a profit of \$2166.50 be divided?

A. B. C. 
$$30 \times \$2100 = \$63,000 \quad 30 \times \$1750 = \$52,500 \quad 18 \times \$2500 = \$45,000.$$
 $18 \times 700 = 12,600 \quad 18 \times 700 = 12,600$ 
 $\$75,600 \quad \$65,100$ 

$$7560 + 65,100 + 45,000 = 185,700.$$

$$63$$

$$189$$

$$756$$

$$14$$

$$651$$

$$65100$$

$$\$216650$$

$$\frac{756}{75699} \times \frac{14}{$216659} = $882, A's. \qquad \frac{651}{65199} \times \frac{7}{$216659} = $759.50, B's. \\
\frac{46425}{15475} = 3$$

$$\begin{array}{c}
3 \\
15 \\
459 \\
45909 \\
185709 \\
8190 \\
1238
\end{array}$$
175
$$\begin{array}{c}
175 \\
8216659 \\
199 \\
199 \\
1238
\end{array}$$
= \$525, C's.

6. Three graziers hire a pasture, for which they pay \$132.50. One puts in 10 oxen for 3 months, another 12 oxen for 4 months, and the third 14 oxen for 2 months. How much of the rent ought each to pay?

$$3 \times 10 = 30 
4 \times 12 = 48 
2 \times 14 = 28 
\hline
106$$

$$\frac{12}{48} \times \frac{125}{13259} = $60. (2)$$

$$\frac{15}{199} \times \frac{125}{199} \times \frac{5}{13259} = $60. (2)$$

$$\frac{7}{199} \times \frac{125}{199} \times \frac{5}{13259} = $35. (3)$$

The manuse manuscript with a manuse of \$2000, on the 18th of Alarm and or has the course manuse I we approxime with a court and the Jack II has revocate the \$45. When a time object each?

A A said B join maintee in the many Tall. At the end of I mountee A wholevery if his said B \(\frac{1}{2}\) if his and after 11 mounts move they have a pends if \$504550. What is the share of each?

9 s. among three persons, so that the first may have was as the second has shillings; and the second as the third has pounds.

1st has 2½ times as much as 2d. 2d has ½½ as much as 3d.

148.50 - \$1537.50 - \$3311, B's.

3d has 1 part.

2d has 
$$\frac{21}{10}$$
 part.

1st has  $\frac{21}{10}$  part.

3d has 40 parts.

2d has 42 parts.

1st has 105 parts.

1st has 105 parts.

All have 187 parts.

£65 9 s. = 1309 s.

$$\frac{7}{187} \times \frac{7}{1} = 294 s. = £14 14 s.$$

$$\frac{40}{187} \times \frac{7}{1} = 280 s. = £14.$$

10. Two partners begin business each with a capital of \$2000. A adds \$500 at the end of 2 months, and \$500 at the end of 7 months; B adds \$800 at the end of 3 months. What is the share of each, at the year's end, of a profit of \$3605.25?

$$12 \times \$ \ 2000 = \$ \ 24000$$

$$10 \times 500 = 5000$$

$$5 \times 500 = 2500$$

$$\$ \ 31500$$

$$31,500 + 31,200 = 62,700.$$

$$21 \atop 315 \atop 31599 \times $345 \atop 52799 \times $389525 \atop 199 \times $1811.25, A's.$$

$$\$ \ 3605.25 - \$ \ 1811.25 = \$ \ 1794, B's.$$

## EXERCISE LXVII.

1. The population of a town in 1870 was 12,275, and it increased 8% in the next ten years. Find its population in 1880.

If 100 represent the population in 1870, then 108 will represent the population in 1880.

$$\frac{27}{199} \text{ of } \frac{491}{1} = 13,257. \text{ Ans.}$$

2. How much metal will be obtained from 365 tons of ore, if the metal be 7% of the ore?

If 100 represent the ore, then 7 will represent the metal in the ore.

$$\frac{7}{199}$$
 of  $\frac{73}{1} = \frac{511}{20} = 25.55$  tons. Ans.

3. If gunpowder contains 75% of saltpetre, 10% of sulphur, 15% of charcoal, how much of each is there in a ton of gunpowder?

If 100 represent the gunpowder, then 75, 10, and 15 will represent respectively the saltpetre, sulphur, and charcoal.

$$\frac{75}{199} \times \frac{20}{1} = 1500 \text{ lbs. saltpetre.}$$

$$\frac{10}{199} \times \frac{20}{1} = 200 \text{ lbs. sulphur.}$$

$$\frac{15}{199} \times \frac{20}{1} = 300 \text{ lbs. charcoal.}$$

4. A manufactory uses 24 tons of coal a day, and 20% of it is lost in smoke. How much coal would be needed if this waste could be prevented?

If 100 represent the number of tons of coal used, then 20 will he number of tons lost in smoke.

$$-\frac{24}{5}$$
 = 4.8 t. 24 t. - 4.8 t. = 19.2 t. Ans.

s of 20.0265% (by measure) of oxygen gas and agen. How much oxygen in 1750 cu. ft. of air? sent the number of cubic feet of air, then 20.0265 ent the number of cubic feet of oxygen.

- 6. A town, after decreasing 25%, has 4539 inhabitants. Find its number at first.
  - If 100 represent the population at first, then 75 will represent the population now.

$$\frac{4}{190} \times \frac{1513}{4539} = 6052. Ans.$$

- 7. 2% of a regiment of 750 men are killed in an engagement, 6% are wounded, and 4% are missing. What is the number still available for service?
  - If 100 represent the number of men in the regiment then 2, 6, and 4 will represent the number, killed, wounded, and missing.

- 8. If 3\frac{3}{4} tons of sulphur are required to make 31\frac{1}{4} tons of gunpowder, what is the per cent of sulphur in gunpowder?
  - If 100 represent the whole weight, then the number required to represent  $3\frac{3}{4}$  tons of sulphur will be  $\frac{3\frac{3}{4}}{31\frac{1}{4}}$  of 100 = 12.

    That is, 12%. Ans.
- 9. In a school of 80 children,  $17\frac{1}{2}\%$  are girls. Find the number of boys.
  - If 100 represent the number of scholars in the school, then  $100-17\frac{1}{2}$ , or  $82\frac{1}{2}$ , will represent the number of boys in the school.

$$\frac{821}{100} \text{ of } 80 = \frac{165}{2} \times \frac{1}{100} \times \frac{80}{1} = 66 \text{ beys. } Ans.$$

10. If goods are bought for \$415, and sold for \$500, what is the gain per cent?

$$$500 - $415 = $85$$
, actual gain.

Since the gain on \$415 is \$85, the gain on 100 is

$$\frac{100}{415} \text{ of } \frac{35}{1} = 2049\%. \quad \therefore \text{ the gain is } 2049\%. \quad Ans.$$

11. If goods are bought for \$415, and sold for \$400, what is the loss per cent?

\$415 - \$400 - \$15, actual loss.

Since the loss on \$415 is \$15, the loss on 100 is

$$\frac{100}{415} \text{ of } \frac{3}{15} = 3\frac{1}{5}. \quad \therefore \text{ the loss is } 3\frac{5}{5}\frac{1}{5}\%. \text{ Ans.}$$

12. \$500 is 4% of what number?

If 4 represent \$500, 100 will represent  $\frac{190}{4}$  of \$500 = \$12,500.

13. A farmer buys 24 head of cattle at \$80 a head, and, after losing 6, sells the remainder at \$105 a head. How much does he gain or lose per cent?

24 head of cattle at \$80 per head cost \$1920.

18 head of cattle at \$105 per head cost \$1890.

\$1920 - \$1890 = \$30, actual loss.

Since the loss on \$1920 is \$30, the loss on 100 is

$$\frac{25}{199} \frac{199}{1929} \text{ of } \frac{39}{1} = 1_{16}^{9}. \therefore \text{ he loses } 1_{16}^{9}\%. \text{ Ans.}$$

14. If a ton (2240 lbs.) of ore in a gold mine yield 5 oz. (troy) of gold, what is the yield per cent?

5 oz. troy =  $\frac{5}{12}$  lbs. troy =  $\frac{5}{12}$  of  $\frac{7000}{5760}$  lbs. av. =  $\frac{12}{35}$  lb. av.

If 100 be taken to represent the ore, the number required to represent the metal will be

$$\frac{\frac{12}{15}}{2240} \text{ of } 100 = \frac{1}{2249} \times \frac{3}{25} \times \frac{199}{1} = \frac{3}{196}. \text{ That is, } \frac{3}{196} \text{ of } 1\%. \text{ Ans.}$$

15. If the ore in a mine yields  $\frac{3}{80}$  of 1% of pure gold, how many tons (2240 lbs.) of ore must be taken to obtain 7 lbs. (troy) of gold?

7 lbs. troy =  $7 \times \frac{5760}{7000}$  lbs. av. =  $5\frac{19}{25}$  lbs. av.

If 100 be taken to represent the ore,  $\frac{3}{80}$  will represent the gold in the ore. If  $\frac{3}{80}$  represent  $5\frac{19}{25}$  lbs., 100 will represent

$$\left(\frac{100}{\frac{3}{80}} \text{ of } 5\frac{19}{25}\right) \text{ lbs. or } \frac{\frac{100}{3} \text{ of } 5\frac{19}{25}}{2240} \text{ tons } = \frac{\cancel{100}}{\cancel{1}} \times \frac{\cancel{30}}{\cancel{3}} \times \frac{\cancel{144}}{\cancel{25}} \times \frac{\cancel{14$$

16. 12½ tons of iron are obtained from 235 tons of ore. What per cent of the ore is iron?

If 100 be taken to represent the whole weight of the ore, the number required to represent 12½ tons will be

$$\frac{12\frac{1}{2}}{235} \text{ of } 100 = \frac{25}{47} \times \frac{1}{235} \times \frac{50}{1} = 5\frac{15}{47}. \text{ That is, } 5\frac{15}{47}\%. \text{ Ans.}$$

17. Goods are sold, at a loss of 3%, for \$2667.50. What was the cost?

If 100 be taken to represent the cost, 100 - 3 = 97 will represent the selling price. Therefore the selling price was  $\frac{100}{97}$  of \$2667.50 = \$2750. Ans.

18. Teas at 68 cents, 86 cents, and 96 cents a pound, are mixed in equal quantities, and sold at 90 cents a pound. Find the gain per cent.

$$\frac{68+86+96}{3} = 83\frac{1}{3}$$
 cost per lb.  $90-83\frac{1}{3}=6\frac{2}{3}$ , actual gain.

Since the gain on  $83\frac{1}{3}$  cents is  $6\frac{2}{3}$  cents, the gain on 100 is  $\frac{100}{83\frac{1}{3}}$  of  $6\frac{2}{3}=8$ . That is, 8%. Ans.

19. By selling goods for \$1173.92, a merchant gains \$153.12. Find the gain per cent on the cost.

\$1173.92 - \$153.12 = \$1020.80, cost.

Since the gain on \$1020.80 is \$153.12, the gain on 100 is  $\frac{100}{1020.80}$  of 153.12 = 15. That is, 15%. Ans.

20. If to 25 gals. of alcohol 2 gals. of water are added, how much per cent of the mixture is water? how much per cent is alcohol?

25 + 2 = 27 gals., the whole amount.

If 100 be taken to represent the whole amount, the number required to represent 2 gals. will be  $\frac{2}{27}$  of  $100 = 7\frac{1}{27}$ . That is,  $7\frac{1}{2}$ % water. Ans.

 $100 - 7\frac{1}{2} = 92\frac{1}{2}$ % alcohol. Ans.

21. What was the cost when 17½% was gained by selling goods for \$253.80?

If 100 be taken to represent the cost,  $100 + 17\frac{1}{2} = 117\frac{1}{2}$  will represent the selling price.

Therefore, the cost was  $\frac{100}{117\frac{1}{2}}$  of \$253.80 = \$216. Ans.

22. A wine merchant mixes 24 gallons, at \$7 a gallon, with 18 gallons, at \$5 a gallon, and sells the whole at \$7 a gallon. What does he gain per cent?

 $24 \times \$7 + 18 \times \$5 = \$168 + \$90 = \$258$ , cost.

24 + 18 = 42, whole number of gallons.

 $42 \times \$7 = \$294$ , selling price.

\$294 - \$258 = \$36, actual gain.

Since the gain on \$258 is \$36, the gain on 100 is  $\frac{1}{2}$  of 36 = 13. That is,  $13\frac{1}{2}$ %. Ans.

23. By selling a horse for \$200, a dealer loses 12½%. What would he have gained or lost per cent by selling at \$250?

If 100 be taken to represent the selling price,  $100 - 12\frac{1}{2} = 87\frac{1}{2}$  will represent the cost.

Therefore the cost was  $\frac{100}{87\frac{1}{2}}$  of \$200 = \$228\$.

\$250 - \$2284 = \$214, gain by selling at \$250.

Since the gain on \$228‡ would have been \$21‡, the gain on 100 would have been  $\frac{100}{228‡}$  of 21‡ = 9‡. That is, 9‡% gain. Ans.

24. A spirit merchant buys 75 gals., at \$3.25 a gallon, and, after drawing off 10 gals., sells the remainder so as to gain 5% on the whole. What is the selling price per gallon?

 $75 \times $3.25 = $243.75$ , cost.

If 100 be taken to represent the cost, 100 + 5 = 105 will represent the selling price.

Therefore, the selling price is  $\frac{188}{188}$  of \$243.75 = \$255.93\.

75 gals. -10 gals. =65 gals., number sold.

 $\frac{$255.93\frac{3}{4}}{65} = $3.93\frac{3}{4}$ , selling price per gallon. Ans.

25. A person owns two estates worth respectively \$9845 and \$12,155. If the first rise in value 32%, and the second fall 13%, determine the rise or fall per cent in the value of his whole property.

If 100 be taken to represent the value of the first estate at first, 100 + 32 = 132 will represent its value after rising 32%.

Therefore, the value after rising is  $\frac{132}{130}$  of \$9845 = \$12,995.40.

If 100 be taken to represent the value of the second estate at first, 100 - 13 = 87 will represent its value after falling 13%.

Therefore, the value after falling is  $\frac{87}{100}$  of \$12,155 = \$10,574.85.

\$9845 + \$12,155 = \$22,000, value of the estates at first.

12,995.40 + 10,574.85 = 23,570.25, value afterwards.

23,570.25 - 22,000 = 1570.25, actual gain.

Since the gain on \$22,000 is \$1570.25, the gain on 100 is  $\frac{1000}{22000}$  of \$1570.25 =  $7\frac{1}{80}$ . That is,  $7\frac{1}{80}$ % gain. Ans.

26. A tradesman marks an article \$5, but takes off 5% for cash. If his profit is 14%, what was the cost of the article?

If 100 be taken to represent the marked price, 100-5=95 will represent the actual price.

Therefore, the actual price was  $\frac{100}{95}$  of \$5 = \$4.75.

If 100 be taken to represent the cost, 100 + 14 = 114 will represent the price.

Therefore, the cost was  $\frac{100}{114}$  of \$4.75 = \$4.16\frac{2}{3}\$. Ans.

27. What would a dishonest dealer gain per cent by using a false weight of 15 oz. instead of a pound?

16 oz. -15 oz. = 1 oz., actual gain.

Since the gain on 15 oz. is 1 oz., the gain on 100 is  $\frac{1}{15}$  of 100 = 6 $\frac{2}{5}$ . That is, 6 $\frac{2}{5}$ %. Ans.

28. A dishonest dealer gains 12% by using false weights. What is the real weight of his pound?

If 100 be taken to represent the false weight of a pound, 100 + 12 - 112 will represent the true weight of a pound. Therefore, the false weight is  $\frac{1}{1}$  of 16 oz. -14 oz. Ass.

29. A tradesman, in selling goods, deducts from the marked price 5% for cash. What is the marked price of some goods for which he receives \$7.121?

If 100 be taken to represent the marked price, 100 - 5 = 95 will represent the actual price.

Therefore, the marked price is  $\frac{100}{100}$  of \$7.12\frac{1}{2} = \$7.50. Ans.

30. The lead ore from a certain mine yields 60% of metal, and of the metal \(\frac{1}{4}\) of 1% is silver. How much silver and lead will be obtained from 1200 tons of ore?

If 100 be taken to represent the ore, 60 will represent the metal. Therefore, the amount of metal is  $\frac{60}{100}$  of 1200 t. = 720 t.

If 100 be taken to represent the metal, ‡ will represent the silver.

Therefore, the amount of silver is  $\frac{3}{100}$  of 720 = 5.4 t. Ans. 720 t. -5.4 t. = 714.6 t., lead. Ans.

31. If ore loses 411% of its weight in reasting, and 431% of the remainder in smelting, how much ore will be required to yield 1000 tons of metal?

If 100 be taken to represent the ore,  $100 - 41\frac{1}{2} = 58\frac{1}{2}$  will represent the ore after roasting.

 $6\frac{1}{4}$  represent the ore after roasting,  $58\frac{1}{4} - 43\frac{1}{4}\%$  of  $58\frac{1}{4} - 32\frac{1}{4}\frac{1}{4}$  rill represent the ore after smelting.

refore,  $\frac{32\frac{32}{100}}{100}$  t. will be the amount of metal in 1 ton of ore,

and  $\frac{1000}{32\frac{32}{100}}$  t. = 3038.936 t. will be the amount of ore required to

take 1000 tons of metal. Ans.

32. How many per cent above cost must a man mark his goods in order to take off 10%, and still make a profit of 17%?

If 100 be taken to represent the cost, the selling price will be represented by 117.

As the selling price is to be 10% below the marked price, the selling price (117) will be  $\frac{90}{100}$  of the marked price.

Therefore, the marked price will be  $\frac{100}{90}$  of 117 = 130.

That is, the goods must be marked 30% above cost. Ans.

33. How many per cent above cost must a man mark his goods in order to take off 12½%, and still make a profit of 12½%?

If 100 be taken to represent the cost, the selling price will be represented by 112½.

As the selling price is to be  $12\frac{1}{2}$ % below the marked price, the selling price (112\frac{1}{2}) will be  $\frac{87\frac{1}{2}}{100}$  of the marked price.

Therefore, the marked price will be  $\frac{100}{87\frac{1}{2}}$  of  $112\frac{1}{2} = 128\frac{4}{2}$ .

That is, the goods must be marked 28‡% above cost. Ans.

34. How many per cent above cost must a man mark his goods in order to take off 15%, and still make a profit of 15%?

If 100 be taken to represent the cost, the selling price will be represented by 115.

As the selling price is to be 15% below the marked price, the selling price (115) will be  $\frac{85}{100}$  of the marked price.

Therefore, the marked price will be  $\frac{100}{85}$  of  $115 = 135 \frac{5}{17}$ .

That is, the goods must be marked  $35_{17}$ % above cost. Ans.

35. How many per cent above cost must a man mark his goods in order to take off 33\frac{1}{3}\%, and still make a profit of 33\frac{1}{3}\%?

If 100 be taken to represent the cost, the selling price will be represented by 1331.

As the selling price is to be  $33\frac{1}{3}\%$  below the marked price, the selling price (133 $\frac{1}{3}$ ) will be  $\frac{66\frac{2}{3}}{100}$  of the marked price.

Therefore, the marked price will be  $\frac{100}{66\frac{2}{3}}$  of  $133\frac{1}{3} = 200$ .

That is, the goods must be marked 100% above cost. Ans.

36. If 5% of the population of a town has been the increase in the preceding ten years, what per cent of the population ten years ago has been added?

If 100 be taken to represent the population, the population 10 years ago will be represented by 95.

Since the gain on 95 is 5, the gain on 100 is  $\frac{149}{15}$  of  $5 = 5\frac{1}{15}$ . That is,  $5\frac{1}{15}$ %. Ans.

37. If, in a population of 27,000,000, 13% are foreign-born, how many foreign-born are there? What is the ratio of the foreign-born to the native?

If 100 be taken to represent the population, 13 will represent the foreign-born population.

Therefore, the foreign-born population is  $\frac{13}{100}$  of 27,000,000 = 3,510,000 (1). 13%:87% = 13:87. (2) Ans.

38. A man bought a horse for \$70, and sold him for \$80. What per cent did he gain? What per cent of the money received for the horse was gained?

\$80 - \$70 - \$10 actual gain.

Since the gain on \$70 is \$10, the gain on 100 is  $\frac{1}{2}$ \$ of 100 = 14\$. That is,  $14\frac{1}{4}$ %. (1) Ans.

Since the gain on \$80 is \$10, the gain on 100 is  $\frac{14}{18}$  of 100 = 12. That is,  $12\frac{1}{4}\%$ . (2) Ans.

39. If, by selling goods for 12½ per cent profit, a merchant clears \$800, what was the cost of the goods, and for how much were they sold?

If  $12\frac{1}{2}$  represent \$800, 100 will represent  $\frac{100}{12\frac{1}{4}}$  of \$800 = \$6400, cost. \$6400 + \$800 = \$7200, selling price. Ans.

A man selling eggs at 40 cents a dozen clears 331% on the what was the cost? Another, selling at the same price, clears, of his receipts; what did his eggs cost?

If 100 be taken to represent the cost, 133\ will represent the selling price.

Therefore the cost was  $\frac{100}{133\frac{1}{8}}$  of 40 cents = 30 cents. (1) Ans.

If 100 be taken to represent the selling price, 66% will represent the cost.

Therefore, the cost was  $\frac{66\frac{2}{3}}{100}$  of 40 cents =  $26\frac{2}{3}$  cents. (2) Ans.

41. By selling a carriage for \$117, a carriage-maker lost 10% of the cost. What ought he to have sold it for to make 10%?

If 100 be taken to represent the cost, 90 will represent the selling price.

Therefore, the cost was  $\frac{100}{90}$  of \$117 = \$130.

If 100 be taken to represent the cost, 110 will represent the price at which he ought to have sold it.

Therefore, the selling price ought to have been  $\frac{118}{108}$  of \$130 = \$143.

42. A man gained in January 3% in weight, and in February lost 3%. What per cent of his weight on the first day of January is his weight on the first day of March?

If 100 be taken to represent his weight Jan. 1, 103 will represent it Feb. 1.

If 100 be taken to represent his weight Feb. 1, 97 will represent it March 1.

Therefore, his weight March 1 was  $\frac{97}{100}$  of  $103 = 99\frac{91}{100}$ .  $99\frac{91}{100}$  is  $99\frac{91}{100}$ % of 100. Ans.

43. 7 lbs. of a certain article lose 3 oz. in weight by drying. What per cent of the original weight is water?

7 lbs. = 112 oz.

If 100 be taken to represent the whole weight, the number required to represent 3 oz. is  $\frac{3}{112}$  of  $100 = 2\frac{19}{28}$ .

That is, 218%. Ans.

44. 7 lbs. of a dry article have lost 3 oz. by drying. What per cent of the original weight was water?

7 lbs. = 112 oz. 112 oz. + 3 oz. = 115 oz., whole weight.

If 100 be taken to represent the whole weight, the number required to represent 3 oz. is  $\frac{3}{115}$  of  $100 = 2\frac{14}{25}$ .

That is,  $2\frac{14}{23}\%$ . Ans.

45. A dry article was exposed to damp air, and absorbed 3 oz. of water; it then weighed 7 lbs. What per cent of its present weight is water?

7 lbs. = 112 oz.

If 100 be taken to represent the whole weight, the number required to represent 3 oz. is  $\frac{3}{112}$  of  $100 = 2\frac{19}{23}$ .

That is,  $2\frac{19}{28}\%$ . Ans.

46. If rosin is melted with 20% of its weight of tallow, what per cent of tallow does the mixture contain?

If 100 be taken to represent the rosin, 120 will represent the mixture.

Therefore, the tallow will be represented by  $\frac{20}{120}$  of  $100 = 16\frac{2}{3}$ . That is,  $16\frac{2}{3}\%$ . Ans.

47. If 20% of a mixture of tallow and rosin is tallow, what per cent of the weight of the rosin is the weight of the tallow?

If 100 be taken to represent the mixture, 100 - 20 = 80 will represent the rosin.

If 80 is 100%. 20 is  $\frac{2}{8}\%$  of 100% = 25%. Ans.

48. How many pounds of tallow must be mixed with 8½ lbs. of rosin in order that the mixture may contain 15% of tallow?

If 100 be taken to represent the mixture, 100 - 15 = 85 will represent the rosin.

If 85 represent  $8\frac{1}{2}$  lbs., 15 will represent  $\frac{15}{85}$  of  $8\frac{1}{2}$  lbs. =  $1\frac{1}{2}$  lb.

49. Nitrogen gas, under standard pressure and temperature, is } of 1% of the weight of an equal volume of water. What is its specific gravity?

If 100 be taken to represent the water,  $\frac{1}{8}$  will represent nitrogen. Therefore, the specific gravity of nitrogen is  $\frac{\frac{1}{8}}{100} = 0.00125$ . Ans.

50. Oxygen gas is  $\frac{1}{7}$  of 1% of the weight of an equal volume of water; what is its specific gravity? How many gallons of oxygen will it take to weigh as much as a pint of water? How many of nitrogen?

If 100 be taken to represent water, } will represent oxygen.

Therefore, the specific gravity of oxygen is  $\frac{1}{100} = \frac{1}{700}$ . (1) Ans.

As 1 gal. of oxygen weighs  $\frac{1}{700}$  of a gallon of water, it will take as many gallons of oxygen to weigh as much as a pint of water as  $\frac{1}{700} = 87\frac{1}{2}$  gals. (2) Ans.

As 1 gal. of nitrogen weighs 0.00125 of a gallon of water, it will take as many gallons of nitrogen to weigh as much as a pint of water as  $\frac{1}{0.00125} = 100$  gals. (3) Ans.

51. If common air consist of 4 volumes of oxygen to 13 of nitrogen, what is its specific gravity?

4 volumes of oxygen =  $4 \times \frac{1}{700} = \frac{1}{175}$ .

13 volumes of nitrogen =  $13 \times \frac{1}{800} = \frac{18}{800}$ .

 $\frac{1}{175} + \frac{13}{500} = \frac{123}{5600}$ , for 17 volumes.

Therefore, the specific gravity is  $\frac{1.28}{5600} + 17 = 0.00129$ . Ans.

- 52. How many gallons of air weigh as much as a pint of water?

  As 1 gallon of air weighs 0.00129 of a gallon of water, it will take as many gallons of air to weigh as much as a pint of water as  $\frac{1}{0.00129} = 96\frac{11}{12}\frac{6}{9}$  gals. Ans.
- 53. If by heating iron 185° F. it expands  $\frac{1}{2}$  of 1%, what will be the expansion of iron in passing from  $-20^{\circ}$  F. to  $+120^{\circ}$  F.?

The difference between  $-20^{\circ}$  and  $+120^{\circ}$  is 140°.

If  $\frac{1}{3}$  of 1% is the expansion for 185°, the expansion for 140° is  $\frac{149}{148}$  of  $\frac{1}{3}$  of 1% =  $\frac{7}{14}$  of 1%. Ans.

54. A tubular iron bridge is 450 ft. long, and one end is fast to a pier. How much play must be allowed at the other end, if the iron expands at the above rate, and if the climate varies from  $-30^{\circ}$  F. in winter to  $+130^{\circ}$  F. in a July sun?

The difference between  $-30^{\circ}$  and  $+130^{\circ}$  is 160°.

If  $\frac{1}{3}$  of 1% is the expansion for 185°, the expansion for 160° is  $\frac{160}{185}$  of  $\frac{1}{3}$  of 1% =  $\frac{4}{37}$  of 1%.

 $\frac{4}{37}$  of 1% of 450 ft. is  $\frac{1}{3}$  ft. =  $5\frac{3}{37}$  in. Ans.

55. How much longer is 100 miles of iron rail at 118° F, than at 20° below zero?

The difference between  $-20^\circ$  and  $+118^\circ$  is  $138^\circ$ . If  $\frac{1}{1}$  of 1% is the expansion for  $185^\circ$ , the expansion for  $138^\circ$  is  $\frac{118}{148}$  of  $\frac{1}{1}$  of  $1\% = \frac{1}{140}$  of 1%.

#### EXERCISE LXVIII.

- 1. Find the brokerage, at  $\frac{1}{2}$  of 1%, to be paid on \$10,450. \$10,450 × 0.00 $\frac{1}{2}$  = \$13.06. Ans.
- 2. Find the commission on \$2595, at  $2\frac{1}{1}$ %. \$2595 \times 0.025 = \$64.88. Ans.
- 3. An agent sells 200 bbls. of flour, at \$6.25; 600 gals, molasses, at 65 cents; and charges a commission of 1½%. What are the net proceeds?

emmission merchant received \$1640 with which to buy deducting a commission of 2½%. What is the amount of saion, and how many bushels of corn at 62½ cents a bushel ??

be taken to represent the amount to be paid for the goods, will represent the \$1640. Therefore, the amount ex-

ded for goods will be  $\frac{100}{1021}$  of \$ 1640 = \$ 1600.

21% of \$1600 - \$40, commissions. (1) Ane.

bu. - 2560 bu. can be bought for \$1600. (2) Ans.

5. A commission merchant sells a consignment of cotton for \$5216. He pays \$51 for freight and storage, and charges a commission of 2½%. What are the net proceeds?

Consignment = \$5216.00  
\$5216 
$$\times$$
 0.02\frac{1}{4} = \$117.36 = commission.  
Storage = 51.00  
Total expenses =  $\frac{168.36}{5047.64}$  = net proceeds. Ans.

6. A consignment of butter was sold for \$1570, of which \$1546.45 were the net proceeds. What was the rate per cent of commission?

\$1570 - \$1546.45 = \$23.55, commission.

If 100 be taken to represent the consignment, the number required to represent \$23.55 will be  $\frac{23.55}{1570}$  of  $100 = 1\frac{1}{2}$ .

That is,  $1\frac{1}{2}$ %. Ans.

7. What are the net proceeds from the sale of 2250 bbls. of flour, at \$6.25 a barrel, if the charges for freight and storage be 50 cents a barrel, commission for selling 2%, for guaranteeing payment 1½%?

$$2250 \times \$6.25 = \$14062.50$$
  
 $\$14062.50 \times 0.035 = \$492.19$   
 $2250 \times \$0.50 = 1125.00$   
Total expenses =  $\frac{1617.19}{\$12445.31} = \text{net proceeds. Ans.}$ 

8. A commission merchant sells 350 crates of peaches, at \$2.60. If the commission be 4½%, find the net proceeds.

$$350 \times \$ 2.60 = \$ 910.00$$
  
 $\$ 910 \times 0.045 = 40.95$   
 $\$ 869.05$ . Ans.

9. A man sells 420 acres of land, at \$40 an acre, and charges 1½% commission. What is his commission?

$$420 \times \$40 = \$16,800$$
  
 $\$16,800 \times 0.01\frac{1}{4} = \$210$ . Ans.

10. An agent, charging 4½% commission, receives for his services \$313. Find the amount of his sales.

If 
$$4\frac{1}{4}$$
 represent \$313, 100 will represent  $\frac{100}{4\frac{1}{2}}$  of \$313 = \$6955.56.

11. A merchant buys, through an agent, 730 yds. of carpeting, at \$1.25 a yard, and pays the agent \( \frac{1}{2} \) of 1% commission; the freight amounted to \$7.37. At what price per yard must the carpeting be sold to realize a profit of 20%?

 $730 \times $1.25 = $912.50$ .  $0.0075 \times $912.50 = $6.84$ , commission. \$912.50 + \$6.84 + \$7.37 = \$926.71, total expenses. If 100 represent the cost, 120 will represent selling price. Therefore, the selling price must be  $\frac{130}{100}$  of \$926.71 = \$1112.05. \$1112.05 + 730 = \$1.523. Ans.

12. An agent sells a consignment of goods for \$2100. He pays \$33.50 for freight, and, reserving his commission, remits \$2024.77. Find the rate of his commission.

\$2024.77 + \$33.50 = \$2058.27, consignment less commission.

\$2100 - \$2058.27 = \$41.73, commission.

If 100 be taken to represent the consignment, the number required to represent \$41.73 will be  $\frac{41.73}{2100}$  of  $100 = 1\frac{691}{700}$ .

That is, the commission was 1551%. Ans.

13. A commission merchant has consigned to him 5000 lbs. of cotton, which he sells at 14 cents a pound, and charges 2% commission. With the net proceeds he buys cotton cloth, at 10 cents a yard, charging 1½% commission for buying. How many yards of cloth does he buy?

$$5000 \times \$0.14 = \$700$$
  
 $\$700 \times 0.02 = 14$   
 $\$686 = \text{net proceeds.}$ 

If 100 be taken to represent the amount to be paid for the goods, 101.5 will represent the \$686.

Therefore, the amount expended for goods will be  $\frac{100}{101.5}$  of \$686 = \$675.86.

 $\frac{675.86}{0.10}$  = 6758.6 yds. can be bought for \$675.86, at \$0.10. Ans.

14. A commission merchant has consigned to him 500 bbls. of flour, which he sells at \$5.50 a barrel, and charges  $2\frac{1}{2}\%$  commission; the expenses for freight, etc., amounted to \$250. With the net proceeds he buys sugar, at  $6\frac{1}{4}$  cents a pound, charging  $2\frac{1}{2}\%$  commission for buying. How much sugar does he buy, and what is the amount of his commissions?

 $500 \times $5.50 = $2750.00$   $$2750 \times 0.025 = $68.75 = \text{commission.}$ Freight, etc. = 250.00 Total expenses = 318.75 \$2431.25 net proceeds.

If 100 be taken to represent the amount to be paid for the sugar,  $2\frac{1}{2}$  will represent the commission, and  $102\frac{1}{2}$  will represent the \$2431.25. Therefore, the amount expended for sugar will be  $\frac{100}{102\frac{1}{2}}$  of \$2431.25 = \$2371.95.

And  $2\frac{1}{2}$ % of \$2371.95 = \$59.30, commission.

Therefore,  $\frac{2371.95}{0.06\frac{1}{4}}$  lbs. = 37,951.2 lbs. will be bought. (1) Ans.

\$68.75 + \$59.30 = \$128.05, whole commission. (2) Ans.

15. A collector's commission for collecting taxes, at 1½%, is \$206.55. What was the sum collected?

If  $1\frac{1}{2}$  represent \$206.55, 100 will represent  $\frac{100}{1\frac{1}{2}}$  of \$206.55=\$13,770.

16. An agent received \$2961 with which to purchase goods after deducting his commission at 5%. How much was his commission?

If 100 be taken to represent the amount to be paid for the goods, 5 will represent the commission, and 105 will represent the \$2961. Therefore, the amount expended for the goods will be \frac{108}{108} of \$2961 = \$2820.

And 5% of \$2820 = \$141, commission. Ans.

17. An agent buys 3100 bbls. of flour, at \$4.50 a barrel, and charges 1½% commission. What is the amount of the bill, including the commission?

$$3100 \times \$4.50 = \$13,950.00$$
  
 $\$13,950 \times 0.015 = 209.25$   
 $\$14,159.25$ . Ans.

- 18. A broker receives \$6150 to invest in cotton, at 10½ cents a pound. His commission is 2½%. How many pounds of cotton can he buy?
  - If 100 be taken to represent the amount to be paid for the cotton, 102½ will represent the \$6150. Therefore, the amount expended for cotton will be  $\frac{100}{102½}$  of \$6150 = \$6000.
  - $\frac{6000}{0.10\frac{1}{4}}$  lbs. = 58,536 $\frac{24}{1}$  lbs. of cotton will be bought. Ans.
- 19. An agent sells 1100 bbls. of flour, at \$4.50 a barrel, and charges 2½% commission. He invests the proceeds in steel, at 1½ cents a pound, charging 1½% commission. What is his entire commission, and how many tons of steel (2240 lbs. to a ton) does he buy?

$$1100 \times \$4.50 = \$4950.00$$
  
 $\$4950 \times 0.025 = 123.75 = \text{commission.}$   
 $\$4826.25$ 

If 100 be taken to represent the amount to be paid for the steel,  $1\frac{1}{2}$  will represent the commission, and  $101\frac{1}{2}$  will represent the \$4826.25. Therefore, the amount expended for steel will be  $\frac{100}{101\frac{1}{2}}$  of \$4826.25 = \$4754.93.

And  $1\frac{1}{2}$ % of \$4754.93 = \$71.32, commission.

\$123.75 + \$71.32 = \$195.07, total commission. (1) Ans.

Therefore,  $\frac{4754.93}{0.015}$  lbs. = 316,995 $\frac{1}{8}$  lbs. = 141.51562 t. of steel will be bought. (2) Ans.

### EXERCISE LXIX.

1. Find the premium of fire insurance for \$2650, at 1 of 1%.

$$2650 \times 0.005 = 13.25$$
. Ans.

2. Find the premium to be paid for insuring a person's life for \$2500, at an age for which the rate is  $2\frac{1}{4}\%$ 

$$$2500 \times 0.02$$
 =  $$56.25$ . Ans.

3. At 23%, what premium of insurance will be paid on a vessel worth \$36,400?

$$36,400 \times 0.02 = 1001.00$$
. Ans.

- 4. A vessel is worth \$12,052. Determine the sum to be insured, and the premium to be paid at 1\frac{3}{4}\%, so that in the event of loss the owner may receive both the value of the vessel and the premium.
  - If 100 be taken to represent the sum to be insured,  $1\frac{3}{4}$  will represent the premium, and  $100 1\frac{3}{4} = 98\frac{1}{4}$  will represent the value of the vessel.

Hence, the sum to be insured will be

$$$12,052 + 0.98\frac{1}{2} = $12,266.67.$$

And  $1\frac{3}{4}\%$  of \$12,266.67 = \$214.67, premium. Ans.

5. The premium for insurance at 1½% is \$150. What is the amount insured?

If 
$$1\frac{1}{4}$$
 represent \$150, 100 will represent  $\frac{100}{1\frac{1}{4}}$  of \$150 = \$12,000.

6. If a premium of insurance at 2\frac{3}{4}\% amount to \$28.60, what is the sum insured?

If 
$$2\frac{3}{4}$$
 represent \$28.60, 100 will represent  $\frac{100}{2\frac{3}{4}}$  of \$28.60 = \$1040.

7. A vessel is so insured that if lost the owner may receive both the value of the vessel and the premium. The value of the vessel is \$96,084, and the rate of insurance 17%. Find the premium.

If 100 be taken to represent the sum to be insured,  $1\frac{7}{8}$  will represent the value of the vessel.

Hence, the sum to be insured will be \$96,084 +  $0.98\frac{1}{8}$  = \$97,920. And  $1\frac{7}{8}$  of \$97,920 = \$1836, premium. Ans.

8. A building worth \$8000 is insured at § of its value, at § of 1% per annum. What is the annual premium?

$$\frac{1}{3}$$
 of  $38000 = 5000$ .  
 $5000 \times 0.00 = 6.25$ . Ans.

9. Four companies join in insuring a ship and cargo for \$60,000. One company takes \(\frac{1}{2}\), at \(\frac{2}{3}\) of 1%; a second takes \\$10.000, at \(\frac{2}{3}\) of 1%; a fourth, the remainder, at \(\frac{1}{2}\) of 1%. How much is paid for insurance?

(1) (2) (3) (4)

$$\frac{1}{3}$$
 of \$60,000 = \$20,000. \$10000 \$15000 The remainder is

 $\frac{520000}{0.00\frac{3}{5}}$  \$75.00 \$93.75  $\frac{0.00\frac{1}{3}}{575.00}$ 

\$120 + \$75 + \$93.75 + \$75 = \$363.75, total premium. Ans.

10. If the ship in the last problem receive damage to the amount of \$4500, what ought each company to pay?

$$\frac{1}{6}$$
 of \$4500 = \$1500 (1).  
 $\frac{18888}{68886} = \frac{1}{6}$ .  $\frac{1}{6}$  of \$4500 = \$750 (2).  
 $\frac{1}{6}$   $\frac{1}{6}$ 

11. A man insures his life for \$10,000, paying \$350 a year in advance. He dies the day before the fifth premium was due. The company pay his widow \$10,000. How much have they lost by him, if the interest gained on the premiums paid amount to \$175?

 $4 \times $350 + $175 = $1575$ , total premiums with interest. \$10,000 - \$1575 = \$8425, company's loss. Ans.

12. A merchant shipped a cargo to London; and to cover both the cargo and the premium, he took out a policy of \$100,800, at  $3\frac{1}{2}$ %. What was the value of the cargo?

If 100 be taken to represent the sum insured,  $100 - 3\frac{1}{2} = 96\frac{1}{2}$  will represent the value of the cargo.

Hence, the value of the cargo is  $0.96\frac{1}{4}$  of \$100,800 = \$97,272.

13. Three companies insure, at \(\frac{2}{3}\) of its value, a building worth \(\frac{2}{3}\)16,000. The first company takes \(\frac{1}{3}\) the risk, at \(\frac{2}{3}\) of 1\%; the second, \(\frac{2}{3}\) of it, at \(\frac{7}{3}\) of 1\%; and the third, the remainder, at \(\frac{2}{3}\) of 1\%. Find the total premium.

$$\frac{2}{3}$$
 of \$16,000 = \$12,000.  
 $\frac{1}{3}$  of \$12,000 = \$4800.  
 $\frac{3}{4}$  of \$12,000 = \$4800.  
 $\frac{3}{4}$   $\frac{3}{4}$ 

14. S. Williams pays \$18.40 premium for insuring his house for \$\frac{2}{3}\$ of its value, at \$1\frac{1}{2}\%\$. What is the value of his house?

If  $1\frac{1}{2}$  represent \$18.40, 100 will represent  $\frac{100}{1\frac{1}{2}}$  of \$18.40 = \$1226\frac{2}{3}\$. If \$1226\frac{2}{3}\$ is \frac{2}{3}\$, the whole is \frac{2}{3}\$ of \$1226\frac{2}{3}\$ = \$1840\$. Ans.

## EXERCISE LXX.

1. If James Brown be assessed \$2500 on his house, and \$5200 on personal property, and pays for 2 polls at \$1.50 each, how much will his tax be, the rate being \$12.18 on \$1000?

$$$2500 + $5200 = $7700.$$
  
 $0.01218 \text{ of } $7700 = $93.79.$   
 $$93.79 + $3.00 = $96.79.$  Ans.

2. If the rate of tax be \$12.25 on \$1000, and the tax be \$11,788.50, what is the valuation?

12.25 on 1000 = 1.225%

If 1.225 represent \$11,788.50, 100 will represent  $\frac{100}{1.225}$  of \$11,788.50 = \$962,326.53. Ans.

3. If the assessed valuation of a town be \$1,777,000, and the property-tax be \$6870, what is the rate on \$1000?

\$6870 + \$1,777,000 = 0.003866.

That is, the rate is 0.3866 of 1%, or \$3.866 on \$1000. Ans.

4. What sum must be assessed, in order that \$15,000 shall remain after paying a commission of 2% for collecting the taxes?

If 100 be taken to represent the sum to be assessed, 98 will represent the \$15,000.

Therefore, the sum to be assessed is  $\frac{100}{8}$  of \$15,000 = \$15,306.12.

5. A tax of \$1857.60 is levied upon a school district for building a school-house. The assessed valuation of the district is \$1,935,000. What is the tax on property valued at \$6250?

\$1857.60 + \$1,935,000 = 0.00096.

Therefore, tax on the property is 0.00096 of \$6250 = \$6.00. Ans.

6. In a certain town there are 1350 polls. The assessed value of the real estate is \$713,250; of the personal property is \$738,954; the poll-tax is \$2. The tax on property is 1½%. But only 96% of the tax can be collected, and the collector is paid 2½% of the amount collected. How much does the town receive from the taxes?

The amount of poll-taxes =  $1350 \times \$2 = \$2700$ .

\$713,250 + \$738,954 = \$1,452,204, assessed value.

 $0.01\frac{1}{8}$  of \$1,452,204 = \$16,337.31, amount to be raised on property.

\$16,337.31 + \$2700 = \$19,037.31, amount to be raised.

0.96 of \$19,037.31 = \$18,275.82, amount collected.

 $0.02\frac{1}{2}$  of \$18,275.82 = \$456.90, collector's pay.

\$18,275.82 - \$456.90 = \$17,818.92, amount town receives. Ans.

7. What is the duty, at 20% ad valorem (that is, 20% of the cost), on 320 boxes of raisins, each containing 40 lbs., and costing 8 cents a pound?

$$320 \times 40 \times \$0.08 = \$1024.00$$
.  
 $0.20 \text{ of } \$1024 = \$204.80$ . Ans.

8. What is the duty, at 6 cents a gallon, on 420 hhds. of molasses, 63 gals. in a hogshead?

$$420 \times 63 \times \$0.06 = \$1587.60$$
. Ans.

9. At 40%, what is the duty on 300 tons of iron (2240 lbs. to a ton) invoiced at 1½ cents a pound?

$$300 \times 2240 \times \$0.01\frac{1}{2} = \$10,080.$$
  
 $0.40 \text{ of } \$10,080 = \$4032. Ans.$ 

10. Paid \$1360.80 duty on 300 hhds. of molasses, each containing 63 gals., at 25 cents a gallon. What was the rate per cent of duty?

$$300 \times 63 \times \$0.25 = \$4725$$
.

If 100 be taken to represent \$4725, the number required to represent \$1360.80 is  $\frac{$1360.80}{$4725}$  of  $100 = 28\frac{4}{5}$ .

That is, 284 %. Ans.

11. A sugar refiner imports 50 hhds. of sugar weighing 480 lbs. each, and 120 hhds. of molasses containing 63 gals. each. What is the amount of the duties, if the sugar pay 3 cents a pound, and the molasses 8 cents a gallon, an allowance being made on the sugar of 10%, and 2% on the molasses?

$$50 \times 480 \times \$0.03 = \$720.$$
 $0.90 \text{ of } \$720 = \$648.$ 
 $120 \times 63 \times \$0.08 = \$604.80$ 
 $0.98 \text{ of } \$604.80 = \$592.70.$ 
 $\$648 + \$592.70 = \$1240.70.$  Ans.

12. An importer paid \$825 duty on an invoice of silks, the duty being 24%. But damages of 15% were allowed at the custom-house. What was the entire cost of the goods?

If 24 represent \$825, 100 will represent  $\frac{100}{34}$  of \$825 = \$3437.50. If 100 be taken to represent the cost, 100 - 15 = 85 will represent the invoice price.

 $\frac{100}{25}$  of \$3437.50 = \$4044 12, cost. \$4044.12 + \$825 = \$4869.12. Ans.

13. Paid \$325 duty on goods which had been damaged, allowance for damage is 24%, and the duty was 24%. What was the invoice price of the goods?

If 24 represent \$325, 100 will represent  $\frac{199}{32}$  of \$325 = \$1354.17. If 100 be taken to represent the cost, 100 - 24 = 76 will represent the invoice price.

Therefore, the invoice price was  $\frac{1}{2}$  of \$1354.17 = \$1781.80.

#### FREECISE LXXI.

Find the interest of \$680.40 for 2 yrs. 4 mos. 6 dys., at 6%.

\$95.94. Ans.

2. Find the interest of \$25.625 for 30 dys., at 6%.

Find the interest of \$85.85 rr. 7 mos. 21 dys., at 6%.

4. Find the interest of \$1100 for 3 yrs. 4 mos., at 5%.

5. Find the interest of \$1275 for 3 yrs. 2 mos. 15 dys., at 8%.

3 yrs. = 0.18  
2 mos. = 0.01  
15 dys. = 
$$\frac{0.0025}{0.1925}$$
  
 $\frac{4}{0.7700}$   
 $\frac{0.25\frac{2}{3}}{0.25\frac{2}{3}}$ 

$$$1275$$
 $\times 0.25\frac{2}{3}$ 
 $$327.25$ . Ans.

6. Find the interest of \$475.16 for 27 dys., at  $4\frac{1}{2}$ %.

27 dys. = 
$$0.0045$$
  
 $\times 3$   
4)  $0.0135$   
 $0.0033\frac{3}{2}$ 

$$$475.16$$
  
 $\times 0.0033\frac{3}{4}$   
 $$1.60. Ans.$ 

7. Find the interest of \$1290.50 for 60 dys., at 6%.

60 dys. = 0.01.  

$$$1290.50$$
  
 $\times 0.01$   
 $$12.91$ . Ans.

8. Find the interest of \$125 for 1 yr. 2 mos. 2 dys., at 9%.

1 yr. = 0.06  
2 mos. = 0.01  
2 dys. = 
$$\frac{0.000\frac{1}{3}}{0.070\frac{1}{3}}$$
  
 $\frac{\times 3}{2)0.211}$   
0.1055  
 $\frac{\times $125}{$13.19}$ . Ans.

9. Find the interest of \$250.80 for 10 mos. 10 dys., at  $3\frac{1}{2}$ %.

10 mos. = 
$$0.05$$
  
10 dys. =  $0.001\frac{2}{3}$   
 $0.051\frac{2}{3}$   
 $\frac{7}{12)}\frac{0.361\frac{2}{3}}{0.030\frac{5}{36}}$   
\$ 250.80  
 $\times 0.030\frac{5}{36}$   
\$ 7.56. Ans.

10. Find the interest of \$258.85 from Mar. 6 to June 24, at 5%.

mos. dys. 
$$6$$
 24  $\frac{3}{3}$   $\frac{6}{18}$   $\frac{3}{18}$   $\frac{6}{3}$   $\frac{18}{18}$   $\frac{3}{3}$  mos. = 0.015  $\frac{6}{18}$  dys. =  $\frac{0.003}{0.018}$   $\frac{5}{0.015}$   $\frac{5}{0.015}$  \$258.85  $\times$  0.015  $\frac{5}{3.88}$  Ans.

11. Find the interest of \$380 for 2 yrs. 11 mos. 27 dys., at 4½%.

2 yrs. = 
$$0.12$$
  
11 mos. =  $0.055$   
27 dys. =  $0.0045$   
 $0.1795$   
 $\times 3$   
4)  $0.5385$   
 $0.13461$   
 $\times $380$   
\$51.16. Ans.

12. Find the interest of \$475.05 for 1 yr. 9 mos. 14 dys., at  $7\frac{3}{10}\%$ .

1 yr. = 
$$0.073$$
  
9 mos. =  $0.05475$   
14 dys. =  $0.002838$   
 $0.130588$   
 $\times $475.05$   
 $$62.04$ . Ans.

13. Find the interest of \$725.40 for 11 mos. 24 dys., at 51%.

11 mos. = 
$$0.0481\frac{1}{4}$$
24 dys. =  $0.0035$ 

$$0.0516\frac{1}{4}$$
\$ 725.40
$$\times 0.0516\frac{1}{4}$$
\$ 37.45. Ans.

14. Find the interest of from May 5, \$680.50 for 2 yrs. 6 days, at 5%. 1881, at 5½%.

15. Find the interest of \$630.50 for 90 dys., at 6%.

90 dys. = 
$$0.01\frac{1}{2}$$
.  
\$630.50  
 $\times 0.01\frac{1}{2}$   
\$9.46. Ans.

16. Find the interest of \$547.60 from Feb. 20 to Dec. 5, at  $6\frac{1}{2}$ %.

mos. dys. 
$$12$$
 5  $2$  20  $9$  15  $9$  mos.  $= 0.045$   $15$  dys.  $= 0.0025$   $6)0.0475$   $0.0079\frac{1}{8}$   $\times 6\frac{1}{2}$   $0.05145\frac{1}{8}$  \$28.18. Ans.

17. Find the interest of \$875 from May 5, 1880, to June 21, 1881, at  $5\frac{1}{2}$ %.

yrs.	mos.	dys.
1881	6	21
1880	5	5
1	1	16

1 yr. = 0.06  
1 mo. = 0.005  
16 dys. = 
$$0.002\frac{2}{3}$$
  
12)  $0.067\frac{2}{3}$   
 $0.005\frac{2}{3}\frac{8}{6}$   
 $0.062\frac{1}{3}\frac{1}{6}$ 

\$875  $\times 0.062_{\frac{1}{8}6}$  \$54.27. Ans.

18. Find the interest of \$758.50 from Jan. 5 to July 1, at  $4\frac{1}{2}\%$ .

5 mos. = 
$$0.025$$
  
26 dys. =  $0.004\frac{1}{8}$   
4)  $0.029\frac{1}{8}$   
 $0.007\frac{1}{8}$   
 $0.022$ 

\$758.50 × 0.022 \$16.69. Ans.

19. Find the interest of \$342.42 from Feb. 5, 1879, to Mar. 15, 1881, at 7%.

yrs. mos. dys.

1881 3 15

1879 2 5

2 1 10

2 yrs. = 0.12

1 mo. = 0.005

10 dys. = 
$$\frac{0.001}{0.12\frac{2}{3}}$$
 $\frac{0.02\frac{1}{3}}{0.14\frac{7}{3}}$ 

\$342.42

 $\times 0.14\frac{7}{3}$ 

\$50.60. Ans.

20. Find the interest of \$540 from Mar. 5 to Sept. 21, at  $3\frac{1}{2}$ %.

mos. dys. 
$$9$$
 21  $\frac{3}{6}$   $\frac{5}{6}$   $\frac{16}{16}$  6 mos.  $= 0.03$  16 dys.  $= \frac{0.002\frac{2}{3}}{0.032\frac{2}{3}}$   $\frac{7}{12)}\frac{0.228\frac{2}{3}}{0.019\frac{1}{18}}$  \$540  $\times \frac{0.019\frac{1}{18}}{10.29}$  Ans.

21. Find the amount of \$431.50 for 2 yrs. 8 mos., at  $4\frac{1}{2}$ %

\$431.50  

$$\frac{\times 0.04\frac{1}{2}}{\$19.4175} = \text{Int. for 1 yr.}$$
  
 $\frac{\times 2\frac{2}{3}}{\$51.78} = 2 \text{ yrs. 8 mos.}$   
\$51.78  
 $\frac{431.50}{\$483.28}$ . Ans.

22. Find the amount of \$476.50 from July 5, 1880, to Feb. 9, 1881, at 4%.

s, 1001, m	1 2 70.	
1881	2	9
1880	7	- 5
	7	4
7 mos	-0.03	5
4 dys	0.00	0
	8) 0.03	5 <del>3</del>
	0.01	18
	0.02	37
\$47	6.50	
× 0.0	0237	
\$1	1.33	
47	6.50	
\$48	7.83. A	718.

23. Find the amount of \$319.20 from April 7 to Aug. 31, at 31%.

8	474. 31
4	7
	24
	= 0.02
	s 0.004
	6) 0.024
	0.004
	31
	0.013
	319.20
	< 0.013
	\$4.15
	319.20
	323.35 Ana.

24. Find the amount of \$6460 from June 15, 1878, to May 7, 1880, at 41%.

JTL.	mos.	dys.
1880	5	7
1878	6	15
1	10	22
1 уг	0.06 = 0.06	
10 mos	-0.05	
22 dys	- 0.003 <u>‡</u>	
	6) 0.113	_
	0.018	7
	$\times 4.25$	
	0.08051	L.
	×\$6460	
	\$520.12	
	6460.00	
4	6980.12.	Ans.

25. Find the amount of \$150 from Aug. 5, 1879, to Mar. 17, 1881, at 7%.

yrs.	mee.	dys.
1881	3	17
1879	8	5
1	7	12
1 1	yr. = 0.0	6
7 m	ов. — 0.0	35
12 d	ya. — <u>0.0</u>	02
	6) 0.0	97
	0.0	161
	0.1	131
	×\$1	50
	\$16.	98
	150.	00
	\$166.	98. <b>Ans.</b>

26. Find the amount of \$527.20 from Jan. 1 to Nov. 20, at 4½%.

mos. dys.

11 20

1 1

10 19

10 mos. = 
$$0.05$$

19 dys. =  $0.003\frac{1}{8}$ 

4)  $0.053\frac{1}{8}$ 

0.013 $\frac{7}{24}$ 

0.039 $\frac{7}{8}$ 

\$ 21.02

527.20

\$ 548.22. Ans.

27. Find the amount of \$1250 from Nov. 15, 1880, to Mar. 1, 1881, at 5%.

28. Find the amount of \$624.36 from Mar. 5 to Dec. 20, at  $7\frac{8}{10}$ %.

\$624.36 × 0.073 12)\$45.57828. Int. for 1 yr. \$3.79819. Int. for 1 mo.

29. Find the amount of \$12,260 from May 6 to Oct. 24, at 3½%.

mos. dys.

10 24

$$\frac{5}{6}$$
 $\frac{6}{6}$ 
 $\frac{18}{5}$ 
18

5 mos. = 0.025

18 dys. = 0.003

0.028

 $\begin{array}{r} \times 3\frac{1}{4} \\ \hline 6)0.105 \\ \hline 0.0175 \\ \hline \hline $12260 \\ \hline \times 0.0175 \\ \hline \hline $214.55 \\ \hline 12260.00 \\ \hline $12,474.55. Ans. \\ \end{array}$ 

30. Find the amount of \$11,216 from Oct. 20 to Dec. 31, at 1% a month.

mos.
 dys.
 \$ 11216

 12
 31
 
$$\times 0.023\frac{2}{3}$$

 10
 20
  $\times 265.45$ 

 2
 11
 11216.00

 2 mos. = 0.02
 \$ 11,481.45. Ans.

 11 dys. =  $0.003\frac{2}{3}$ 

31. Find the rate per cent when the interest on \$326 for 15 yrs. is \$220.05.

Interest on \$326 for 15 yrs. is \$202.05; on \$326 for 1 yr. is  $\frac{1}{15}$  of \$202.05; on \$1 for 1 yr. is  $\frac{1}{326}$  of  $\frac{1}{15}$  of \$202.05 = \$0.04\frac{1}{2}\$. Therefore, the rate required is  $4\frac{1}{2}$ %. Ans.

32. Find the rate per cent when the interest on \$372.50 for 18 yrs. is \$301.725.

Interest on \$372.50 for 18 yrs. is \$301.725;  
on \$372.50 for 1 yr. is 
$$\frac{$301.725}{18}$$
;  
on \$1 for 1 yr. is  $\frac{$301.725}{18 \times 372.50} = $0.04\frac{1}{2}$ .

Therefore, the rate required is  $4\frac{1}{2}\%$ . Ans.

33. Find the rate per cent when \$245 amount to \$252.961 for 9 mos.

The interest is \$252.96\frac{1}{2} - \$245 = \$7.96\frac{1}{2}.

The time is 9 mos. = 0.75 yr.

Interest on \$245 for 0.75 yr. is \$7.96\frac{1}{2};

on \$245 for 1 yr. is 
$$\frac{$7.96\frac{1}{2}}{0.75}$$
;

on \$1 for 1 yr. is  $\frac{$7.96\frac{1}{2}}{0.75 \times 245} = $0.04\frac{1}{2}.$ 

Therefore, the rate required is 4\frac{1}{3}\%. Ans.

34. Find the rate per cent when the interest on \$235.25 is \$70.575 for 5 yrs.

Interest on \$235.25 for 5 yrs. is \$70.575; on \$235.25 for 1 yr. is  $\frac{$70.575}{5}$ ; on \$1 for 1 yr. is  $\frac{$70.575}{5 \times 235.25} = $0.06$ .

Therefore, the rate required is 6%. Ans.

35. Find the rate per cent when \$363.125 amount to \$371.598 for 7 mos.

The interest is \$371.598 - \$363.125 = \$8.473.

The time is 7 mos.  $=\frac{7}{12}$  yr.

Interest on \$363.125 for  $\frac{7}{12}$  yr. is \$8.473;

on \$363.125 for 1 yr. is 
$$\frac{$8.473}{73}$$
;

on \$1 for 1 yr. is 
$$\frac{$8.473}{\frac{7}{12} \times $363.125} = $0.04$$
, nearly.

Therefore, the rate required is 4%, nearly. Ans.

36. Find the rate per cent when the interest on \$249.43\frac{1}{4} is \$49.88\frac{1}{4} for 5 yrs. 4 mos.

The time is 5 yrs. 4 mos. =  $5\frac{1}{3}$  yrs.

Interest on \$249.43\ for 5\ yrs. is \$49.88\;

on \$249.43\frac{2}{2} for 1 yr. is 
$$\frac{$49.88\frac{2}{2}}{5\frac{1}{8}}$$
;

on \$1 for 1 yr. is 
$$\frac{$49.88\frac{3}{4}}{5\frac{1}{4} \times 249.43\frac{3}{4}} = $0.03\frac{3}{4}$$
.

Therefore, the rate required is 33% Ans.

37. Find the rate per cent when \$350 amount to \$406.70 for 3 yrs. 7 mos. 6 dys.

The time is 3 yrs. 7 mos. 6 dys. = 3.6 yrs.

The interest is \$406.70 - \$350 = \$56.30.

Interest on \$350 for 3.6 yrs. is \$56.30;

on \$350 for 1 yr. is 
$$\frac{$56.30}{3.6}$$
;

on \$1 for 1 yr. is 
$$\frac{$56.30}{3.6 \times 350} = $0.04\frac{1}{2}$$
.

Therefore, the rate required is  $4\frac{1}{2}$ %. Ans.

38. Find the rate per cent when the interest on \$6875 is \$72.05 for 90 dys.

The time is 90 dys. = 0.25 yr.

Interest on \$6875 for 0.25 yr. is \$72.05;

on \$6875 for 1 yr. is 
$$\frac{$72.05}{0.25}$$
;

on \$1 for 1 yr. is 
$$\frac{$72.05}{0.25 \times 6875} = $0.04_{125}^{24}$$
.

Therefore, the rate required is 41 %, nearly. Ans.

39. Find the rate per cent when the interest on \$642 is \$10.70 for 5 mos.

The time is 5 mos.  $=\frac{5}{12}$  yr.

Interest on \$642 for  $\frac{6}{12}$  yr. is \$10.70;

on \$642 for 1 yr. is 
$$\frac{$10.70}{12}$$
;

on \$1 for 1 yr. is 
$$\frac{\$10.70}{\frac{5}{12} \times 642} = \$0.04$$
.

Therefore, the rate required is 4%. Ans.

40. Find the rate per cent when the interest on \$8432 for 2 yrs 7 mos. 23 dys. is \$1339.28.

The time is 2 yrs. 7 mos. 23 dys. =  $2\frac{388}{60}$  yrs.

Interest on \$8432 for 2333 yrs. is \$1339.28;

on \$8432 for 1 yr. is 
$$\frac{$1339.28}{2\frac{233}{360}}$$
;

on \$8432 for 1 yr. is 
$$\frac{\$1339.28}{2\frac{2}{3}\frac{3}{6}\frac{3}{6}}$$
;  
on \$1 for 1 yr. is  $\frac{\$1339.28}{2\frac{2}{3}\frac{3}{6}\frac{3}{6}} = \$0.06$ , nearly.

Therefore, the rate required is 6%, nearly. Ans.

41. Find the rate per cent when a sum of money is doubled in 14 yrs.

Interest on \$1 for 14 yrs. is \$1;

on \$1 for 1 yr. is 
$$\frac{\$1}{14} = \$0.07\frac{1}{7}$$
.

Therefore, the rate required is 71 %. Ans.

42. Find the rate per cent when an investment for 5 yrs. 2 mos. produces a sum equal to  $\frac{2}{3}$  of the capital.

The time is 5 yrs. 2 mos. =  $5\frac{1}{6}$  years.

Interest on \$1 for  $5\frac{1}{5}$  yrs. is  $\frac{$2}{5}$ ;

on \$1 for 1 yr. is 
$$\frac{\$^2}{5\frac{1}{k}} = \$0.07\frac{24}{\$^2}$$
.

Therefore, the rate required is 733%. Ans.

43. Find the rate per cent when an investment for 3 yrs. 1 mo. 15 dys. produces a sum equal to  $\frac{1}{3}$  of the capital.

The time is 3 yrs. 1 mo. 15 dys.  $= 3\frac{1}{8}$  yrs.

Interest on \$1 for  $3\frac{1}{8}$  yrs. is  $\frac{61}{8}$ ;

on \$1 for 1 yr. is 
$$\frac{\$_{\frac{1}{2}}}{3\frac{1}{4}} = \$0.04$$
.

Therefore, the rate required is 4%. Ans.

44. Find the time in which the interest on \$450 will amount to \$72, at 4%.

Interest on \$450, at 4%, for 1 yr. is 0.04 of \$450 = \$18. Therefore, the number of years will be  $\frac{$72}{$18}$  = 4 yrs. Ans.

45. Find the time in which the interest on \$487.50 will amount to \$39, at 4%.

Interest on \$487.50, at 4%, for 1 yr. is 0.04 of \$487.50 = \$19.50. Therefore, the number of years will be  $\frac{$39}{$19.50}$  = 2 yrs. Ans.

46. Find the time in which the interest on \$238.75 will amount to \$64.46, at  $4\frac{1}{2}$ %.

Interest on \$238.75, at 4½%, for 1 yr. is 0.045 of \$238.75 = \$10.74. Therefore, the number of years will be  $\frac{$64.46}{$10.74} = 6$  yrs. Ans.

47. Find the time in which the sum of \$793.875 will amount to \$805.84, at 51%.

The interest is \$805.84 - \$793.875 = \$11.965.

Interest on \$793.875, for 1 yr. at 51% is 0.055 of \$793.875 = \$43.663.

Therefore, the number of years will be  $\frac{$11.965}{$43.663} = 0.274$ .

0.274 yr. = 3 mos. 9 dys. Ans.

48. Find the time in which a sum of money will double itself at 4%.

Interest on \$1, at 4%, for 1 yr. is 0.04 of \$1 = \$0.04.

Therefore, the number of years will be  $\frac{$1}{$0.04}$  = 25. Ans.

49. Find the time in which the sum of \$10 will amount to \$17, at 6%.

The interest is \$17 - \$10 = \$7.

Interest on \$10, at 6%, for 1 yr. is 0.06 of \$10 = \$0.60.

Therefore, the number of years will be  $\frac{\$7}{\$0.60} = 11$ .

11‡ yrs. = 11 yrs. 8 mos. Ans.

50. Find the time in which the sum of \$502.67 will amount to \$578.07, at 41%.

The interest is \$587.07 - \$502.67 - \$75.40.

Interest on \$502.67, at 41 % for 1 yr. is 0.045 of \$502.67 = \$22.62.

Therefore, the number of years will be  $\frac{$75.40}{$22.62}$  = 31.

31 yrs. - 3 yrs. 4 mos. Ans.

51. Find the time in which the interest on \$537.50 will amount to \$80.625, at 4 %.

Interest on \$537.50, at 4% for 1 yr. is 0.04 of \$537.50 = \$21.50.

Therefore, the number of years will be  $\frac{$80.625}{$21.50}$  = 3.75.

3.75 yrs. = 3 yrs. 9 mos. Ans.

52. Find the time in which the interest on \$6875 will amount to \$75.05, at  $4\frac{1}{4}$ %

Interest on \$6875, at  $4\frac{1}{4}$ %, for 1 yr. is 0.0425 of \$6875 = \$292.19.

Therefore, the number of years will be  $\frac{$75.05}{$292.19} = 0.256$ .

0.256 yrs. = 3 mos. 2 dys. Ans.

53. Find the time in which the interest on \$8520 will amount to \$1746.60, at 6%.

Interest on \$8520, at 6%, for 1 yr. is 0.06 of \$8520 = \$511.20.

Therefore, the number of years will be  $\frac{$1746.60}{$511.20} = 3\frac{5}{12}$ .

 $3\frac{5}{12}$  yrs. = 3 yrs. 5 mos. Ans.

54. Find the principal that will produce \$90 interest in 3 yrs., at 4%.

Interest for 1 yr. is  $\frac{$90}{3} = $30$ .

Interest on \$1 for 1 yr., at 4% = \$0.04.

Hence, principal required =  $\frac{30}{0.04}$  of \$1 = \$750. Ans.

55. Find the principal that will produce \$63 interest in 3 yrs., at 61%.

Interest for 1 yr. is  $\frac{$63}{3} = $21$ .

Interest on \$1 for 1 yr., at  $6\frac{1}{4}\% = $0.0625$ .

Hence, principal required =  $\frac{21}{0.0625}$  of \$1 = \$336. Ans.

56. Find the principal that will produce \$100 interest in 8 yrs 6 mos., at 5%.

8 yrs. 6 mos. = 8.5 yrs.

Interest for 1 yr. =  $\frac{$100}{8.5}$  = \$11.7647.

Interest on \$1 for 1 yr., at 5% = \$0.05.

Hence, principal required =  $\frac{11.7647}{0.05}$  of \$1 = \$235.29. Ans.

57. Find the principal that will produce \$1746.60 interest in 3 yrs. 5 mos., at 6%

3 yrs. 5 mos. = 3 1 yrs.

Interest for 1 yr. = 
$$\frac{$1746.60}{3\sqrt{5}}$$
 = \$511.20.

Interest on \$1 for 1 yr., at 6% is \$0.06.

Hence, principal required =  $\frac{511 20}{0.06}$  of \$1 = \$8529. Ans.

58. Find the principal that will produce \$12 interest in 7 mos., at 5%.

7 mos. =  $\frac{7}{12}$  yr.

Interest for 1 yr. = 
$$\frac{$12}{172}$$
 = \$20.5714.

Interest on \$1 for 1 yr, at 5% = \$0.05.

Hence, principal required = 
$$\frac{20.5714}{0.05}$$
 of \$1 = \$411.43. Ans.

59. Find the principal that will produce \$50 interest in 228 dys. at 41%.

228 dys. = 1 yr.

Interest for 1 yr. 
$$=\frac{$50}{18}$$
 = \$78.9474.

on \$1 for 1 yr., at  $4\frac{1}{2}\% = 30.045$ .

rincipal required = 
$$\frac{78.9474}{0.045}$$
 of \$1 = \$1754.39, Ans.

the principal that will produce \$1339.28 interest in 24 dys., at 6%.

mos. 24 dys. = 2.65 yrs.

for 1 yr. = 
$$\frac{$1339 28}{2.65}$$
 = \$505.8887.

on \$1 for 1 yr., at 6% - \$0.06.

runcipal required = 
$$\frac{505.3887}{0.06}$$
 of \$1 = \$8423.14. Ass.

\_ . . =

61. Find the principal that will produce \$1312.65 interest in 2 yrs. 3 mos., at 6%.

2 yrs. 3 mos. = 2.25 yrs.

Interest for 1 yr. =  $\frac{$1312.65}{2.25}$  = \$583.40.

Interest on \$1 for 1 yr., at 6% = \$0.06.

Hence, principal required =  $\frac{583.40}{0.06}$  of \$1 = \$9723.33. Ans.

62. Find the principal that will produce \$750 interest in 3 yrs. 8 mos., at 5%.

3 yrs. 8 mos. =  $3\frac{2}{3}$  yrs.

Interest for 1 yr. =  $\frac{$750}{3\frac{2}{3}}$  = \$204.5455. Interest on \$1 for 1 yr., at 5% = \$0.05.

Hence, principal required =  $\frac{204.5455}{0.05}$  of \$1 = \$4090.91. Ans.

- 63. Find the principal that will amount to \$840 in 3 yrs., at 4 %. If the principal be represented by 100, the interest will be represented by  $3 \times 4 = 12$ , and the amount will be represented Hence, the principal =  $\frac{100}{112}$  of \$840 = \$750. Ans.
- 64. Find the principal that will amount to \$901.1384 in 2 yrs. 6 mos., at  $4\frac{1}{8}$ %.

2 yrs. 6 mos. =  $2\frac{1}{2}$  yrs.

If the principal be represented by 100, the interest will be represented by  $2\frac{1}{2} \times 4\frac{1}{8} = 10\frac{5}{16}$ , and the amount will be represented by 110<sub>16</sub>.

Hence, the principal =  $\frac{100}{110\sqrt{5}\pi}$  of \$901.1384 = \$816.896. Ans.

65. Find the principal that will amount to \$6000 in 21 dys., at 5%.

21 days. =  $\frac{7}{60}$  yr.

If the principal be represented by 100, the interest will be represented by  $\frac{7}{60} \times 5 = \frac{7}{12}$ , and the amount will be represented

Hence, the principal =  $\frac{100}{100 + 7\pi}$  of \$6000 = \$5982.55. Ans.

66. Find the principal that will amount to \$297.60 in 8 mos., at 6%.

8 mos. - ‡ yr.

If the principal be represented by 100, the interest will be represented by  $\frac{2}{3} \times 6 = 4$ , and the amount will be represented by 104.

Hence, the principal =  $\frac{100}{104}$  of \$297.60 = \$286.15. Ans.

67. Find the principal that will amount to \$6378.75 in 1 yr. 1 mo., at 5%.

1 yr. 1 mo. =  $1\frac{1}{12}$  yr.

If the principal be represented by 100, the interest will be represented by  $1_{12} \times 5 = 5_{12}$ , and the amount will be represented by  $105_{12}$ .

Hence, the principal  $=\frac{100}{105\frac{5}{12}}$  of \$6378.75 = \$6050.99. Ans.

68. Find the principal that will amount to \$21,047.95 in 1 yr. 7 mos. 21 dys., at 4½%.

1 yr. 7 mos. 21 dys.  $= 1\frac{77}{126}$  yr.

If the principal be represented by 100, the interest will be represented by  $1\frac{77}{120} \times 4\frac{1}{2} = 7\frac{3}{50}$ , and the amount will be represented by  $107\frac{3}{50}$ .

Hence, the principal =  $\frac{100}{107\frac{31}{30}}$  of \$21,047.95 = \$19,600. Ans.

69. Find the principal that will amount to \$185.09 in 2 yrs. 3 mos. 18 dys., at 5%.

2 yrs. 3 mos. 18 dys. =  $2\frac{17}{60}$  yrs.

If the principal be represented by 100, the interest will be represented by  $2\frac{17}{5} \times 5 = 11\frac{5}{12}$ , and the amount will be represented by  $111\frac{5}{12}$ .

Hence, the principal =  $\frac{100}{111\frac{5}{12}}$  of \$185.09 = \$166. Ans.

70. Find the principal that will amount to \$659.40 in 2 yrs. 11 mos. 15 dys., at 6%.

2 yrs. 11 mos. 15 dys. =  $2\frac{28}{2}$  yrs.

If the principal be represented by 100, the interest will be represented by  $2\frac{24}{2} \times 6 = 17\frac{2}{4}$ , and the amount will be represented by  $117\frac{2}{4}$ .

Hence, the principal =  $\frac{100}{117\frac{3}{4}}$  of \$659.40 = \$560. Ans.

71. Find the principal that will amount to \$9437.516 in 2 yrs. 7 mos. 24 dys., at 4½%.

2 yrs. 7 mos. 24 dys. =  $2\frac{18}{20}$  yrs.

If the principal be represented by 100, the interest will be represented by  $2\frac{1}{2}\frac{3}{5} \times 4\frac{1}{2} = 11\frac{3}{4}\frac{7}{5}$ , and the amount will be represented by  $111\frac{3}{4}\frac{7}{5}$ .

Hence, the principal =  $\frac{100}{111\frac{3}{4}\frac{7}{6}}$  of \$9437.516 = \$8432. Ans.

72. Find the principal that will amount to \$10,266.60 in 3 yrs. 5 mos., at 6%.

3 yrs. 5 mos. =  $3\frac{5}{12}$  yrs.

If the principal be represented by 100, the interest will be represented by  $3\frac{5}{12} \times 6 = 20\frac{1}{2}$ , and the amount will be represented by  $120\frac{1}{2}$ .

Hence, the principal =  $\frac{100}{120\frac{1}{4}}$  of \$10,266.60 = \$8520. Ans.

73. What is the interest of \$195 for 2 yrs. 2 mos. 2 dys., at 6½ %?

2 yrs. = 0.12 \$195  
2 mos. = 0.01 
$$\times 0.141\frac{1}{4}$$
  
2 dys. =  $0.000\frac{1}{3}$  \$27.53. Ans.  
12)  $0.130\frac{1}{3}$   $0.010\frac{1}{3}$   $0.141\frac{1}{4}$ 

74. At what rate per cent will \$1025.20 produce \$25.72 in 4 mos. 9 dys.?

4 mos. 9 days. = 0.3583 yr.

Interest on \$1025.20 for 0.3583 yr. is \$25.72;

on \$1025.20 for 1 yr. is 
$$\frac{$25.72}{0.3583}$$
;

on \$1 for 1 yr. is 
$$\frac{$25.72}{0.3583 \times 1025.20} = $0.07$$
, nearly.

Hence, the rate required is 7%, nearly. Ans.

75. The principal is \$653; the interest \$5.52; the rate 8%. Find the time.

Interest on \$658, at 8%, for 1 yr. is 0.08 of \$653 = \$52.24. Therefore, the number of years will be  $\frac{$5.52}{52.24}$  = 0.1056. 0.1056 yr. = 1 mo. 8 dys. Ans.

**76.** Find the amount of \$520 for 2 mos. 3 dys., at  $4\frac{1}{2}$ %.

77. What sum bearing interest at 41% will yield an annual income of \$1000?

Interest on \$1 for 1 yr., at  $4\frac{1}{2}\% = \$0.045$ . Hence, principal required =  $\frac{1000}{0.045}$  of \$1 = \$22,222.22. Ans.

- 78. How long will it take \$4000 to produce \$625 interest, at  $5\frac{1}{2}$ %? Interest on \$4000, at  $5\frac{1}{2}$ %, for 1 yr. is 0.055 of \$4000 = \$220. Therefore, the number of years will be  $\frac{$625}{$220}$  = 2.841. And 2.841 yrs. = 2 yrs. 10 mos. 3 dys. Ans.
- 79. At what rate per cent will \$3000 produce \$250 interest in 1 yr. 2 mos. 24 dys.?

1 yr. 2 mos. 24 dys. =  $1\frac{7}{30}$  yrs.

Interest on \$3000 for  $1\frac{7}{30}$  yrs. is \$250;

on \$3000 for 1 yr. is 
$$\frac{$250}{1\frac{7}{30}}$$
;  
on \$1 for 1 yr. is  $\frac{$250}{1\frac{7}{30} \times 3000} = $0.06\frac{25}{37}$ .

Hence, the rate required is 635%. Ans.

80. Find the interest of \$1721.84 from April 1 to Nov. 12 at  $4\frac{1}{2}$ %.

81. How long must \$3904.92 be on interest to amount to \$4568.76, at 5%.

The interest = \$4568.76 - \$3904.92 = \$663.84.

Interest on \$3904.92, at 5%, for 1 yr. is 0.05 of \$3904.92 = \$195.246.

Therefore, the number of years will be  $\frac{$663.84}{$195:246} = 3.4$ .

And 3.4 yrs. = 3 yrs. 4 mos. 24 dys. Ans.

82. Find the interest of \$137.60 from July 3 to Dec. 12, at  $7\frac{8}{10}$ %.

83. Find the interest of \$680.20, at  $7\frac{1}{2}\%$ , for 73 dys., reckoning 365 dys. for a year.

73 dys. = 
$$\frac{78}{165}$$
 yr. =  $\frac{1}{5}$  yr.   
\$680.20  
 $\times 0.07\frac{1}{2}$   
5)\$51.0150  
\$10.20. Ans.

# EXERCISE LXXII.

Find day of maturity, the time to run, the discount, and proceeds of the following notes:

1. \$750.

New York, Jan. 1, 1881.

Four months from date I promise to pay to the order of James Fay seven hundred and fifty dollars, value received.

Discounted at 7%, Jan. 12.

JOHN PRAY.

The note becomes due 4 mos. from Jan. 1 = May  $\frac{1}{4}$ .

The time to run is 19 dys. in January, 28 in February, 31 in March, 30 in April, and 4 in May = 112 dys.

The discount is the interest on \$750, for 112 dys., at 7%.

Therefore, the discount is 0.0217 of \$750 = \$16.33.

And the proceeds is \$750 - \$16.33 = \$733.67. Ans.

2. \$4325.50.

Boston, Jan. 3, 1881.

Sixty days from date I promise to pay to James Finn, or order, four thousand three hundred twenty-five and  $\frac{50}{100}$  dollars, value received.

Discounted at 6½%, Jan. 6.

GEORGE BELLOWS.

Counting 60 days, from Jan. 3, there are 28 in January, 28 in February, and 4 in March.

Therefore, the note becomes due March 4/7.

The time to run is 25 dys. in January, 28 in February, and 7 in March = 60 dys.

The discount is the interest on \$4325.50, for 60 dys., at  $6\frac{1}{2}$ %. Therefore, the discount is  $0.010\frac{1}{2}$  of \$4325.50 = \$46.86.

And the proceeds is \$4325.50 - \$46.86 = \$4278.64. Ans.

#### **3.** \$1340.70.

RICHMOND, Va., Jan. 6, 1881.

Ninety days from date I promise to pay to the order of Peter Bright thirteen hundred forty and  $\frac{70}{100}$  dollars, value received.

Discounted at 7%, Jan. 26.

GEORGE WRIGHT.

Counting 90 dys., from Jan. 6, there are 25 in January, 28 in February, 31 in March, and 6 in April.

Therefore, the note becomes due April 6/2.

The time to run is 5 dys. in January, 28 in February, 31 in March, and 9 in April = 73 dys.

The discount is the interest on \$1340.70, for 73 dys., at 7%. Therefore, the discount is  $0.014\frac{7}{36}$  of \$1340.70 = \$19.03. And the proceeds is \$1340.70 - \$19.03 = \$1321.67. Ans.

# **4**. \$1456.30.

CHARLESTON, S.C., Jan. 19, 1881.

Three months after date I promise to pay to the order of John George fourteen hundred fifty-six and  $\frac{80}{100}$  dollars, value received.

Discounted at 5%, Feb. 1.

JOHN WALDORF.

The note becomes due 3 mos. from Jan. 19 = April  $^{19}/_{22}$ .

The time to run is 2 mos. 21 dys.

The discount is the interest on \$1456.30, for 2 mos. 21 dys., at 5%. Therefore, the discount is 0.01125 of \$1456.30 = \$16.38.

And the proceeds is \$1456.30 - \$16.38 = \$1439.92. Ans.

#### **5.** \$4550.36.

DETROIT, Mich., Feb. 2, 1881.

Four months after date I promise to pay to the order of John Callender four thousand five hundred fifty and \$6 dollars, value received.

Discounted at 5½%, Feb. 16.

JAMES BARTON.

The note becomes due 4 mos. from Feb. 2 = June  $^{2}/_{5}$ .

The time to run is 3 mos. 19 dys.

The discount is the interest on \$4550.36, for 3 mos. 19 dys., at 5½%.

Therefore, the discount is  $0.0166\frac{19}{16}$  of \$4550.36 = \$75.78.

And the proceeds is \$4550.36 - \$75.78 = \$4474.58.

#### **6.** \$5000.

CHICAGO, Ill., Oct. 4, 1880.

Six months after date I promise to pay to John Adams, or order, five thousand dollars, value received, with interest at seven per cent. Discounted at 8%, Dec. 31.

WILLIAM DUNN

Interest on note for 6 mos. 3 dys. = \$177.92. Amount of note \$5000 + \$177.92 = \$5177.92. Day of maturity, April  $\frac{4}{7}$ . Time to run, 3 mos. 6 dys. Discount on \$5177.92 at 8%, for 3 mos. 6 dys. = \$110.46. Proceeds is \$5177.92 - \$110.46 = \$5067.46. Ans:

## 7. \$4760.

MILWAUKEE, Wis., Jan. 1, 1881.

Ninety days after date I promise to pay to the order of James Pike four thousand seven hundred and sixty dollars, value received.

Discounted at 71%, Feb. 15.

WILLIAM CLEMENT.

The note becomes due April <sup>1</sup>/<sub>4</sub>. The time to run is 13 dys. in February, 31 in March, and 4 in April = 48 dys. The discount is the interest on \$4760 for 48 dys., at 7½%. Therefore, the discount is 0.01 of \$4760 = \$47.60. And the proceeds is \$4760 - \$47.60 = 4712.40. Ans.

## **8.** \$2017.85.

Kansas City, Mo., Jan. 14, 1881.

\*Three months after date I promise to pay to the order of John Brown two thousand seventeen and  $\frac{8.5}{100}$  dollars, value received.

Discounted at 10%, Mar. 1.

TIMOTHY BRUCE.

The note becomes due 3 mos. from Jan.  $14 = April^{14}/_{17}$ . The time to run is 31 + 17 = 48 dys. The discount is the interest on \$2017.85 for 48 dys., at 10%. Therefore, the discount is  $0.013\frac{1}{3}$  of \$2017.85 = \$26.90. And the proceeds is \$2017.85 = \$26.90 = 1990.95. Ans.

#### **9.** \$652.45.

CONCORD, N.H., Jan. 25, 1881.

Five months after date I promise to pay to the order of Charles Barrett six hundred fifty-two and 100 dollars, value received, with interest at six per cent.

Discounted at 4½%, Mar. 15.

WILLIAM KIMBALL

Interest on note for 5 mos. 3 dys. = \$16.64. Amount of note \$652.45 + \$16.64 = \$669.09.

\*Note. — In Delaware, Maryland, Missouri, Pennsylvania, and the District of Columbia, banks reckon the day of discount in the time for which they charge interest; that is, they charge interest on a 30-day, 60-day, or 90-day note for 34, 64, 94 days, respectively.

Day of maturity, June 25/28.

Time to run, 3 mos. 13 dys.

Discount on \$669.09, at  $4\frac{1}{2}\%$ , for 3 mos. 13 dys. = \$8.61.

Proceeds is \$669.09 - \$8.61 = \$660.48. Ans.

# **10.** \$9040.

Baltimore, Md., Jan. 19, 1881.

Sixty days from date I promise to pay to the order of Charles Carroll nine thousand and forty dollars, value received.

Discounted at 5½%, Feb. 16.

JAMES MONBOR.

Counting 60 dys., from Jan. 19, there are 12 in January, 28 in February, and 20 in March.

Therefore, the note becomes due March 20/28.

The time to run is 13 dys. in February and 23 in March = 36 dys.

The discount is the interest on \$9040, for 36 dys., at 51%.

Therefore, the discount is  $0.005\frac{1}{2}$  of \$9040 = \$49.72.

And the proceeds is \$9040 - \$49.72 - \$8990.28. Ans.

### 11. \$215.

AUGUSTA, Me., Jan. 28, 1881.

Thirty days after date I promise to pay to the order of James Fogg two hundred and fifteen dollars, value received.

Discounted at 6%. Feb. 3.

JOHN MOSES.

Counting 30 dys., from Jan. 28, there are 3 in January and 27 in February.

Therefore, the note becomes due Feb. 27/March 2.

The time to run is 25 dys. in February and 2 in March = 27 dys.

The discount is the interest on \$215, for 27 dys., at 6%.

Therefore, the discount is 0.0045 of \$215 = \$0.97.

And the proceeds is \$215 - 0.97 = \$214.03. Ans.

12. Find the face of a note at 90 dys. that will realize \$850 when discounted at 7%.

The discount on \$1 for 93 dys. is \$0.0180§.

Proceeds on \$1 is \$1 - \$0.0180 = \$0.9819 = \$

Therefore, the face required for \$850 is  $\frac{$850}{0.9819\frac{1}{4}}$  = \$865.65. Ans.

18. Find the face of a note at 4 mos. that will realize \$1600 when discounted at 51 %.

The discount on \$1 for 4 mos. 3 dys. is \$0.0187\frac{1}{1}.

Proceeds on \$1 is \$1 - \$0.0187\frac{1}{1} = \$0.9812\frac{1}{1}.

Therefore, the face required for \$1600 is  $\frac{$1600}{0.9812\sqrt{1}} = $1630.64$ .

14. Find the face of a note at 30 dys, that will realize \$ 1200 when discounted at 61 %.

The discount on \$1 for 33 dys. is \$0.0059 $_{13}^{7}$ . Proceeds on \$1 is \$1 - \$0.0059 $_{13}^{7}$  = \$0.9940 $_{13}^{8}$ . Therefore, the face required for \$1200 is  $\frac{$1200}{0.9940_{13}^{8}}$  = \$1207.19.

15. Find the face of a note at 60 dys. that will realize \$4000 when discounted at 8%

The discount on \$1 for 63 dys. is \$0.0140. Proceeds on \$1 is \$1 \$0.014 = \$0.986.

Therefore, the face required for \$4000 is  $\frac{$4000}{0.986} = $4056.80$ . Am.

16. Find the face of a note at 2 mos. that will realize \$4500 when discounted at  $7\frac{\pi}{10}\%$ .

at on \$1 for 63 dys. is \$0.012775. 1 \$1 is \$1 - \$0.012775 = \$0.987225. the face required for \$4500 is  $\frac{$4500}{0.987225}$  = \$4558.23.

face of a note at 3 mos. that will realize \$1100 when %-

at on \$1 for 3 mos. 3 dys. is \$0.01808\frac{1}{2}.

1 \$1 is \$1 - \$0.01808\frac{1}{2} = \$0.98191\frac{1}{2}.

the face required for \$1100 =  $\frac{$1100}{0.98191\frac{1}{2}} = $1220.28$ .

present worth of \$500 due in 11 mos. at 5%. aken to represent the present worth, the discount will sented by  $\frac{1}{14} \times 5 = 4\frac{7}{14}$ .

The given sum will be represented by  $104\frac{7}{12}$ .

Hence, the present worth is  $\frac{100}{104\frac{7}{12}}$  of \$500 = \$478.09. Ans.

19. Find the present worth and discount of \$3334.62 due in 2 yrs., at 4½%.

If 100 be taken to represent the present worth, the discount will be represented by  $2 \times 4\frac{1}{2} = 9$ .

The given sum will be represented by 109.

Hence, the present worth is  $\frac{189}{189}$  of \$3334.62 = \$3059.28; and the discount is \$3334.62 - \$3059.28 = \$275.34. Ans.

20. Find the present worth and discount of \$4261.33 due at the end of 1 yr. 6 mos., at 6%.

If 100 be taken to represent the present worth, the discount will be represented by  $1\frac{1}{4} \times 6 = 9$ .

The given sum will be represented by 109.

Hence, the present worth is  $\frac{1}{100}$  of \$4261.33 - \$3909.48.

The discount is \$4261.33 - \$3909.48 = \$351.85. Ans.

21. Find the present worth and discount of \$2416.50 due in 7 mos., at 5%.

If 100 be taken to represent the present worth, the discount will be represented by  $\frac{7}{12} \times 5 = 2\frac{1}{12}$ .

The given sum will be represented by 10211.

Hence, the present worth is  $\frac{100}{102\frac{1}{12}}$  of \$2416.50 = \$2348.02, and the discount is \$2416.50 = \$2348.02 = \$68.48. Ans.

22. Find the present worth of \$678.40 due in 16 mos., at  $4\frac{1}{2}$ %.

If 100 be taken to represent the present worth, the discount will be represented by  $1\frac{1}{3} \times 4\frac{1}{2} = 6$ .

The given sum will be represented by 106.

Hence, the present worth is  $\frac{168}{100}$  of \$678.40 = \$640. Ans.

23. Find the present worth and discount of \$574.17 due in 2 yrs. 3 mos., at 51%.

If 100 be taken to represent the present worth, the discount will be represented by  $2\frac{1}{4} \times 5\frac{1}{4} = 12$ .

The given sum will be represented by 112.

Hence, the present worth is 199 of \$574.17 - \$512.65; and the discount is \$574.17 - \$512.65 - \$61.52. Ans.

24. Find the present worth and discount of \$625.13 due in 8 mes, at 7.5 %.

If 100 be taken to represent the present worth, the discount will be represented by  $\frac{1}{2} \times 7\frac{4}{16} = 4\frac{14}{16}$ .

The given sum will be represented by 10414.

Hence, the present worth is  $\frac{100}{104\frac{18}{18}}$  of \$625.13 = \$596.12; and the discount is \$625.13 = \$596.12 = \$29.01. Ans.

25. Find the present worth and discount of \$715.20 due in 1 yr. 4 mos., at 31%.

If 100 be taken to represent the present worth, the discount will be represented by  $1\frac{1}{4} \times 3\frac{1}{4} = 4\frac{2}{4}$ .

The given sum will be represented by 104.

Hence, the present worth is  $\frac{100}{1043}$  of \$715.20 = \$683.31; and the discount is \$715.20 = \$683.31 = \$31.89. 4ms.

1y goods Jan. 10, at 30 dys., for \$218; Feb. 5, at 60, and pay Feb. 10, \$200, March 17, \$50, what is due test at 6%?

27. A note for \$618.75, dated April 17, 1880, payable on demand, bears the following endorsements: June 5, \$126.50; Aug. 20, \$137.25; Nov. 17, \$210. What is due Jan. 1, 1881, reckoning interest at 6%?

Amount of \$618.75 for 8 mos. 14 dys.  $\Rightarrow$ **\$**644.94 Amount of \$126.50 for 6 mos. 26 dys. = \$130 84 Amount of \$137.25 for 4 mos. 11 dys. = 140.25Amount of \$210 for 1 mo. 14 dys. = **\$**482.63

Balance due,

\$162.31. Ans.

28. A note for \$1000, dated April 1, 1880, payable on demand, with interest at 7%; bears the following endorsements: May 6, \$200; July 5, \$225.37; Oct. 18; \$322. What is due Jan. 1, 1881?

Amount of \$1000 for 9 mos. **\$** 1052.50 Amount of \$200 for 7 mos. 25 dys. **= \$ 209.14** Amount of \$225.37 for 5 mos. 26 dys. -233.08 Amount of \$322 for 2 mos. 13 dys. = 326.57\$768.79

Balance due,

\$283.71. Ans.

29. A note for \$835.25, dated July 1, 1880, payable on demand, with interest at 61%, bears the following endorsements: Aug. 20, \$157.50; Sept. 21, \$180.25; Oct. 5, \$200; Dec. 1, \$80. What is due Jan. 1, 1881?

Amount of \$835.25 for 6 mos. **\$**862.39 Amount of \$157.50 for 4 mos. 11 dys. = \$161.23 Amount of \$180.25 for 3 mos. 10 dys. = 183.49Amount of \$200 for 2 mos. 26 dys. 203.11 Amount of \$80 for 1 mo. 80.43

**\$**628.26

Balance due,

\$ 234.13. Ans.

30. A note of \$2000, dated Jan. 22, 1880, and drawing interest at 6%, had payments endorsed upon it as follows: May 20, 1880, \$100, July 20, 1880, \$325, Nov. 2, 1880, \$20; Dec. 23, 1880, \$125. Find the balance due March 1, 1881.

уг. 1880	5	474. 26		\$200	
1880	1	22		0.019	<u> </u>
*000	<u></u>		0.0104	<b>\$</b> 39.3	3 1st interest.
	3	28	0.019	2000.0	2
				\$ 2039.3	3
	\$1	00.		100.0	lat payment.
1880	7	20		\$1939.3	3 2d principal.
1880	5	20		0.0	<u>l</u>
	2		0.01	•	2d interest.
				1939.3	3
				\$1958.7	3
	<b>₽</b> 3	25.		325.0	2d payment.
1880	11	2		\$ 1633.7	3 3d principal.
1880	7	20		0.01	7
	3	12	0.017	\$20 \$27.7	3d interest.
				\$1633.7	3d principal.
	\$:	20.		0.008	5
				\$125 \$13.8	8 4th interest.
				27.7	3 3d interest.
			0.0085	1633.7	3
			0.0000	\$1675.3	9
				145.0	3d & 4th payments.
				\$1530.3	9 4th principal.
				0.011	<u> </u>
				\$17.3	5th interest.
			0.0114	1530.3	9
			2.022	\$1547.7	3 Ans.

31. A note of \$1662.50, dated Jan. 15, 1880, and drawing interest at  $6\frac{1}{2}$ %, had payments endorsed upon it as follows: April 30, 1880, \$25; June 24, 1880, \$25; Sept. 2, 1880, \$625; Jan. 31, 1881, \$700. Find the balance due May 12, 1881.

уг. 1880	mos.	dys. 30	,		\$ 1662.50	
1880	1	15			0.0189	
	3	15	0.0189 <sub>1</sub> 7	<b>\$</b> 25	\$ 31.52	1st interest.
	J	10	0.010013		\$ 1662.50	1st principal.
					$0.0097\frac{1}{2}$	•
	\$ :	25.		<b>\$2</b> 5	\$16.21	2d interest.
1880	6	24	•	•	-	1st interest.
1880	4	30			1662.50	• •
	1	24	0.00971		\$1710.23	
	_				50.00	1st & 2d payments.
			•		<b>\$</b> 1660.23	2d principal.
•	\$2	25.			$0.012_{18}^{5}$	
1880	9	2			\$ 20.38	3d interest.
1880	6	24			1660.23	
	2	8.	$0.012_{18}^{5}$		\$1680.61	
					625.00	3d payment.
	<b>\$</b> 6	25.			\$1055.61	
1881	. <i>,</i>	31			0.026\$\$	
1880	9	2			-	4th interest.
	4	29	0.02655		1055.61	
	*	20	0.02077		\$1084.01	
					700.00	4th payment.
	\$7	00.			\$ 384.01	4th principal.
1881	5	12			0.01847	
1881	1	31			\$7.00	
	3	11	0.018 17		384.01	
					\$391.01	Ans.

32. A note of \$4580, dated Jan. 22, 1879, and drawing interest at 7% had payments endorsed upon it as follows: Jan. 10, 1880, \$2000; Aug. 31, 1880, \$500; Jan. 15, 1881, \$1200; March 4, 1881, \$860. Find the balance due June 15, 1881.

JV:	<b>mor.</b>	474.		\$4560
1880 1879	1	10 22		0.067
1010				\$308.56 1st interest.
	11	18	0.067	4560.00
				\$4868.56
		200		2000.00 lat payment.
	<b>₽</b> 2	000.		\$.2868.56 2d principal.
0567	8	31		0.0449
1000	1	10		\$128.85 2d interest.
	7	21	0.04494	2868.56
				\$2997.41
				500,00 2d payment.
	\$5	00.		\$2497.41 3d principal.
1881	1	15		0.026 1r
17770	8	31		<del></del>
	4	14	0.026	\$65.07 3d interest. 2497.41
	•	13	V.02018	
				\$ 2562.48
	<b>0</b> 11	200.		1200.00 3d payment.
	<b>₽</b> 1	<i>200</i> .		\$1362.48 4th principal.
1881	3	4		0.00918
1881	1	15		\$12.98 4th interest.
		•	0.00918	1362.48
				<b>\$</b> 1375.46
				880.00 4th payment.
				\$515.46 5th principal.
		5		0.018##
		Ĺ		\$10.12 5th interest.
		-	0,018##	\$515.46
		•	0,01038	\$525.58 Ans.
				# mm

33. A note of \$785.50, dated Jan. 30, 1879, and drawing interest at 5%, had payments endorsed upon it as follows: July 17, 1879, \$100; Jan. 29, 1880, \$100; Dec. 31, 1880, \$20; Mar. 16, 1881, \$300; June 14, 1881, \$50. Find the balance due July 23, 1881.

yr.	mos.	dys.		<b>\$</b> 785.50
1879	7	17		0.02333
1879	1	30		\$18.22 1st interest.
	5	17	0.02333	785.50
				<b>\$</b> 803.72
	\$1	<b>0</b> 0.		100.00 1st payment.
1880	1	29		\$703.72 2d principal.
1879	7	17		0.023
1070				\$18.77 2d interest.
	6	12	0. <b>6</b> 23	703.72
				\$722.4 <del>9</del>
	<b>\$</b> 1	00.		100.00 2d payment.
188 <b>0</b>	12	31		\$622.49 3d principal.
1880	. 1	29	0.0461	0.046 <del>1</del>
	11 .	2		\$ 20 <u>\$ 28.71</u> 3d interest.
	11 /	4		\$622.49 3d principal.
	\$:	20.		$0.010_{13}^{5}$
1001	•			\$300 \$6.48 4th interest.
1881	3	16		28.71 3d interest.
1880	12	31		622.49 • 657.69
	2	15	$0.010_{\frac{5}{12}}$	\$657.68 320.00 3d & 4th payments.
				\$337.68 4th principal.
	\$3	<b>300.</b>		0.01%
1881	Ŕ	14		\$4.13 5th interest.
1881	3	16		337.68
		<u>28</u>	Λ Λ1 9	<b>\$341.81</b>
	2	20	0.013	50.00 5th payment.
	œ	<b>56</b> .		\$291.81 5th principal.
	₩.			0,005-5-
1881	7	23		\$1.58 6th interest.
1881	6	14		<b>2</b> 91.81
	1	9	$0.005_{12}^{5}$	\$ 293.39 Ans.

34. A note of \$300.25, dated Aug. 4, 1879, and drawing interest at 61%, had payments endorsed upon it as follows: Oct. 14, 1879, \$100; July 21, 1880, \$100; Oct. 11, 1880, \$50; Jan. 18, 1881, \$50. Find the amount due July 22, 1881.

ye.	wer.	470.		\$300.25
1879	10	14		0.01234
1879	. 8	4		\$3.79 let interest.
	2	10	0.01233	300.25
				\$304.04
	<b>g</b> 1	100.		100.00 lat payment.
	₩.	.00.		\$204.04 2d principal.
1880	7	21		0.049##
1879	10	14		\$10.14 2d interest.
,	9	7	0.04927	204.04
				\$214.18
				100.00 2d payment.
	<b>\$</b> 1	.00.		\$114.18 3d principal.
1880	10	14		0.01471
1830	7	21		\$1.71 3d interest.
	2	23	0.01471	114.18
				<b>\$115.89</b>
				50.00 3d payment.
	<b>₽</b> 0	50,		\$65.89 4th principal.
	ļ	18		0.017#}
	)	11		\$1.15 4th interest.
	3	7	0.01742	65.89
				\$67.04
				50.00 4th payment.
	\$5	iO.		\$17.04 5th principal.
	,	22		0.083
		18		\$0.57 5th interest.
	1	4	0.033	17.04
		_		\$17.61 Ans.

· 4.

35. Find the amount of \$356.25 in 4 yrs., at 5%, compound interest.

\$356.25 0.05 **\$**17.81 365.25 \$374.06 0.05\$18.70 374.06 **\$**392.76 0.05 **\$**19.64 392.76 \$412.40 0.05 \$20.62 **\$**412.40 \$433.02 Ans.

36. Find the amount of \$637.50 in 2 yrs. 6 mos., at 4%, compound interest.

37. Find the compound interest of \$800 in 3 yrs. 9 mos., at 6%.

\$800.00 0.06 \$48.00 800.00 **\$**848.00 0.06 **\$**50.88 848.00 \$898.88 0.06 \$53.93 898.88 **\$**952.81  $0.04\frac{1}{4}$ \$42.88 952.81 \$995.69 800.00 \$195.69 Ans.

38. Find the compound interest of \$39.35 in 1 yr. 9 mos., at 5%.

\$39.35 0.05 \$1.97 39.35 \$41.32 0.03\frac{1}{2} \$1.55 41.32 \$42.87 39.35 \$3.52 Ans. 39. Find the compound interest of \$300 in 2 yrs., at 4%, interest being payable semi-annually.

<b>\$</b> 300	<b>\$</b> 312.12
0.02	0.02
\$6.00	\$6.24
<b>5</b> 00.00	312.12
<b>\$</b> 306.00	<b>\$318.36</b>
0.02	0.02
\$6.12	\$6.37
306.00	<b>9</b> 18. <b>3</b> 8
<b>\$312.12</b>	<b>\$324.73</b>
•	300.00
	\$24.73 Ans.

40. Find the compound interest of \$525 in 1 yr. 8 mos., at 5% interest being payable semi-annually.

<b>\$52</b> 5	<b>\$</b> 544.93	
0.011	0.011	
<b>\$</b> 6.5 <b>6</b>	\$ <del>0</del> .81	
525.00	544.93	
\$531.56	<b>\$</b> 551.74	
0.014	0.01	
\$6.6 <b>4</b>	\$ 6.90	
531.56	551.74	
<b>\$ 538.2</b> 0	\$558.64	
0.011	0.011	
\$6.73	\$6.98	
538.20	558.64	
<b>\$544.93</b>	\$565.62	
-	<b>525.00</b>	
	\$40.62 A1	18.

41. Find the compound interest of \$10,000 in 6 mos., at 6% interest being paid monthly.

\$10000	\$ 10150.75
0.005	0.005
<b>\$</b> 50.00	\$50.75
10000.00	10150.75
<b>\$</b> 10050.00	<b>\$</b> 10201.50
0.005	0.005
<b>\$</b> 50.25	\$51.01
10050.00	10201.50
<b>\$</b> 10100.25	<b>\$</b> 10252. <b>5</b> 1
0.005	0.005
<b>\$</b> 50.50	\$51. <b>2</b> 6
10100.25	10252.51
<b>\$</b> 10150.75	<b>\$</b> 10303.77
-	10000.00
	\$303.77 Ans.

42. What principal will amount to \$137.81 in 2 yrs., at 5% compound interest?

The amount of \$1 for 2 yrs. at 5% is  $$1 \times 1.05^2 = $1.1025$ . The principal is \$137.81 + 1.1025 = \$125. Ans.

43. What principal will amount to \$1860.96 in 3 yrs., at 6% compound interest?

The amount of \$1 for 3 yrs. at 6% is  $$1 \times 1.06^8 = $1.191016$ . The principal is \$1860.96 + 1.191016 = \$1562.50. Ans.

44. What principal will amount to \$1500 in 1 yr., at 4% compound interest, payable quarterly?

The amount of \$1 for 1 yr. at 4%, payable quarterly, is  $$1 \times 1.01^8 = $1.04060401$ .

The principal is \$1500 + 1.04060401 = \$1441.47. Ans.

45. What principal will produce \$100 in 1 yr. 6 mos., at 6% compound interest, payable semi-annually?

The amount of \$1 for 1 yr. 6 mos., payable semi-annually, is  $$1 \times 1.03^8 = $1.092727$ .

The interest is \$1.092727 - \$1 = \$0.092727.

The principal is \$100 + 0.092727 = \$1078.43. Ans.

46. Find the interest due May 19, 1881, on a note dated Dec. 26, 1877, for \$1224.60, with interest payable annually at 5%, when no interest has been paid.

\$1224.60

1881 5 19

1877 12 26

3 4 23 0.203\$

\$1249.61

41.60

\$208.01 interest for 3 yrs. 4 mos. 23 dys.

\$1224.60

\$208.01 interest for 3 yrs. 4 mos. 23 dys.

\$1224.60

2 4 23

1 4 23

4 23

4 23

4 23

$$\frac{4}{23}$$

\$61.23 annual interest.

 $\frac{60.05}{30.0615}$ 

\$12.83

 $\frac{208.01}{30.001}$ 

\$208.01

\$208.01

\$208.01

47. Find the amount due May 27, 1881, on a note dated Jan. 4, 1879, for \$215.50, with interest payable annually at 5½%, when no interest has been paid.

yrs. 1001	mos. 5	dys. 27		<b>\$</b> 215.50
1881 1879	1	4 ( 1		0.143
			0.4.0.	12)30.996
2	4	23	0.143	2.583
		•	• •	\$28.41 interest for 2 yrs. 4 mos. 23 dys.

\$215.50  
1 4 23  

$$\frac{4}{23}$$
  
 $\frac{3}{1}$  9 16 =  $1\frac{148}{180}$  yrs.  
\$\frac{0.05\frac{1}{2}}{\$11.85}\$ annual interest.  
 $\frac{0.05\frac{1}{2}}{$0.6518}$   
 $\frac{1\frac{148}{180}}{$1.17}$  interest on annual interest.  
 $\frac{28.41}{$29.58}$  total interest.  
 $\frac{215.50}{$245.08}$  Ans.

48. Find the amount due Jan. 16, 1881, on a note dated Jan. 8, 1879, for \$3115.20, with interest payable annually at 5%, when no interest has been paid.

49. Find the amount due Jan. 18, 1881, on a note dated Jan. 8, 1877, for \$2875, at 6%: (1) simple interest; (2) annual interest; (3) compound interest.

(1)	(2)	(3)
yra. mos. dys. 1881 1 18	yrs. mos. dys. 3 0 10 2 0 10	<b>\$ 28</b> 75 <b>0.</b> 06
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 0 10 10	\$ 172.50 2875.00
0.241 <b>}</b> \$ 2875	6 1 10 = 61 yrs.	\$ 3047.50 0.06
0.241 <del>3</del> \$ 694.79	Simple interest = \$694.79.	\$ 182.85 3047.50
2875.00 \$ 3569.79 Ans.	\$ 2875 0.06	\$ 3230.35 0.06
	\$ 172.50 0.06	\$ 193.82 3230.35
	\$ 10.35 6 <del>1</del>	\$ 3424.17 0.06
	\$63.25 694.79 2875.00	\$ 205.45 3424.17
	\$3633.04 Ans.	\$ 3629.62 0.001}
		\$ 6.05 3629.62
		<b>\$</b> 3635.67

# EXERCISE LXXIII.

- Find the cost of \$4000 stock, at 109\(\frac{7}{4}\).
   If \$1 stock cost \$1.09\(\frac{7}{4}\), \$4000 stock will cost 4000 \times \$1.09\(\frac{7}{4}\) = \$4395. Ans.
- 2. Find the cost of \$2500 stock, at 98.
  If \$1 stock cost \$0.98, \$2500 stock will cost 2500 × \$0.98 = \$2450. Ans.

- 3. Find the cost of \$3900 stock, at 78\frac{1}{4}.

  If \$1 stock cost \$0.78\frac{1}{4}, \$3900 stock will cost  $3900 \times $0.78\frac{1}{4} = $3046.88$ . Ans.
- 4. Find the cost of \$4700 stock, at  $100\frac{1}{2}$ . If \$1 stock cost \$1.00\frac{1}{2}\$, \$4700 stock will cost  $4700 \times \$1.00\frac{1}{2} = \$4723.50$ . Ans.
- 5. Find the cost of \$1250 stock, at 87\\$, brokerage \{\frac{1}{8}}. If \{\frac{1}{8}}\ be the brokerage,  $87\{\frac{1}{8}} + \{\frac{1}{8}} = 87\{\frac{1}{2}}\ is total cost. If $1 stock cost $0.87\{\frac{1}{4}}, $1250 stock will cost 1250 \times $0.87\{\frac{1}{4}} = $1096.88. Ans.$
- 6. How much bank stock, at  $75\frac{1}{4}$ , may be bought for \$8729? If \$0.75\frac{1}{4} buys \$1 stock, \$8729 will buy  $\frac{$8729}{0.75\frac{1}{4}} = $11600$ . Ans.
- 7. How much railroad stock, at  $91\frac{1}{8}$ , may be bought for \$4237\frac{5}{16}?

  If \$0.91\frac{1}{8} buy \$1 stock, \$4237\frac{5}{16} will buy  $\frac{$4237\frac{5}{16}}{0.91\frac{1}{8}} = $4650$ .
- 8. How much railroad stock may be bought for \$6305, at 121½? If \$1.21½ buy \$1 stock, \$6305 will buy  $\frac{$6305}{1.21½}$  = \$5200. Ans.
- 9. How much railroad stock may be bought for \$5137.50, at  $102\frac{2}{4}$ ?

  If \$102\frac{2}{4}\$ buy \$1 stock, \$5137.50 will buy  $\frac{$5137.50}{1.02\frac{2}{4}}$  = \$5000.
- 10. How many \$100 railroad shares, at 682, may be bought for \$1650?
- 11. What must be the price of stock, in order that \$9200 stock may be bought for \$8970?

If \$9200 stock cost \$8970, then \$1 stock costs \$8970 + 9200 = 0.97\frac{1}{2}. Hence, the stock is quoted at 97\frac{1}{2}. Ans. 12. If \$1500 stock be bought for \$1374.375, what is the price of the stock?

If \$1500 stock cost \$1374.375,
then \$1 stock costs \$1374.375 + 1500 = \$0.91\$.
Hence, the stock is quoted at 91\$. Ans.

- What income will be derived from \$29,700 4% stock?
   0.04 of \$29,700 \$1188. Ans.
- 14. Find the income from \$4500 6% stock.

0.08 of \$4500 - \$270. Ans.

15. How much will a person receive from \$9400 railroad stock if a dividend of 31% be declared?

0.035 of \$9400 - \$329. Ans.

16. How much 8% stock must be bought to give an income of \$2400?

Since \$0.08 is derived from \$1 stock, \$2400 will be derived from \$2400 + 0.08 = \$30,000. Ans.

17. A person receives \$343 as his semi-annual dividend from a 7% atock. How much stock does he hold?

Since \$0.07 is derived from \$1 stock,  $2 \times $343 = $686$  will be derived from \$686 + 0.07 = \$9800. Ans.

nd the total income of a person whose property consists of 6 stocks and \$8200 7% stocks.

of \$3000 - \$180, income from 6% stocks. of \$8200 - \$574, income from 7% stocks.

) + \$574 - \$754, total income. Ans.

nd the rate of dividend paid by some stock, when a holder 0 receives \$924.50.

30 be taken to represent \$24,600, the number required to present \$924.50 will be  $\frac{$924.50}{$24600}$  of  $100 = 3\frac{34}{5}$ .

ia, 3272 %. Ana.

29. Find the rate per cent at which \$11,100 will yield a semi-annual return of \$499.50.

If 100 be taken to represent \$11,100, the number required to represent  $2 \times $499.50 = $999$  will be  $\frac{$999}{$11100}$  of 100 = 9.

That is, 9%. Ans.

21. If \$19,500 be invested in 4% stock, at 91, what income will be received?

\$91 is the cost of \$100 stock.

Hence, \$19,500 = cost of  $\frac{$19500}{0.91}$  = \$21,428.57 stock.

And 0.04 of 21,428.57 = 857.14. Ans.

22. Find the income on \$7000 when invested in 4% stock, at 1031.

\$103\(\frac{1}{2}\) is the cost of \$100 stock.

Hence,  $\$7000 = \cos t \text{ of } \$7000 + 1.03\frac{1}{4} = \$6779.66$ .

And 0.04 of \$6779.66 = \$271.19. Ans.

23. What income will be derived from \$6800 if it be invested in 7% stocks, at 130?

\$130 is the cost of \$100 stock.

Hence,  $$6800 = \cos t \text{ of } $6800 + 1.30 = $5230.77.$ 

And 0.07 of \$5230.77 = \$366.15. Ans.

24. A person invests \$7650 in railroad stock, at 63‡. What will he receive if a dividend of 3½% be declared?

\$63 is the cost of \$100 stock.

Hence,  $\$7650 = \cos t \text{ of } \$7650 + 0.63 = \$12,000.$ 

And  $0.03\frac{1}{4}$  of \$12,000 = \$390. Ans.

25. If 3% stocks are at 881, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$881. \$100 stock pays \$3.

Hence, the \$881 invested pays \$3.

Therefore, the rate of interest is  $3 + 88\frac{1}{8} = 0.03\frac{19}{47}$  or  $3\frac{10}{47}$ %. Ans.

26. If an 8% stock is at 150, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$150. \$100 stock pays \$8.

Hence, the \$150 invested pays \$8.

Therefore, the rate of interest is  $8 + 150 = 0.05\frac{1}{8}$  or  $5\frac{1}{8}$ %. Ans.

27. If a 10% stock is at 175, what rate per cent interest will an investor receive on his money?

\$100 stock costs \$175. \$100 stock pays \$10.

Hence, the \$175 invested pays \$10.

Therefore, the rate of interest is 10 + 175 = 0.05 or 5 %. Ans.

28. If a 4½% stock is at 85, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$85. \$100 stock pays \$41.

Hence, the \$85 invested pays \$41.

Therefore, the rate of interest is  $4\frac{1}{4} + 85 = 0.05\frac{5}{17} = 5\frac{5}{17}\%$ . Ans.

29. If a 7% stock is at 114, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$114. \$100 stock pays \$7.

Hence, the \$114 invested pays \$7.

Therefore, the rate of interest is  $7 + 114 = 0.06 \frac{8}{57}$  or  $6 \frac{8}{57} \%$ . Ans.

30. If a 6% stock is at 130, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$130. \$100 stock pays \$6.

Hence, the \$130 invested pays \$6.

Therefore, the rate of interest is  $6 + 130 = 0.04\frac{s}{13}$  or  $4\frac{s}{13}\%$ . Ans.

31. If an 8% stock is at 140, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$140. \$100 stock pays \$8.

Hence, the \$140 invested pays \$8.

Therefore, the rate of interest is 8 + 140 = 0.05 or 5 %. Ans.

32. How much money must be invested in 4% stock, at 92, to receive \$245 income?

\$100 stock costs \$92. \$100 stock pays \$4.

Hence, the \$92 invested pays \$4.

Therefore, the rate of interest is  $4 + 92 = 0.04\frac{8}{28}$  or  $4\frac{8}{28}$ %.

Since \$0.04 $\frac{8}{23}$  is derived from \$1 stock, \$245 will be derived from \$245 + 0.04 $\frac{8}{23}$  = \$5635. Ans.

33. Find the sum required for an investment in a 4% stock, at 981, to produce an income of \$200 a year.

\$100 stock cost \$98\frac{1}{2}. \$100 stock pays \$4.

Hence, the \$981 invested pays \$4.

Therefore, the rate of interest is  $4 + 98\frac{1}{2} = 0.04\frac{13}{13}$  or  $4\frac{13}{13}$ %.

Since \$0.04 $\frac{12}{197}$  is derived from \$1 stock, \$200 will be derived from \$200 + 0.04 $\frac{12}{197}$  = \$4925. Ans.

34. A person bought some bank stock at 107, and received \$384.25 when a dividend of 7½% was paid. How much had he invested?

Since \$0.07\frac{1}{4}\$ is derived from \$1 stock, \$384.25 will be derived from  $$384.25 + 0.07\frac{1}{4} = $5300$ .

\$5300 is the cost of 53 shares at 100.

Therefore, the cost of 53 shares at 107 will be  $53 \times $107 = $5671$ .

35. What must be the price of a 5% stock, in order that a buyer may receive 6% on his money?

If \$100 pay \$5 at 5%, the number of dollars required to pay \$5 at 6% will be  $\frac{1}{6}$  of \$100 = \$83 $\frac{1}{6}$ .

That is, the stock is quoted at 831. Ans.

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36. What must be the price of a 7% stock, in order that a buyer may receive 6% interest on his money?

If \$100 pay \$7 at 7%, the number of dollars required to pay \$7 at 6% will be  $\frac{7}{6}$  of \$100 = \$116 $\frac{2}{3}$ .

That is, the price of the stock will be 116%. Ans.

37. What may be paid for an 8% stock, in order that a buyer may receive 6% interest on his money? for a 9% stock? for a 10% stock?

If \$100 pay \$8 at 8%, the number of dollars required to pay \$8 at 6% will be  $\frac{1}{2}$  of \$100 = \$133 $\frac{1}{2}$ .

That is, the price of the stock will be 1331. (1) Ans.

If \$100 pay \$9 at 9%, the number of dollars required to pay \$9 at 6% will be \$0 of \$100 - \$150.

That is, the price of the stock will be 150. (2) Ans.

If \$100 pay \$10 at 10%, the number of dollars required to pay \$10 at 6% will be  $\frac{1}{6}$  of \$100 = \$166\frac{2}{3}.

That is, the price of the stock will be 166. (3) Ans.

38. A person invested \$2855 in a bank, when the stock was at 142‡. What is the rate per cent of the dividend when he receives \$150?

The number of shares is \$2855 + \$142 = 20.

If 20 shares pay \$150, 1 share will pay  $\frac{$150}{20} = $7\frac{1}{2}$ .

That is, 7½%. Ans.

39. How much will be received for some 3% stock, from which an income of \$250 has been derived, if sold at 87½?

Since \$0.03 is derived from \$1 stock, \$250 will be derived from 250 + 0.03 = 8333.33 = 831 shares.

83\frac{1}{2} shares at \$87\frac{1}{2}\$ will cost  $83\frac{1}{2} \times $87\frac{1}{2} = $7291.67$ . Ans.

40. If a 5% stock pays \$340 income, and is sold out for \$7990, at what price is it sold?

Since \$0.05 is derived from \$1 stock, \$340 will be derived from \$340 + 0.05 = \$6800.

If \$6800 stock be sold for \$7990, then \$1 is sold for 7990 + 6800 = 1.17.

Hence, the stock is sold at 1171. Ans.

41. On what per cent stock must an investment have been made from which \$185.50 was derived yearly, and which, when sold out at 97, brought \$5141?

If 97 represent \$5141, 100 will represent  $\frac{100}{57}$  of \$5141 = \$5300 The interest on \$5300 for 1 year is \$185.50;

on \$1 for 1 year is  $\frac{$185.50}{$5300}$  = \$0.035.

Hence, the rate is 3½%. Ans.

42. A person receives 41% interest on his money by investing it in some 6% stock. At what price did he buy it?

If \$100 pay \$6 at 6%, the number of dollars required to pay \$6 at  $4\frac{1}{6}$ % is  $\frac{6}{4\frac{1}{4}}$  of \$100 = \$144.

Therefore, the price of the stock was 144. Ans.

43. If \$4800 3% stocks be sold at 88, and the proceeds be invested in 5% stocks at 105%, what additional income will be obtained?

0.03 of \$4800 = \$144, income from the 3% stock.

0.88 of \$4800 = \$4224, amount from the 3% stock.

\$1.056 is paid for \$1 worth of 5% stock.

Hence, \$4224 is paid for \$4224 + 1.056 = \$4000 stock.

0.05 of \$4000 = \$200, income from 5 % stock.

\$200 - \$144 = \$56, increase in income. Ans.

44. If \$7800 3½% stocks be sold at 60, and the proceeds be invested in 5% stocks at 90, find the alteration in income.

 $0.03\frac{1}{2}$  of \$7800 = \$273, income from the  $3\frac{1}{2}$ % stock.

0.60 of \$7800 = \$4680, amount from the  $3\frac{1}{2}\%$  stock.

\$0.90 is paid for \$1 worth of 5% stock.

Hence, \$4680 is paid for \$4680 + 0.90 = \$5200.

0.05 of \$5200 = \$260, income from 5% stock.

\$273 - \$260 = \$13, decrease in income. Ans.

45. If \$10,000 3% stocks be sold at 88, and the proceeds be invested in 3½% stock at par, find the alteration in income.

0.03 of \$10,000 = \$300, income from the 3 % stock.

0.88 of \$10,000 = \$8800, amount from the 3% stock.

 $0.03\frac{1}{4}$  of \$8800 - \$308, income from the  $3\frac{1}{2}\%$  stock.

\$308 - \$300 = \$8, increase in income. Ans.

46. If \$10,000 8% stocks be sold at 150, and the proceeds be invested in 6% stocks at par, find the alteration in income.

0.08 of \$10,000 = \$800, income from the 8% stock.

1.50 of \$10,000 = \$15,000, amount from the 8% stock.

0.06 of \$15,000 = \$900, income from the 6% stock.

\$900 - \$800 - \$100, increase in income. Ans.

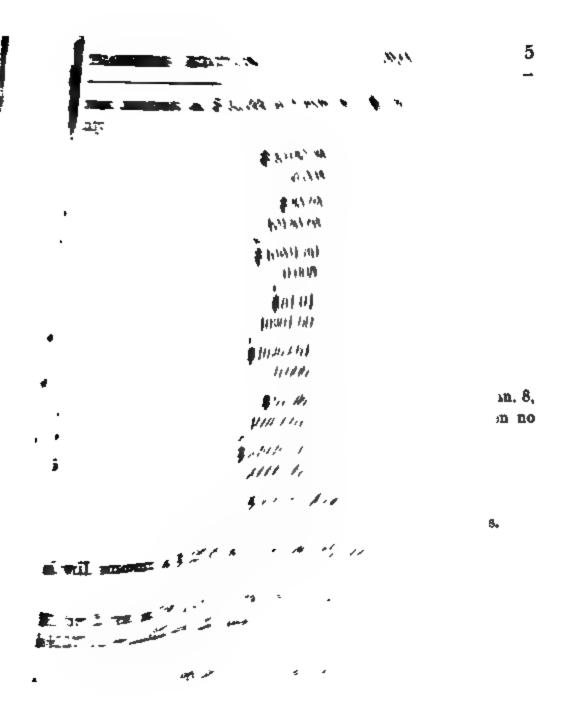
Find the compround interest of \$300 in 2 years are seen, annually.

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45. What principal will produce-\$100 in 1 yr. 6 mos., at 6% compound interest, payable semi-annually?

The amount of \$1 for 1 yr. 6 mos., payable semi-annually, is  $$1 \times 1.03^3 = $1.092727$ .

The interest is \$1.092727 - \$1 = \$0.092727.

The principal is \$100 + 0.092727 = \$1078.43. Ans.

46. Find the interest due May 19, 1881, on a note dated Dec. 26, 1877, for \$1224.60, with interest payable annually at 5%, when no interest has been paid.

47. Find the amount due May 27, 1881, on a note dated Jan. 4. 1879, for \$215.50, with interest payable annually at 5½%, when no interest has been paid.

yrs.		dys.		<b>\$</b> 215.50
1881	5	27		0.143 <del>§</del>
1879	1	4		12)30.996
2	4	23	0.143	2.583
		•	• ;.	\$28.41 interest for 2 yrs. 4 mos. 23 dys

\$215.50  
1 4 23  
4 23  
1 9 16 = 
$$1\frac{148}{180}$$
 yrs.  
\$215.50  
\$11.85 annual interest.  
0.05\frac{1}{2}\$  
\$0.6518  
\frac{1\frac{148}{180}}{11.17} \text{ interest on annual interest.}  
28.41  
\$29.58 total interest.  
215.50  
\$245.08 Ans.

48. Find the amount due Jan. 16, 1881, on a note dated Jan. 8, 1879, for \$3115.20, with interest payable annually at 5%, when no interest has been paid.

49. Find the amount due Jan. 18, 1881, on a note dated Jan. 8, 1877, for \$2875, at 6%: (1) simple interest; (2) annual interest; (3) compound interest.

(1)	(2)	(3)
yrs. mos. dys. 1881 1 18	yra. mos. dys. 3 0 10	<b>\$ 28</b> 75 <b>0</b> .06
$\frac{1877}{4} \frac{1}{0} \frac{8}{10}$	2 0 10 1 0 10 10	\$ 172.50 2875.00
0.241 <del>3</del> \$ 2875	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	\$ 3047.50 0.06
0.241 <del>3</del> \$694.79	Simple interest -\$694.79.	\$ 182.85 3047.50
2875.00 \$3569.79 Ans.	\$ 2875 0.06	\$ 3230.35 0.06
	\$172.50 0.06	\$ 193.82 3230.35
	\$ 10.35 6\frac{1}{3}	\$ 8424.17 0.06
	\$ 63.25 694.79	\$ 205.45 3424.17
	2875.00 \$3633.04 Ans.	\$ 3629.62 0.001}
		\$ 6.05 3629.62
		\$ 3635.67 An

# EXERCISE LXXIII.

- Find the cost of \$4000 stock, at 109\(\frac{7}{4}\).
   If \$1 stock cost \$1.09\(\frac{7}{4}\), \$4000 stock will cost 4000 \times \$1.09\(\frac{7}{4}\) = \$4395. Ans.
- 2. Find the cost of \$2500 stock, at 98.
  If \$1 stock cost \$0.98, \$2500 stock will cost 2500 × \$0.98 = \$2450. Ans.

- 3. Find the cost of \$3900 stock, at  $78\frac{1}{8}$ . If \$1 stock cost \$0.78\frac{1}{8}, \$3900 stock will cost  $3900 \times $0.78\frac{1}{8} = $3046.88$ . Ans.
- 4. Find the cost of \$4700 stock, at  $100\frac{1}{2}$ . If \$1 stock cost \$1.00\frac{1}{2}\$, \$4700 stock will cost  $4700 \times $1.00\frac{1}{2}$ = $4723.50$ . Ans.
- 5. Find the cost of \$1250 stock, at 87\frac{1}{8}, brokerage \frac{1}{8}.

  If \frac{1}{8} be the brokerage,  $87\frac{1}{8} + \frac{1}{8} = 87\frac{1}{2}$  is total cost.

  If \$1 stock cost \$0.87\frac{2}{4}, \$1250 stock will cost

  1250 \times \$0.87\frac{3}{4} = \$1096.88. Ans.
- 6. How much bank stock, at 75½, may be bought for \$8729?

  If \$0.75½ buys \$1 stock, \$8729 will buy  $\frac{$8729}{0.75½} = $11600$ . Ans.
- 7. How much railroad stock, at 91\frac{1}{8}, may be bought for \$4237\frac{5}{16}\$? If \$0.91\frac{1}{8}\$ buy \$1 stock, \$4237\frac{5}{16}\$ will buy  $\frac{$4237\frac{5}{16}}{0.91\frac{1}{8}} = $4650$ .
- 8. How much railroad stock may be bought for \$6305, at  $121\frac{1}{4}$ ?

  If \$1.21\frac{1}{4} buy \$1 stock, \$6305 will buy  $\frac{$6305}{1.21\frac{1}{4}}$  = \$5200. Ans.
- 9. How much railroad stock may be bought for \$5137.50, at  $102\frac{2}{4}$ ?

  If \$102\frac{2}{4}\$ buy \$1 stock, \$5137.50 will buy  $\frac{$5137.50}{1.02\frac{2}{3}}$  = \$5000.
- 10. How many \$100 railroad shares, at 68‡, may be bought for \$1650?
- 11. What must be the price of stock, in order that \$9200 stock may be bought for \$8970?

If \$9200 stock cost \$8970, then \$1 stock costs \$8970 + 9200 = 0.97\frac{1}{2}. Hence, the stock is quoted at 97\frac{1}{2}. Ans. 12. If \$1500 stock be bought for \$1374.375, what is the price of the stock?

If \$1500 stock cost \$1374.375, then \$1 stock costs \$1374.375 + 1500 = \$0.91\frac{2}{3}. Hence, the stock is quoted at 91\frac{2}{3}. Ans.

- 13. What income will be derived from \$29,700 4% stock?

  0.04 of \$29,700 = \$1188. Ans.
- 14. Find the income from \$4500 6% stock.

0.06 of \$4500 = \$270. Ans.

15. How much will a person receive from \$9400 railroad stock if a dividend of  $3\frac{1}{2}$ % be declared?

0.035 of \$9400 = \$329. Ans.

16. How much 8% stock must be bought to give an income of \$2400?

Since \$0.08 is derived from \$1 stock, \$2400 will be derived from 2400 + 0.08 = 30,000. Ans.

17. A person receives \$343 as his semi-annual dividend from a 7% stock. How much stock does he hold?

Since \$0.07 is derived from \$1 stock,  $2 \times $343 = $686$  will be derived from \$686 + 0.07 = \$9800. Ans.

- 18. Find the total income of a person whose property consists of \$3000 6% stocks and \$8200 7% stocks.
  - 0.06 of \$3000 = \$180, income from 6% stocks.
  - 0.07 of \$8200 = \$574, income from 7% stocks.

\$180 + \$574 = \$754, total income. Ans.

- 19. Find the rate of dividend paid by some stock, when a holder of \$24,600 receives \$924.50.
  - If 100 be taken to represent \$24,600, the number required to represent \$924.50 will be  $\frac{$924.50}{$24600}$  of  $100 = 3\frac{55}{25}$ .

That is, 3373%. Ans.

29. Find the rate per cent at which \$11,100 will yield a semi-annual return of \$499.50.

If 100 be taken to represent \$11,100, the number required to represent  $2 \times $499.50 = $999$  will be  $\frac{$999}{$11100}$  of 100 = 9.

That is, 9%. Ans.

21. If \$19,500 be invested in 4% stock, at 91, what income will be received?

\$91 is the cost of \$100 stock.

Hence, \$19,500 - cost of  $\frac{$19500}{0.91}$  - \$21,428.57 stock.

And 0.04 of 21,428.57 = 857.14. Ans.

22. Find the income on \$7000 when invested in 4% stock, at 1031.

\$103\(\frac{1}{2}\) is the cost of \$100 stock.

Hence,  $\$7000 = \cos t \text{ of } \$7000 + 1.03\frac{1}{2} = \$6779.66$ .

And 0.04 of \$6779.66 = \$271.19. Ans.

23. What income will be derived from \$6800 if it be invested in 7% stocks, at 130?

\$130 is the cost of \$100 stock.

Hence,  $$6800 = \cos t \text{ of } $6800 + 1.30 = $5230.77.$ 

And 0.07 of \$5230.77 = \$366.15. Ans.

24. A person invests \$7650 in railroad stock, at 63‡. What will he receive if a dividend of 3½% be declared?

\$63 is the cost of \$100 stock.

Hence,  $\$7650 = \cos t \text{ of } \$7650 + 0.63 = \$12,000.$ 

And 0.031 of \$12,000 = \$390. Ans.

25. If 3% stocks are at 881, what rate per cent interest will a purchaser receive on his money?

\$100 stock costs \$881. \$100 stock pays \$3.

Hence, the \$881 invested pays \$3.

Therefore, the rate of interest is  $3 + 88\frac{1}{2} = 0.03\frac{1}{2}$  or  $3\frac{1}{2}$ %. Ans.

3. Find the cost of the following draft, when sixty-day bills are quoted at 4.81, and the broker's commission is \frac{1}{3} of 1% of cost of draft:

£500.

New York, Feb. 17, 1881.

Sixty days after sight of this First of Exchange (Second and Third of the same tenor and date unpaid), pay to the order of James Wilson five hundred pounds, value received, and charge to account of

To James Sage & Co., London.

SIMON MORTON & Co.

 $\$4.81 \times 500 = \$2405.$  \$% of \$2405 = \$3.01.\$2405 + \$3.01 = \$2408.01. Ans.

4. Find the face of a draft on Glasgow that can be bought for \$2000, when sterling exchange is quoted at 4.84.

\$ 2000 + \$ 4.84 = 
$$413\frac{27}{121}$$
.  
£  $413\frac{27}{121}$  = £ 413 4 s. 5.5 d. Ans.

5. Find the face of a draft on Dublin that can be bought for \$135.24, when sterling exchange is quoted at 4.83.

$$$135.24 + $4.83 = 28.$$
  
That is, £28. Ans.

6. How large a draft on London can be bought for \$4000, when exchange is quoted at 4.86%?

$$$4000 + $4.86 \frac{2}{3} = 821 \frac{27}{3}$$
.  
£821 \frac{7}{3} = £821 18 s. 4.3 d. Ans.

7. Find the cost of a draft on Paris for 8000 fr., when Paris exchange is quoted at 5.12%, and brokerage is \( \frac{1}{3} \) of 1%.

 $0.00\frac{1}{8}$  of 8000 fr. = 10 fr. 8000 fr. + 10 fr. = 8010 fr.  $8000 + 5.12\frac{2}{8} = 1563.31$ . Hence, draft of 8000 fr. = \$1563.31. Ans. 8. Find the cost of a draft on Paris for 10,000 fr., when Paris exchange is quoted at 5.14.

$$10,000 + 5.14 = 1945.53$$
.  
Hence, draft of  $10,000$  fr. = \$1945.53. Ans.

9. How large a sixty-day draft on Paris can be bought for \$1500, when sixty-day bills are quoted at 5.11½?

$$1500 \times 5.11\frac{1}{2} = 7672.5$$
. That is,  $7672.5$  fr. Ans.

10. How large a sight draft on Paris can be bought for \$2840, when Paris exchange is quoted at  $5.13\frac{1}{2}$ ?

$$2840 \times 5.13\frac{1}{2} = 14,583.4$$
. That is,  $14,583.4$  fr. Ans.

11. Find the cost of a draft on Hamburg for 2876 marks, when German exchange is quoted at 0.951.

$$\frac{2876}{2}$$
 of  $\$0.95\frac{1}{2} = \$686.65$ . Ans.

12. Find the cost of a draft on Munich for 12,000 marks, when German exchange is quoted at 0.94§.

$$\frac{12000}{4}$$
 of  $$0.94\frac{5}{8} = $2838.75$ . Ans.

13. How large a draft on Frankfort can be bought for \$1200, when German exchange is quoted at 0.95½?

$$0.95\frac{1}{2} + 4 = 0.23\frac{7}{8}$$
.  
 $1200 + 0.23\frac{7}{8} = 5026.17$  marks. Ans.

#### EXERCISE LXXVI.

1. If a dozen eggs weigh 692s, what is the mean weight of an egg?

2. Seven boys weigh respectively 119.7 lbs., 105 lbs., 178.3 lbs., 165.3 lbs., 142.8 lbs., 109 lbs., 154.2 lbs. What is their average weight?

3. A merchant mixes 1 lb. of coffee worth 27 cents, 1 lb. worth 35 cents, and 1 lb. worth 40 cents. What are the 3 lbs. together worth? How much a pound is the mixture worth?

4. A merchant mixes 2 lbs. of coffee worth 27 cents a pound, 3 lbs. worth 35 cents a pound, and 1 lb. worth 40 cents. What is a pound of the mixture worth?

$$2 \times \$0.27 = \$0.54$$

$$3 \times 0.35 = 1.05$$

$$1 \times 0.40 = 0.40$$

$$6) \$1.99$$

$$\$0.33 \frac{1}{6}. Ans.$$

5. What is the value per pound of a mixture of coffee containing 7 lbs. worth 26 cents a pound, 4 lbs. worth 31 cents a pound, and 10 lbs. worth 34 cents a pound?

$$7 \times \$0.26 = \$1.82$$
 $4 \times 0.31 = 1.24$ 
 $10 \times 0.34 = 3.40$ 
 $21)\$6.46$ 
 $\$0.30\frac{1}{2}$ . Ans.

6. What is the cost of a gallon of the mixture in which 7 gals. cost 67 cents a gallon, 5 gals. cost 48 cents a gallon, and water, without cost, was added until there were 15 gals. of the mixture?

$$7 \times \$0.67 = \$4.69$$
  
 $5 \times 0.48 = 2.40$   
 $15)\$7.09$   
 $\$0.47$ . Ans.

7. If 7<sup>1</sup> of water be poured into a vessel containing 3<sup>1</sup> of sulphuric acid, specific gravity 1.840, and the mixture shrink to 9.972<sup>1</sup>, what is the specific gravity of the mixture?

$$7 \times 1^{1} = 7.00^{1}$$

$$3 \times 1.84 = 5.52$$

$$9.972^{1}) 12.52^{1}$$

$$1.256. Ans.$$

8. If 41 of water and 11 of sulphuric acid, specific gravity, 1.842, when mixed shrink \(\frac{1}{4}\) of 1%, what is the specific gravity of the mixture?

$$4 \times 1^{1} = 4.000^{1}$$

$$1 \times 1.842 = 1.842$$

$$4.9875^{1}) \overline{5.842^{1}}$$

$$1.171^{1}$$

$$4 + 1 = 5.$$

$$5 - 0.01\frac{1}{4} = 4.9875. Ans.$$

9. In what proportions must tin of specific gravity 7.29 and lead of specific gravity 11.35 be mixed to make a solder of specific gravity 10.21, if no allowance be made for expansion or condensation? (Give the proportions in bulk.)

The specific gravity of tin lacks 2.92 of the required specific gravity; and the specific gravity of lead is 1.14 above the required specific gravity.

Therefore, the tin is to the lead in the inverse ratio of 292 to 114. That is,

Tin: lead = 114:292 = 57:146. Ans.

10. In what proportions must oils worth \$1.25 and 80 cents a gallon be mixed to make a mixture worth \$1 a gallon? (Test the answer.)

The cost of the better oil is \$0.25 above the required cost; and the cost of the worse oil lacks \$0.20 of the required cost.

Therefore, the better is to the worse in the inverse ratio of \$0.25 to \$0.20. That is,

The better: the worse = 20: 25 = 4:5. Ans.

11. In what proportion may oils worth \$1.20, 80 cents, and 60 cents a gallon be mixed so that the mixture shall be worth 70 cents a gallon?

When the 80-cent oil alone is taken, in what ratio to the 60-cent must it be used? When the \$1.20 oil alone is taken, in what ratio to the 60-cent oil must it be used? When the \$1.20 and 80-cent oils are mixed gallon for gallon, how much 60-cent oil must be added? When 1 gal. of the \$1.20 oil and 3 of the 80-cent oil are taken, how much 60-cent oil must be added? If three-fourths of the mixture consist of the 60-cent oil, what per cent of each of the other two must be taken?

(1)

The cost of the \$1.20 is \$0.50 above the required cost; the cost of the \$0.80 oil is \$0.10 above the required cost; and the cost of the \$0.60 oil lacks \$0.10 of the required cost.

Therefore, the \$1.20 oil is to the \$0.80 oil is to the \$0.60 oil in the inverse ratio of 50 to 10 to 10. That is,

The \$1.20 oil: the \$0.80 oil. the \$0.60 oil = 10:10:50=1:1:5.

**(2)** 

The cost of the \$0.80 oil is \$0.10 above the required cost; the cost of the \$0.60 oil lacks \$0.10 of the required cost.

Therefore, the \$0.80 oil is to the \$0.60 oil in the inverse ratio of 10 to 10. That is,

The \$0.80 oil: the 0.60 oil = 10:10=1:1. Ans.

(3)

The cost of the \$1.20 oil is \$0.50 above the required cost; and the cost of the \$0.60 oil lacks \$0.10 of the required cost.

Therefore, the \$1.20 oil is to the \$0.60 oil in the inverse ratio of 50 to 10. That is,

The \$1.20 oil: the 0.60 oil = 10: 50 = 1:5. Ans.

**(4)** 

When 1 gal. of the \$1.20 oil is mixed with 1 gal. of the \$0.80 oil, the mixture costs  $\frac{$1.20 + $0.80}{2} = $1.00$  per gallon.

The cost of the \$1.00 oil is \$0.30 above the required cost; the cost of the \$0.60 oil lacks \$0.10 of the required cost.

Therefore, the \$1.00 oil is to the \$0.60 oil in the inverse ratio of 30:10. That is,

The \$1.00 oil is to the 0.60 oil = 10:30 = 1:3.

1:3::2 gals.: what?

1:3::2 gals.:6 gals. Ans.

(5)

When 1 gal. of the \$1.20 oil is mixed with 3 gals. of the \$0.80 oil, the mixture costs  $\frac{$1.20 + 3 \times $0.80}{4} = $0.90$  per gal.

The cost of the \$0.90 oil is \$0.20 above the required cost; the cost of the \$0.60 oil lacks \$0.10 of the required cost.

Therefore, the \$0.90 oil is to the \$0.60 oil in the inverse ratio of 20:10. That is,

The 0.90 oil: the 0.60 oil = 10: 20 = 1: 2.

1:2::4 gals.: what?

1:2::4 gals.:8 gals. Ans.

(6)

Each of the others will be  $\frac{1-\frac{3}{2}}{2} = \frac{1}{3}$  of the whole, or  $12\frac{1}{2}\%$ . Ans.

12. A solder composed of tin and lead, specific gravities 7.29 and 11.35, has a specific gravity of 10.44. What is the weight of each metal in a kilogram of solder?

Gain on tin = 10.44 - 7.29 = 3.15.

Loss on lead = 11.35 - 10.44 = 0.91.

Ratio = 3.15:0.91; or, as more lead will be needed, 3.15 parts of lead to 0.91 parts of tin in 4.06 parts of solder.

Therefore, the weight of tin is  $\frac{91}{406}$  of  $\frac{729}{1044}$  of  $1000^{\circ} = 156.5^{\circ}$ .

And the weight of lead is  $\frac{3}{100}$  of  $\frac{1}{1000}$  of  $\frac{1}{1000}$  of  $\frac{1}{1000}$  = 843.5s. Ans.

13. Find the equated time for the payment of \$250 due in 3 mos., \$400 due in 6 mos., \$700 due in 8 mos.

$$\$250 \times 0 =$$
 $\$400 \times 3 = \$1200$ 
 $\$700 \times 5 = \$3500$ 
 $\$1350$ 
 $)\$4700$ 
 $3\frac{1}{2}$ 

 $3\frac{1}{2}$  mos. = 3 mos. 14 dys. 3 mos. 14 dys. after 3 mos. = 6 mos. 14 dys.

14. Find the equated time for the payment of \$300 due in 30 dys., \$500 due in 60 dys., and \$200 due in 90 dys.

$$\$300 \times 00 =$$
 $\$500 \times 30 = \$15,000$ 
 $\$200 \times 60 = \$12,000$ 
 $\$1000$ 
 $)\$27,000$ 
 $27$ 

Hence, the equated time is 27 dys. after 30 dys. = 57 dys.

15. Find the equated time for the payment of \$325 due now, \$200 due in 30 dys., \$460 due in 60 dys., and \$150 due in 90 dys.

$$\$325 \times 00 =$$
 $\$200 \times 30 = \$6,000$ 
 $\$460 \times 60 = \$27,600$ 
 $\$150 \times 90 = \$13,500$ 
 $\$1135$ 
 $)\$47,100$ 

Hence, the equated time is 41 dys.

16. Find the equated time for the payment of \$240 due May 10, \$420 due July 2, \$310 due Sept. 14, and \$600 due Oct. 1.

$$\$240 \times 00 =$$
 $\$420 \times 53 = \$22,260$ 
 $\$310 \times 127 = \$39,370$ 
 $\$600 \times 144 = \$86,400$ 
 $\$1570$ 
 $)\$148,030$ 
 $94$ 

Hence, the equated time is 94 dys. after May 10 = Aug. 12.

17. Find the equated time for the payment of \$275 due June 21, \$175 due July 16, \$200 due Aug. 6, and \$150 due Sept. 3.

$$\$275 \times 00 =$$
 $\$175 \times 25 = \$4,375$ 
 $\$200 \times 46 = \$9,200$ 
 $\$150 \times 74 = \$11,100$ 
 $\$800$ 
 $\$24.675$ 

Hence, the equated time is 31 dys. after June 21 - July 22.

18. Find the equated time for the payment of \$112.30 due July 6, \$115.25 due July 30, \$232.15 due Sept. 4, and \$102.36 due Oct. 1.

$$\$112.30 \times 00 =$$
 $\$115.25 \times 24 = \$2,766.00$ 
 $\$232.15 \times 60 = \$13,929.00$ 
 $\$102.36 \times 87 = \$8,905.32$ 
 $\$562.06$ 
 $)\$25,600,32$ 
 $46$ 

Hence, the equated time is 46 dys. after July 6 = Aug. 21.

19. A owed B \$2000 payable in 4 mos., but at the end of 1 mo. he paid him \$500, at the end of 2 mos. \$500, and at the end of 3 mos. \$500. In how many months is the balance due?

$$\$500 \times 3 = \$1500$$
  
 $\$500 \times 2 = \$1000$   
 $\$500 \times 1 = \$500$   
 $\$1500$ 

Therefore, he is entitled to keep the balance (\$500)  $\frac{$000}{500}$  mos. = 6 mos. after its maturity.

20. A merchant bought, Feb. 11, 1881, a bill of goods amounting to \$1700, on 4 months' credit; but he paid March 22, \$400, April 20, \$220, May 10, \$300. When is the balance due?

78. 
$$\frac{1881}{2}$$
  $\frac{11}{4}$   $\frac{4}{0}$   $\frac{1}{1881}$   $\frac{1}{6}$   $\frac{11}{1}$   $-$  June 11, 1881.  $\frac{400 \times 81 = \$32,400}{\$220 \times 52 = \$11,440}$   $\frac{\$300 \times 32 = \$9,600}{\$920}$   $\frac{\$53,440}{\$53,440}$ 

Therefore, he is entitled to keep the balance (\$780)  $\frac{5}{7}\frac{440}{80}$  dys = 69 dys. after its maturity, June 11, 1881, = Aug. 19, 1881.

**\$**34.83

**1900.00** 

**\$**1934.8**3** 

Find the equated time of maturity of each of the following bills, and the amount due at settlement, including interest at 6%:

```
21.
                  JAMES PRICE, to JOHN BATES, Dr.
        1881.
       Apr. 5.
                  To mdse. on 4 mos. credit
                                                          $120.50
                                3
                                                             87.33
       Apr. 15.
                                                            218.17
       May 7.
       May 21.
                                                            317.00
                                                          $743.00
                                                   Paid Oct. 18, 1881.
        \$ 87.33 \times 00 =
                                                   From Aug. 23 to Oct.
                                                18 is 56 dys.
        $120.50 \times 21 = $2,530.50
        \$218.17 \times 23 = \$5,017.91
                                                    56 \text{ dys.} = 0.009 \frac{1}{8}
        \$317.00 \times 68 = \$21,556.00
                                                           $743
                                                           0.009\frac{1}{3}
        $743.00
                        )$29,104.41
                                                          $6.93
                                  39
                                                         743.00
  Hence the equated time is 39 dys. after
July 15, 1881 - Aug. 23, 1881.
                                                       $ 749.93
                 HALL & Co. bought of Boles & Co.
  22.
        1881.
       Feb. 11.
                  To mdse. on 30 dys.
                                                          $ 250.00
       Apr. 20.
                                 2 mos.
                                                            500.00
       May 31.
                                 3 mos.
                                                            150.00
       July 6.
                                60 dys.
                                                           1000.00
                                                  Paid Nov. 10, 1881.
    30 dys. after Feb. 11 = Mar. 13.
                                                  Hence, the equated
      2 mos. after Apr. 20 = \text{June } 20.
                                                time is 132 dys. after Mar.
      3 mos. after May 31 = \text{Aug. } 31.
                                                13, 1881 = \text{July } 23, 1881.
    60 dys. after July 6 = Sept. 4.
                                                   From July 23 to Nov.
                                                10 is 110 dys.
         $250 \times 00 =
                                                110 dys. = 0.018
         $500 \times 99 = $49,500
                                                             $1900
         150 \times 171 = 25,650
```

 $\$1000 \times 175 = \$175,000$ 

**)\$250,150** 

132

**\$** 1900 '

Dr.

# 23. Find the equated time of maturity of each side of the following account:

ADAMS & Co. in account with BACON & Co.

1881.			<u> </u>		······	[
Jan. 3.	To mds	e. 90 <b>dys.</b>	\$ 250	Apr. 11.	By cash,	\$ 200
Mar. 7.	"	60 "	150		"	100
May 3.	4.6	60 "	325	May 30.	66	125
June 7.	"	30 "	175	July 2.	66	400

90 dys. after Jan. 3 - April 3.

60 dys. after Mar. 7 = May 6.

60 dys. after May 3 = July 2.

30 dys. after June 7 = July 7.

	Dr.	•	Cr.
\$250 ×	00 =	$$200 \times 0$	0 =
\$150 ×	33 = \$ 4,950	$$100 \times 1$	9 = \$ 1,900
$$325 \times $$	90 = \$29,250	$$125 \times 4$	9 = \$6,125
\$175 ×	95 = \$16,625	\$400 × 8	2 = \$32,800
\$900	\$ 50,825	\$825	)\$40,825
	56		49

Hence, the equated time is 56 days after April 3 = May 29.

Hence, the equated time is 49 days after April 11 = May 30.

Cr.

Find the time for paying the balance in the following equated bills:

	Average due.				Dr.	Average	lue.	,			Cr.
						Average of Apr. 12, 1881					
						May 17, 1881					
26.	May 30, 1881	•	•	•	<b>\$</b> 1000	June 23, 1881	•	•	•	•	<b>\$</b> 920
27.	July 6, 1881	•	•	•	<b>\$</b> 500	Apr. 14, 1881	•	•	•	•	<b>\$</b> 480

#### 24.

Differences in equated time = 35 dys.

Balance of account = \$1000 - \$950 = \$50.

If the account were settled at the later date, May 17, the \$1000 on the Cr. side would have been on interest 35 dys., and this is equivalent to having the balance, \$50, on interest \(^1\frac{2}{5}\text{0}\) of 35 dys. = 700 dys. Hence, the balance should begin to draw interest 700 dys. before May 17, 1881; that is, June 17, 1879.

#### 25.

The difference in equated time = 35 dys.

Balance of account = \$1000 - \$950 = \$50.

If the account were settled at the later date, May 17, the \$950 would have been on interest 35 dys., which is equivalent to having the balance, \$50, on interest \$950 of 35 dys. = 665 dys. Hence, to increase the Cr. side by an equal amount of interest, the balance should remain unpaid 665 dys.; that is, the balance is due March 13, 1883.

#### 26.

The difference in equated time = 24 dys.

Balance of account = \$1000 - \$920 = \$80.

If the account were settled at the later date, June 23, the \$1000 on the Dr. side would have been on interest 24 dys., and this is equivalent to having the balance, \$80, on interest \(^{1880}\_{80}\) of 24 dys. = 300 dys.

Hence, the balance should begin to draw interest 300 dys. before June 23, 1881; that is, Aug. 27, 1880.

#### 27.

The difference in equated time is 83 dys.

Balance of account = \$ 20.

If the account were settled at the later date, July 6, the \$480 would have been on interest 83 dys., which is equivalent to having the balance, \$20, on interest 480 of 83 dys. = 1992 dys.

Hence, to increase the Dr. side by an equal amount of interest, the balance should remain unpaid 1992 dys.; that is, the balance is due Dec. 19, 1886.

Find (by either method) the cash balance in the following bills, reckoning interest at 6%:

28. 1881. 1881. INT. Dr. INT. Cr. Apr. 20. By cash, **\$**2.03 **\$**250 **\$**3.17 **\$**200 Apr. 5. To mdse. **..** 27. **" 30.** 610 5.49 **500** 4.25 200 0.63 June 4. 400 June 1. 1.07 " 20. By bal. int. " 20. To bal. acc. 40 1.94 **\$**1100 | **\$**9.29 **\$1100 | \$9.29** 

Hence, cash balance = \$40 - \$1.94 = \$38.06. Ans.

#### 29.

1881.		Dr.	Int.	1881.		Cr.	Int.
Apr. 15.	To mdse.	<b>\$25</b> 0.00	\$7.42	Apr. 26. I	By cash,	<b>\$</b> 150.00	\$4.18
May 25.	14	98.50		May 17.		150.00	l e
June 7.	41	300.00	6.25	July 7.	66	200.00	3.17
		;		Oct. 10. B	y bal. ac	c. 148.50	
•				" 10.		t.	4.94
		2010.70	212.01			2010.50	017.04
		<b>\$</b> 648.50	<b> \$15.94</b>	Į		\$648.50	\$15.94

Hence, cash balance = \$148.50 + \$4.94 = \$153.44. Ans.

#### **30**.

1881.		Dr.	INT.	1881.		Cr.	Int.
Feb. 2.	To mdse.	<b>\$</b> 100	<b>\$</b> 3.02	Feb. 25.	By cash,	<b>\$100</b>	<b>\$2.63</b>
Apr. 7.	"	200	3.90	Mar. 22.	46	150	3.33
June 2.	"	95		June 20.		200	
" 9.		150	1.35	Aug. 2.	By bal. a	cc. 95	
				" 2.	" ir	ıt.	. 1.85
		<b>\$545</b>	<b>\$</b> 9.24		•	<b>\$</b> 545	\$9.24

Hence, cash balance = \$95 + \$1.85 = \$96.85. Ans.

#### 31.

1881.		Dr.	INT.	1881.		Cr.	Int.
Apr. 5.	To mdse.	<b>\$</b> 250	<b>\$</b> 6.21	Apr. 20.	By cash	<b>\$200</b>	\$4.47
" 27.	44	670	14.18	" 30.	. 46	<b>5</b> 00	10.33
June 4.	46	200	2.97	June 1.	"	400	6.13
				Sept. 1. " 1.	By bal.	acc. 20	
				" 1.	46	int.	2.43
		\$1120	\$23.36			<b>\$</b> 1120	\$23.36

Hence, cash balance = \$20 + \$2.43 = \$22.43. Ans.

**32**.

1881.		Dr.	INT.	1881.		CR.	Int.
Mar. 10.	To mdse.	<b>\$</b> 580	\$8.31	Mar. 15.	By cash	<b>\$</b> 500	<b>\$</b> 6.75
Apr. 20.	"	200	1.50	Apr. 15.	"	<b>300</b> ·	2.50
May 5.	66	150	0.75	" 25.	44	120	0.80
<b>"</b> 17.	66	<b>325</b>	0.98	May 20.	44	<b>22</b> 5	0.56
				June 4.	By bal.	acc. 110	
				" <b>4.</b>	46	int.	0.93
		<b>\$</b> 1255	<b>\$</b> 11.54			<b>\$1255</b>	\$11.54

Hence, cash balance = \$110 + \$0.93 = \$110.93. Ans.

## EXERCISE LXXVII.

1. Find the square root of 2916.

2. Find the square root of 7921.

3. Find the square root of 494,209.

4. Find the square root of 20,164.

5. Find the square root of 3,345,241.

6. Find the square root of 125,457.64.

12/54/57.64 (354.2 9 65) 354 325 704) 2957 2816 7082) 14164 14164

7. Find the square root of 47,320,641.

47/32/06/41 (6879 36 128) 1132 1024 1367) 10806 9569 13749) 123741 123741

8. Find the square root of 21,609.

2/16/09 (147 1 24) 116 96 287) 2009 2009 9. Find the square root of 53.7289.

53.72/89(7.33 49 143)472 429 1463)4389 4389

10. Find the square root of 883.2784.

8/83.27/84(29.72 4 49)483 441 587)4227 4109 5942)11884 11884

11. Find the square root of 1.97262025.

1.97'26'20'25 (1.4045 1 24) 97 96 2804) 12620 11216 28085) 140425 140425 12. Find the square root of 0.0002090916.

13. Find the square root of 2.

14. Find the square root of 5.

15. Find the square root of 0.3. 0.30/00/00/00 (0.547722

16. Find the square root of 31.

$$3.25'00'00 (1.802775)$$
 $\frac{1}{28}$ 
 $\frac{1}{225}$ 
 $\frac{224}{204}$ 
 $3602) 10000$ 
 $\frac{7204}{3604) 27960}$ 
 $\frac{25228}{27320}$ 
 $\frac{25228}{20920}$ 
 $18020$ 

17. Find the square root of 85

18. Find the square root of 0.9.

$$0.90'00'00'00(0.948683)$$
 $81$ 
 $184) 900$ 
 $736$ 
 $1888) 16400$ 
 $15104$ 
 $18966) 129600$ 
 $113796$ 
 $18972) 158040$ 
 $151776$ 
 $62640$ 
 $56916$ 

19. Find in yards the side of a square field containing 20 acres.

20. Find the side of a square the area of which is 150 sq. ft. 9 sq. in.

124444

62222) 167900

150 sq. ft. 9 sq. in. = 21,609 sq. in.

$$\begin{array}{r}
2'16'09(147) \\
\underline{1} \\
24)116 \\
\underline{96} \\
287)\underline{96} \\
\underline{2009} \\
\underline{2009}
\end{array}$$

147 in. = 12 ft. 3 in.

21. Find the side of a square the area of which is 8 sq. yds. 7 sq. ft. 73 sq. in.

8 sq. yds. 7 sq. ft. 73 sq. in.
= 11,449 sq. in.

1'14'49(107

1
207)1449
1449

107 in. = 8 ft. 11 in.

22. Find to six places of decimals the square roots of  $\frac{4}{3}$ ;  $\frac{5}{3}$ ;  $\frac{5}{7}$ ;  $\frac{3}{4}$ ;  $\frac{3}{8}$ ;  $\frac{5}{7}$ .

$$\sqrt{\frac{4}{3}} = \frac{2}{3} = 0.666667.$$

(2) 
$$\frac{5}{5} = 0.5$$
.

0.55/55/55/55/55/55 (0.745355

```
(6)
              (3)
                                                   \frac{3}{4} = 0.75.
           \frac{1}{2} = 0.5.
                                              0.75'00'00'00 (0.866025
     0.50'00'00'00 (0.707106
       49
                                           166) 1100
  1407) 10000
                                                 996
         9849
                                          1726) 10400
   14141) 15100
                                                 10356
          14141
                                             17320) 44000
    14142) 95900
                                                     34640
            84852
                                                      93600
                                                      86600
              (4)
                                                      (7)
           \frac{3}{5} = 0.6.
                                               \mathbf{4} = 0.66666666.
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  147)\overline{1100}
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                                            161) 266
       1029
                                                 161
   1544) 7100
         6176
                                           1626) 10566
                                                  9756
   15485) 92400
                                            16324) 81066
           77425
                                                    65296
   15490) 149750
           139410
                                            16328) 157706
                                                    146952
            103400
             92940
                                                     107546
                                                      97968
              (5)
                                                      (8)
     = 0.714285714285.
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164) 742
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1685) 8685
                                                    3644
      8425
                                              1824) 15893
16901) 26071
                                                    14592
       16901
                                                      13013
169025) 917042
                                                      12768
        845125
1690304) 7191785
                                                        2453
                                                        1824
          6761216
```

23. Find, by factoring, the square roots of 2025; 17.64; 2.0164; 533.61; 204.49.

$$2025 = 5^{2} \times 9^{2}.$$

$$\therefore \sqrt{2025} = 5 \times 9 = 45. \quad (1) \text{ Ans.}$$

$$17.64 = 6^{2} \times 0.7^{2}.$$

$$\therefore \sqrt{17.64} = 6 \times 0.7 = 4.2. \quad (2) \text{ Ans.}$$

$$2.0164 = 2^{2} \times 0.71^{2}.$$

$$\therefore \sqrt{2.0164} = 2 \times 0.71 = 1.42. \quad (3) \text{ Ans.}$$

$$533.61 = 3^{2} \times 0.7^{2} \times 11^{2}.$$

$$\therefore \sqrt{533.61} = 3 \times 0.7 \times 11 = 23.1. \quad (4) \text{ Ans.}$$

$$204.49 = 11^{2} \times 1.3^{2}.$$

$$\therefore \sqrt{204.49} = 11 \times 1.3 = 14.3. \quad (5) \text{ Ans.}$$

24. A ladder 13 ft. long standing on level ground reaches a window 12 ft. from the ground. How far from the wall is the foot of the ladder?

$$\sqrt{(13+12)(13-12)} = \sqrt{25} = 5$$
 ft. Ans.

25. The two legs of a right triangle are 35 in. and 84 in. respectively. Find the hypotenuse.

$$\sqrt{35^2 + 84^2} = \sqrt{8281} = 91$$
 in. Ans.

23. The hypotenuse of a right triangle is 61 in., and one leg 11 in. Find the other leg.

$$\sqrt{(61+11)(61-11)} = \sqrt{3600} = 60$$
 in. Ans.

27. Find the longest straight line that can be drawn on the floor of a room 20 ft. by 15 ft.

$$\sqrt{20^2 + 15^2} = \sqrt{625} = 25$$
 ft. Ans.

28. Find the longest line in a box that is 8 ft. long, 4 ft. wide, 1 ft. deep.

$$\sqrt{8^2+4^2}=\sqrt{80}$$
.  $\sqrt{\sqrt{80^2+1^2}}=\sqrt{81}=9$  ft. Ans.

## EXERCISE LXXVIII.

1. Find the cube root of 1331.

$$\begin{array}{c|c}
 & 1/331(11) \\
3 \times 10^2 = 300 & 331 \\
3 (10 \times 1) = 30 & 331 \\
1^2 = 1 & 331 & 331
\end{array}$$

2. Find the cube root of 1728.

$$\begin{array}{c|c}
 & 1/728 (12) \\
 & 1 \\
 & 3 \times 10^{3} = 300 \\
 & 3 (10 \times 2) = 60 \\
 & 2^{3} = 4 \\
 & 364 \\
 & 728
 \end{array}$$

3. Find the cube root of 12.167.

$$3 \times 20^{2} = 1200 \\
3(20 \times 3) = 180 \\
3^{2} = 9 \\
1389$$
4167

4. Find the cube root of 300.763.

$$300.763 (6.7)$$

$$3 \times 60^{2} = 10800$$

$$3(60 \times 7) = 1260$$

$$7^{2} = 49$$

$$12109$$

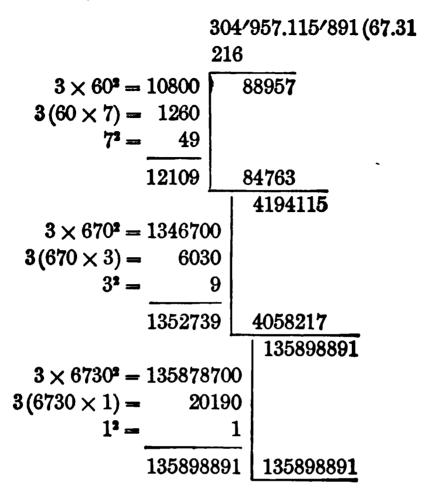
$$84763$$

5. Find the cube root of 148,877.

**6.** Find the cube root of 2,048,383.

7. Find the cube root of 59.776471.

#### 8. Find the cube root of 304957.115891.



### 9. Find the cube root of 0.007821346625.

$$\begin{array}{c|ccccc}
0.007/821/346/625 & (0.1985) \\
\hline
3 \times 10^2 &= 300 & 6821 \\
3(10 \times 9) &= 270 & 5859 \\
\hline
3 \times 190^2 &= 108300 & 962346 \\
3 \times 190^2 &= 108300 & 962346 \\
3(190 \times 8) &= 4560 & 903392 & 58954625 \\
\hline
3 \times 1980^2 &= 11761200 & 58954625 \\
\hline
3(1980 \times 5) &= 29700 & 58954625 \\
\hline
11790925 & 58954625
\end{array}$$

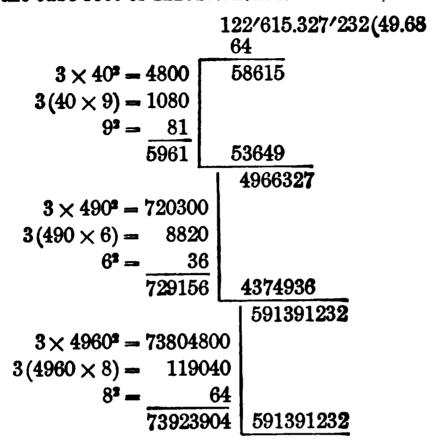
#### 10. Find the cube root of 104.600290750613.

104./600/290/750/613(4.7117 **64**  $3 \times 40^2 = 4800$ 40600  $3(40 \times 7) = 840$  $7^2 = 49$ 5689 39823 777290  $3 \times 470^2 = 662700$  $3(470 \times 1) =$ 1410  $1^2 =$ 664111 664111 113179750  $3 \times 4710^2 = 66552300$  $3(4710\times1) =$ 14130  $1^2 =$ 66566431 66566431 46613319613  $3 \times 47110^2 = 6658056300$  $3(47110 \times 7) =$ 989310 72 = 49 6659045659 46613319613

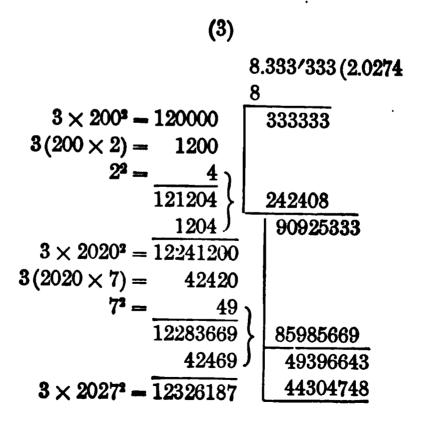
# 11. Find the cube root of 17,183,498,535,125.

17/183/498/535/125(25805 8  $3\times20^2=1200$ 9183  $3(20 \times 5) = 300$  $5^2 = 25$ 1525 7625 1558498  $3 \times 250^2 = 187500$  $3(250 \times 8) = 6000$  $8^2 =$ 193564 1548512 9986535125  $3 \times 25800^2 = 1996920000$  $3(25800 \times 5) =$ 387000  $5^2 =$ 1997307025 9986535125

12. Find the cube root of 122615.327232.



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14. Find the cube root of 5; \(\frac{5}{3}\); \(\frac{5}{

$$\begin{array}{c|c}
 & 5.000 (1.7099) \\
\hline
3 \times 10^2 = 300 & 4000 \\
3(10 \times 7) = 210 & 4000 \\
7^2 = 49 \\
\hline
559 & 3913 \\
259 & 87000000 \\
3 \times 1700^2 = 8670000 \\
3(1700 \times 9) = 45900 & 87000000 \\
9^2 = 81 \\
\hline
8715981 & 78443829 \\
\hline
85561710 & 78858387
\end{array}$$

(4) 0.750'000'000 (0.9085) 729  $3 \times 900^2 = 2430000$   $3(900 \times 8) = 21600$   $8^2 = \underbrace{64}_{2451664}$   $\underbrace{21664}_{2473392}$  19613312  $\underbrace{13866880}_{12366960}$  12366960

15. Find the entire surface of a cube the volume of which is 14 cu. ft. 705.088 cu. in.

14 cu. ft. 705.088 cu. in. × 1728 24192 cu. in. 705.088 24897.088 cu. in

$$3 \times 20^{3} = 1200 \\
3(20 \times 9) = 540 \\
9^{2} = 81 \\
1821 \\
621$$

$$16389 \\
16389 \\
508088$$

$$3 \times 290^{3} = 252300 \\
3(290 \times 2) = 1740 \\
2^{2} = 4 \\
254044$$

$$508088$$

$$29.2 \\
\times 29.2 \\
\times 29.2 \\
852.64 \text{ sq. in. in each face.}$$

$$6 \\
144)5115.84 \text{ sq. in.}$$

$$35 \text{ sq. ft. } 75.84 \text{ sq. in.}$$

#### EXERCISE LXXIX.

1. If the diameter of the moon be reckoned at 2000 mi., and that of the earth at 8000 mi., find the ratio of the surface of the moon to that of the earth. Also, find the ratio of the volume of the moon to that of the earth.

 $2000^2:8000^3 = 1^2:4^2 = 1:16.$  (1) Ans.  $2000^3:8000^3 = 1^3:4^3 = 1:64.$  (2) Ans.

2. If the diameter of the earth be reckoned at 8000 mi., that of Jupiter at 84,000 mi., and that of the sun at 880,000 mi., find the ratios of their volumes.

 $8000^{8}:84000^{8}:880000^{8}=2^{8}:21^{8}:220^{8}=8:9261:10648000$ . Ans.

3. If the diameters of two circles be 20 in. and 40 in. respectively, find the ratio of their circumferences and the ratio of their surfaces.

20: 40 = 1: 2. $20^2: 40^2 = 1^2: 2^2 = 1: 4.$  Ans.

4. If the areas of two circles be 8000 sq. in. and 36,000 sq. in. respectively, find the ratio of their diameters to the nearest thousandth of an inch.

 $\sqrt{8000}$ :  $\sqrt{36000} = \sqrt{4}$ :  $\sqrt{18} = 2$ : 4.242 = 1: 2.121. Ans.

5. If the volumes of two spheres be 100 cu. in. and 1000 cu. in. respectively, find the ratio of their diameters to the nearest thousandth of an inch.

 $\sqrt[8]{100}$ :  $\sqrt[8]{1000} = \sqrt[8]{1}$ :  $\sqrt[8]{10} = 1$ : 2.154. Ans.

6. If two stacks of hay of the same shape contain 4 t. 6 cwt. and 1 t. 8 cwt. respectively, find the ratio of their heights.

 $\sqrt[3]{86}$ :  $\sqrt[3]{28} = 4.414 : 3.037 = 1 : 0.688$ . Ans.

7. If an ox 7 ft. in girth weigh 1500 lbs., what will be the girth of a similar ox weighing 2500 lbs.?

 $\sqrt[8]{1500}$ :  $\sqrt[8]{2500}$ :: 7 ft.: what?

 $\sqrt[8]{1}$ :  $\sqrt[8]{\frac{3}{2}}$  : : 7 ft. : what?

1:1.186::7 ft.: what?

1:1.186::7 ft.:8.3 ft. Ans.

8. The surface of a pyramid is 560 sq. in. What is the surface of a similar pyramid whose volume is 27 times as great?

 $\sqrt[3]{1}: \sqrt[3]{27} = 1:3.$ 

12:32::560 sq. in.: what?

1:9::560 sq. in.:5040 sq. in. Ans.

9. The volume of a pyramid is 1331 cu. in. What is the volume of a similar pyramid whose surface is 4 times as great?

 $\sqrt{1}:\sqrt{4}=1:2.$ 

18: 28:: 1331 cu. in.: what?

1:8::1331 cu. in.: 10648 cu. in. Ans.

10. If a well-proportioned man 5 ft. 10 in. high weigh 160 lbs., what should a man 6 ft. high weigh, to the nearest tenth of a pound? What should be the height, to the nearest tenth of an inch, of a man weighing 210 lbs.?

5 ft. 10 in. = 70 in. 6 ft. = 72 in.

708: 728::160 lbs.: what?

343000: 373248:: 160 lbs.: 174.1 lbs. (1) Ans.

 $\sqrt[8]{160}$ :  $\sqrt[8]{210}$ :: 70 in.: what?

5.43:5.95::70 in.:76.6 in.

76.6 in. = 6 ft. 4.6 in. (2) Ans.

11. A three-gallon jug and a one-gallon jug are of the same shape. What, to the nearest thousandth, is the ratio of their diameters?

 $\sqrt[8]{3}$ :  $\sqrt[8]{1} = 1.443$ : 1 = 1: 0.693. Ans.

12. Two hills have exactly the same shape; one is 900 ft. high, the other 1200 ft. Find the ratio of their surfaces, and also the ratio of their volumes.

 $900^2: 1200^2 = 3^2: 4^2 = 9: 16.$  (1) Ans.  $900^3: 1200^3 = 3^3: 4^3 = 27: 64.$  (2) Ans.

13. A ball 3 in. in diameter weighs 4 lbs.; another ball of the same metal weighs 9 lbs. Find the diameter of the second ball to the nearest thousandth of an inch.

 $\sqrt[8]{4}$ :  $\sqrt[8]{9}$ :: 3 in.: what? 1.587: 2.080:: 3 in.: 3.931 in. Ans.

14. If Apollo's altar were a perfect cube 10 ft. on a side, what, to the nearest hundredth of an inch, would be the dimensions of a new cubical altar containing twice as much stone?

 $10 \times 10 \times 10 = 1000$  cu. ft.  $2 \times 1000 = 2000$  cu. ft.  $\sqrt[8]{1000}$ :  $\sqrt[8]{2000}$ :: 10: what? 10: 12.599: 10: 12.599 ft. 12.599 ft. = 12 ft. 7.19 in. Ans.

15. A man standing 40 ft. from a building 24 ft. wide observed that, when he closed one eye, the width of the building hid from view 90 rods of fence which was parallel to the width of the building. Find the distance from the eye of the observer to the fence.

24:40::90 rds.: what? 24:40::90 rds.:150 rds. Ans.

16. A bushel measure and a peck measure are of the same shape. Find the ratio of their heights.

1 bushel = 4 pecks.  $\sqrt[3]{4}$ :  $\sqrt[3]{1}$  = 1.587: 1 = 1:0.63. Ans.

#### EXERCISE LXXX.

Given:  $\log 2 = 0.3010$ ;  $\log 3 = 0.4771$ ;  $\log 5 = 0.6990$ ;  $\log 7 = 0.8451$ .

Find the logarithms of the following numbers by resolving the numbers into factors, and taking the sum of the logarithms of the factors.

1.  

$$\log 6 = \log (2 \times 3)$$
  
 $= \log 2 + \log 3$ .  
 $\log 2 = 0.3010$   
 $\log 3 = 0.4771$   
 $0.7781$ . Ans.

2.  

$$\log 15 - \log (3 \times 5)$$
  
 $= \log 3 + \log 5$ .  
 $\log 3 = 0.4771$   
 $\log 5 = 0.6990$   
1.1761. Ans.

3.  $\log 21 = \log (3 \times 7)$   $= \log 3 + \log 7$ .  $\log 3 = 0.4771$   $\log 7 = 0.8451$ 1.3222. Ans.

5.  

$$\log 35 = \log (5 \times 7)$$
  
 $= \log 5 + \log 7$ .  
 $\log 5 = 0.6990$   
 $\log 7 = 0.8451$   
1.5441. Ans.

log 
$$9 = \log(3 \times 3)$$
  
 $= \log 3 + \log 3$ .  
log  $3 = 0.4771$   
log  $3 = 0.4771$   
 $0.9542$ . Ans.

7.  

$$\log 8 = \log (2 \times 2 \times 2)$$

$$= \log 2 + \log 2 + \log 2$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$0.9030. Ans.$$

8.  

$$\log 49 = \log (7 \times 7)$$
  
 $= \log 7 + \log 7$ .  
 $\log 7 = 0.8451$   
 $\log 7 = 0.8451$   
 $1.6902$ . Ans.

$$\log 25 = \log (5 \times 5)$$

$$= \log 5 + \log 5.$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$1.3980. Ans.$$

10.

$$\log 30 = \log (2 \times 3 \times 5)$$

$$= \log 2 + \log 3 + \log 5.$$

$$\log 2 = 0.3010$$

$$\log 3 = 0.4771$$

$$\log 5 = 0.6990$$

$$1.4771. Ans.$$

11.

$$\log 42 = \log (2 \times 3 \times 7)$$

$$= \log 2 + \log 3 + \log 7.$$

$$\log 2 = 0.3010$$

$$\log 3 = 0.4771$$

$$\log 7 = 0.8451$$

$$1.6232. Ans.$$

12.

$$\log 420 = \log (2 \times 2 \times 3 \times 5 \times 7)$$

$$= \log 2 + \log 2 + \log 3$$

$$+ \log 5 + \log 7.$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$\log 3 = 0.4771$$

$$\log 5 = 0.6990$$

$$\log 7 = 0.8451$$
2.6232. Ans.

**13**.

$$\log 12 = \log (2 \times 2 \times 3)$$

$$= \log 2 + \log 2 + \log 3.$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$\log 3 = 0.4771$$

$$1.0791. Ans.$$

14.

$$\log 60 = \log (2 \times 2 \times 3 \times 5)$$

$$= \log 2 + \log 2 + \log 3$$

$$+ \log 5.$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$\log 3 = 0.4771$$

$$\log 5 = 0.6990$$

$$1.7781. Ans.$$

**15**.

$$\log 75 = \log (3 \times 5 \times 5)$$

$$= \log 3 + \log 5 + \log 5.$$

$$\log 3 = 0.4771$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$1.8751. Ans.$$

$$\log 7.5 = \log (5 \times 5 \times 3 \times 0.1)$$

$$= \log 5 + \log 5 + \log 3$$

$$+ \log 0.1$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 3 = 0.4771$$

$$\log 0.1 = 9.0000 - 10$$

$$0.8751. Ans.$$

$$\log 0.021 = \log (3 \times 7 \times 0.001)$$

$$= \log 3 + \log 7$$

$$+ \log 0.001.$$

$$\log 3 = 0.4771$$

$$\log 7 = 0.8451$$

$$\log 0.001 = 7.0000 - 10$$

$$8.3222 - 10. Ans.$$

#### 18.

log 
$$0.35 - \log (5 \times 7 \times 0.01)$$
  
 $-\log 5 + \log 7$   
 $+\log 0.01$ .  
log  $5 - 0.6990$   
log  $7 = 0.8451$   
log  $0.01 - 8.0000 - 10$   
 $9.5441 - 10$ . Ans.

#### **19**.

$$\log 0.0035 = \log (5 \times 7 \times 0.0001)$$

$$= \log 5 + \log 7$$

$$+ \log 0.0001.$$

$$\log 5 = 0.6990$$

$$\log 7 = 0.8451$$

$$\log 0.0001 = 6.0000 - 10$$

$$7.5441 - 10. Ans.$$

#### 20

$$\log 0.004 = \log (2 \times 2 \times 0.001)$$

$$= \log 2 + \log 2$$

$$+ \log 0.001.$$

$$\log 2 = 0.3010$$

$$\log 2 = 0.3010$$

$$\log 0.001 = 7.0000 - 10$$

$$7.6020 - 10, Ans.$$

$$\log 0.05 = \log (5 \times 0.01)$$

$$= \log 5 + \log 0.01.$$

$$\log 5 = 0.6990$$

$$\log 0.01 = 8.0000 - 10$$

$$8.6990 - 10. Ans.$$

#### 22.

 $\log 12.5 = \log (5 \times 5 \times 5 \times 0.1)$ 

$$= \log 5 + \log 5 + \log 5 + \log 5 + \log 0.1.$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 0.1 = 9.0000 - 10$$

$$1.0970. Ans.$$

#### 23.

 $\log 1.25 = \log (5 \times 5 \times 5 \times 0.01)$ 

$$= \log 5 + \log 5 + \log 5$$

$$+ \log 0.01.$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 0.01 = 8.0000 - 10$$

$$0.0970. Ans.$$

$$\log 37.5 = \log (3 \times 5 \times 5 \times 5 \times 0.1)$$

$$= \log 3 + \log 5 + \log 5$$

$$+ \log 5 + \log 0.1.$$

$$\log 3 = 0.4771$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 5 = 0.6990$$

$$\log 0.1 = 9.0000 - 10$$

$$1.5741. Ans.$$

	25.
log	$2.1 = \log\left(3 \times 7 \times 0.1\right)$
•	$= \log 3 + \log 7 + \log 0.1$ .
log	3 = 0.4771
log	7 = 0.8451
log	0.1 = 9.0000 - 10
	0.3222. Ans.
	26.
log	$16 = \log(2 \times 2 \times 2 \times 2)$
	$= \log 2 + \log 2 + \log 2$
	$+\log 2$
log	2 = 0.3010

# 1.2040. Ans. 27. $\log 0.056 = \log (2 \times 2 \times 2 \times 7 \times 0.001)$ $= \log 2 + \log 2 + \log 2$ $+ \log 7 + \log 0.001.$ $\log 2 = 0.3010$ $\log 2 = 0.3010$ $\log 2 = 0.3010$

2 = 0.3010

2 = 0.3010

2 = 0.3010

log

log

log

log

$$\log 0.001 = \frac{7.0000 - 10}{8.7481 - 10}$$
 Ans.

7 = 0.8451

28.  $\log 0.63 = \log (3 \times 3 \times 7 \times 0.01)$   $= \log 3 + \log 3 + \log 7$   $+ \log 0.01$ .  $\log 3 = 0.4771$   $\log 3 = 0.4771$   $\log 3 = 0.4771$   $\log 0.01 = 8.0000 - 10$ 9.7993 - 10. Ans.

29.  $1.75 = \log(5 \times 5 \times 7 \times 0.01)$ log  $= \log 5 + \log 5 + \log 7$  $+ \log 0.01$ . 5 = 0.6990log 5 - 0.6990log · log 7 = 0.84510.01 = 8.0000 - 10log 0.2431. Ans. **30**.  $105 = \log(3 \times 5 \times 7)$ log  $= \log 3 + \log 5 + \log 7.$ log 3 - 0.47715 = 0.6990log 7 = 0.8451log 2.0212. Ans. 31.  $\log 0.0105 - \log (3 \times 5 \times 7 \times 0.0001)$  $= \log 3 + \log 5 + \log 7$ 

## 31. $\log 0.0105 = \log (3 \times 5 \times 7 \times 0.0001)$ $= \log 3 + \log 5 + \log 7$ $+ \log 0.0001.$ $\log 3 = 0.4771$ $\log 5 = 0.6990$ $\log 7 = 0.8451$ $\log 0.0001 = 6.0000 - 10$ 8.0212 - 10. Ans.

32.  $\log 1.05 = \log (3 \times 5 \times 7 \times 0.01)$   $= \log 3 + \log 5 + \log 7$   $+ \log 0.01.$   $\log 3 = 0.4771$   $\log 5 = 0.6990$   $\log 7 = 0.8451$   $\log 0.01 = 8.0000 - 10$  0.0212. Ans.

#### EXERCISE LXXXI.

Given:  $\log 2 = 0.3010$ ;  $\log 3 = 0.4771$ ;  $\log 5 = 0.6990$ ;  $\log 7 = 0.8451$ .

Find logarithms of the following:

1. 
$$\log 2^6 = 3 \times \log 2 = 3 \times 0.3010 = 0.9030$$
. Ans.

2. 
$$\log 5^2 = 2 \times \log 5 = 2 \times 0.6990 = 1.3980$$
. Ans.

3. 
$$\log 7^4 = 4 \times \log 7 = 4 \times 0.8451 = 3.3804$$
. Ans.

4. 
$$\log 3^8 = 8 \times \log 3 = 8 \times 0.4771 = 3.8168$$
. Ans.

5. 
$$\log 7^3 = 3 \times \log 7 = 3 \times 0.8451 = 2.5353$$
. Ans.

6. 
$$\log 5^5 = 5 \times \log 5 = 5 \times 0.6990 = 3.4950$$
. Ans.

7. 
$$\log 2^{\frac{1}{5}} = \frac{1}{3}$$
 of  $\log 2 = \frac{1}{3}$  of  $0.3010 = 0.1003$ . Ans.

8. 
$$\log 5^{\frac{1}{2}} = \frac{1}{2}$$
 of  $\log 5 = \frac{1}{2}$  of  $0.6990 = 0.3495$ . Ans.

9. 
$$\log 3^{\frac{1}{8}} = \frac{1}{8}$$
 of  $\log 3 = \frac{1}{8}$  of  $0.4771 = 0.0596$ . Ans.

10. 
$$\log 7^{\frac{1}{5}} = \frac{1}{5}$$
 of  $\log 7 = \frac{1}{5}$  of  $0.8451 = 0.1690$ . Ans.

11. 
$$\log 5^{\frac{1}{5}} = \frac{1}{5}$$
 of  $\log 5 = \frac{1}{5}$  of  $0.6990 = 0.1398$ . Ans.

12. 
$$\log 7^{\frac{1}{11}} = \frac{1}{11}$$
 of  $\log 7 = \frac{1}{11}$  of  $0.8451 = 0.0768$ . Ans.

13. 
$$\log 2^{\frac{3}{4}} = \frac{3}{4}$$
 of  $\log 2 = \frac{3}{4}$  of  $0.3010 = 0.2258$ . Ans.

14. 
$$\log 5^{\frac{2}{3}} - \frac{2}{3}$$
 of  $\log 5 - \frac{2}{3}$  of  $0.6990 - 0.4660$ . Ans.

15. 
$$\log 3^{\frac{3}{7}} - \frac{3}{7}$$
 of  $\log 3 = \frac{3}{7}$  of  $0.4771 = 0.2045$ . Ans.

16. 
$$\log 7^{\frac{2}{7}} - \frac{2}{7}$$
 of  $\log 7 - \frac{2}{7}$  of  $0.8451 = 0.2415$ . Ans.

17. 
$$\log 5^{\frac{5}{3}} = \frac{5}{3}$$
 of  $\log 5 = \frac{5}{3}$  of  $0.6990 = 1.1650$ . Ans.

18. 
$$\log 3^{\frac{9}{11}} = \frac{9}{11}$$
 of  $\log 3 = \frac{9}{11}$  of  $0.4771 = 0.3904$ . Ans.

19. 
$$\log 7^{\frac{7}{2}} = \frac{7}{2}$$
 of  $\log 7 = \frac{7}{2}$  of  $0.8451 = 2.9579$ . Ans.

**20.** 
$$\log 3^{\frac{4}{3}} = \frac{4}{3}$$
 of  $\log 3 = \frac{4}{3}$  of  $0.4771 = 0.6361$ . Ans.

**21.** 
$$\log 5^{\frac{7}{2}} = \frac{7}{2}$$
 of  $\log 5 = \frac{7}{2}$  of  $0.6990 = 2.4465$ . Ans.

**22.** 
$$\log 2^{\frac{11}{7}} = \frac{11}{7}$$
 of  $\log 2 = \frac{11}{7}$  of  $0.3010 = 0.4730$ . Ans.

**23.** 
$$\log 5^{\frac{3}{4}} = \frac{3}{4}$$
 of  $\log 5 = \frac{3}{4}$  of  $0.6990 = 0.5243$ . Ans.

**24.** 
$$\log 7^{\frac{11}{7}} = \frac{1}{7}$$
 of  $\log 7 = \frac{1}{7}$  of  $0.8451 = 1.3280$ . Ans.

**25.** 
$$\log 21^{\frac{7}{8}} = \frac{7}{8}$$
 of  $\log 21 = \frac{7}{8}$  of  $\log (3 \times 7)$   
=  $\frac{7}{8}$  of  $(0.4771 + 0.8451)$   
=  $\frac{7}{8}$  of  $1.3222 = 1.1569$ . Ans.

#### EXERCISE LXXXII.

Given:  $\log 2 = 0.3010$ ;  $\log 3 = 0.4771$ ;  $\log 5 = 0.6990$ ;  $\log 7 = 0.8451$ .

Find logarithms for the following quotients:

log 
$$\frac{2}{5} = \log 2 + \operatorname{colog} 5 - 10.$$
  
log  $2 = 0.3010$   
 $\operatorname{colog} 5 - 10 = \underbrace{9.3010 - 10}_{9.6020 - 10.}$  Ans.

log 
$$\frac{2}{7} = \log 2 + \operatorname{colog} 7 - 10.$$
  
log  $2 = 0.3010$   
 $\operatorname{colog} 7 - 10 = \underbrace{9.1549 - 10}_{9.4559 - 10.}$  Ans.

3.  

$$\log \frac{3}{5} = \log 3 + \operatorname{colog} 5 - 10.$$
  
 $\log 3 = 0.4771$   
 $\operatorname{colog} 5 - 10 = 9.3010 - 10$   
 $9.7781 - 10.$  Ans.

log 
$$\frac{8}{7} = \log 3 + \operatorname{colog} 7 - 10.$$
  
log  $3 = 0.4771$   
colog  $7 - 10 = 9.1549 - 10$   
 $9.6320 - 10$ . Ans.

5.  

$$\log \frac{5}{7} = \log 5 + \operatorname{colog} 7 - 10.$$
  
 $\log 5 = 0.6990$   
 $\operatorname{colog} 7 - 10 = 9.1549 - 10$   
 $9.8539 - 10.$  Ans.

6.  

$$\frac{7}{5} = \log 7 + \cos 5 - 10.$$
  
 $\log 7 = 0.8451$   
 $\cos 5 - 10 = 9.3010 - 10$   
 $0.1461.$  Ans.

7. 
$$\log \frac{\$}{\$} = \log 5 + \operatorname{colog} 3 - 10.$$

$$\log 5 = 0.6990$$

$$\operatorname{colog} 3 - 10 = 9.5229 - 10$$

$$0.2219. \ Ans.$$
8. 
$$\log \frac{\$}{\$} = \log 5 + \operatorname{colog} 2 - 10.$$

$$\log 5 = 0.6990$$

$$\operatorname{colog} 2 - 10 = 9.6990 - 10$$

$$0.3980. \ Ans.$$
10. 
$$\log 2 = \log 6990 - 10$$

$$0.5441. \ Ans.$$

$$\log 3 = \log 3 + \operatorname{colog} 2 - 10.$$

$$\log 3 = 0.4771$$

$$\operatorname{colog} 2 - 10 = 9.6990 - 10$$

$$0.1761. \ Ans.$$
12. 
$$\log 7 = 0.8451$$

$$\operatorname{colog} 3 - 10 = 9.5229 - 10$$

$$0.3680. \ Ans.$$
10. 
$$\log 7 = 0.8451$$

$$\operatorname{colog} 2 - 10 = 9.6990 - 10$$

$$0.1761. \ Ans.$$
12. 
$$\log 7 = 0.8451$$

$$\operatorname{colog} 3 - 10 = 9.5229 - 10$$

$$10 = 9.5229 - 10$$

$$10 = 9.6990 - 10$$

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$$10 = 9.6990$$

log  $\frac{0.005}{2} = \log 0.005 + \operatorname{colog} 2 - 10.$ log 0.005 = 7.6990 - 10 $\operatorname{colog} 2 - 10 = \frac{9.6990 - 10}{7.3980 - 10}$ . Ans.

$$\frac{5}{0.07} = \log 5 + \operatorname{colog} 0.07 - 10.$$

$$\log \qquad 5 = 0.6990$$

$$\operatorname{colog} 0.07 - 10 = 11.1549 - 10$$

$$1.8539. Ans.$$

17.

$$\log \frac{3}{0.007} = \log 3 + \operatorname{colog} 0 \ 007 - 10.$$

$$\log \quad 3 = 0.4771$$

$$\operatorname{colog} 0.007 - 10 = \underbrace{12.1549 - 10}_{2.6320. \ \textit{Ans.}}$$

18.

$$\frac{0.003}{7} = \log 0.003 + \operatorname{colog} 7 - 10.$$

$$\log \qquad 0.003 = 7.4771 - 10$$

$$\operatorname{colog} \qquad 7 - 10 = 9.1549 - 10$$

$$6.6320 - 10. \quad Ans.$$

19.

$$\frac{0.05}{0.003} = \log 0.05 + \operatorname{colog} 0.003 - 10.$$

$$\log \qquad 0.05 = 8.6990 - 10$$

$$\operatorname{colog} 0.003 - 10 = 12.5229 - 10$$

$$1.2219. Ans.$$

log 
$$\frac{0.007}{0.02} = \log 0.007 + \operatorname{colog} 0.02 - 10.$$
  
log  $0.007 = 7.8451 - 10$   
colog  $0.02 - 10 = 11.6990 - 10$   
 $9.5441 - 10$ . Ans.

$$\log \frac{0.02}{0.007} = \log 0.02 + \operatorname{colog} 0.007 - 10.$$

$$\log \quad 0.02 = 8.3010 - 10$$

$$\operatorname{colog} 0.007 - 10 = \underbrace{12.1549 - 10}_{0.4559}$$

22.

$$\frac{0.005}{0.07} = \log 0.005 + \operatorname{colog} 0.07 - 10.$$

$$\log \quad 0.005 = 7.6990 - 10$$

$$\operatorname{colog} \quad 0.07 - 10 = 11.1549 - 10$$

$$8.8539 - 10. \text{ Ans.}$$

23.

$$\frac{0.03}{7} = \log 0.03 + \operatorname{colog} 7 - 10,$$

$$\log \qquad 0.03 = 8.4771 - 10$$

$$\operatorname{colog} \qquad 7 - 10 = 9.1549 - 10$$

$$7.6320 - 10. Ans.$$

24.

$$\frac{0.0007}{0.2} = \log 0.0007 + \operatorname{colog} 0.2 - 10.$$

$$\log \quad 0.0007 = 6.8451 - 10$$

$$\operatorname{colog} \quad 0.2 - 10 = \underbrace{10.6990 - 10}_{7.5441 - 10.} \text{ Ans.}$$

$$\frac{0.02^2}{3^3} = \log 0.02^2 + \operatorname{colog} 3^3 - 10.$$

$$\log \quad 0.02^2 = 6.6020 - 10$$

$$\operatorname{colog} \quad 3^3 - 10 = 8.5687 - 10$$

$$5.1707 - 10. \quad Ans.$$

$$\log \frac{3^{3}}{0.02^{2}} = \log 3^{3} + \operatorname{colog} 0.02^{2} - 10.$$

$$\log \quad 3^{3} = 1.4313$$

$$\operatorname{colog} \quad 0.02^{2} - 10 = 13.3980 - 10$$

$$4.8293. \ Ans.$$

$$\frac{7^{3}}{0.02^{2}} = \log 7^{3} + \operatorname{colog} 0.02^{2} - 10.$$

$$\log \qquad 7^{3} = 2.5353$$

$$\operatorname{colog} \quad 0.02^{2} - 10 = 13.3980 - 10$$

$$5.9333. \quad Ans.$$

28.

$$\frac{0.07^{3}}{0.003^{3}} = \log 0.07^{3} + \operatorname{colog} 0.003^{3} - 10.$$

$$\log \qquad 0.07^{3} = 6.5353 - 10$$

$$\operatorname{colog} 0.003^{3} - 10 = 17.5687 - 10$$

$$4.1040. Ans.$$

29.

log 
$$\frac{0.005^2}{7^3} = \log 0.005^2 + \operatorname{colog} 7^3 - 10.$$
log 
$$0.005^2 = 5.3980 - 10$$
colog 
$$7^3 - 10 = \underbrace{7.4647 - 10}_{2.8627 - 10.} Ans.$$

log 
$$\frac{7^3}{0.005^2} = \log 7^8 + \operatorname{colog} 0.005^2 - 10.$$
  
log  $7^3 = 2.5353$   
colog  $0.005^2 - 10 = 14.6020 - 10$   
 $7.1373$ . Ans.

#### EXERCISE LXXXIII.

Find logarithms of the following numbers.

1.

log 70 = 1,8451. Ans.

2

log 101 = 2,0043. Ans.

3.

log 333 = 2.5224. Ans,

4.

log  $3491 = 3.5428 + (\frac{1}{16} \text{ of } 13) = 3.5429$ . Ans.

ii.

log  $1866 = 3.2695 + (\frac{6}{10} \text{ of } 23) = 3.2709$ . Ans.

6.

log  $6897 = 3.8382 + (\frac{7}{10} \text{ of } 6) = 3.8386$ . Ans.

7.

log  $9901 = 3.9956 + (\frac{1}{10} \text{ of } 5) = 3.9957$ . Ans.

A.

log  $4389 = 3.6415 + (\frac{9}{10} \text{ of } 10) = 3.6424$ , Ans.

9,

log  $1111 = 3.0453 + (\frac{1}{10} \text{ of } 39) = 3.0457$ . Are.

10.

 $\log 58343 = 4.7657 + (\frac{44}{105} \text{ of } 7) = 4.7660$ . Ans.

11.

log  $77860 = 4.8910 + (\frac{40}{100} \text{ of } 5) = 4.8913$ . Ans.

12.

log  $30127 = 4.4786 + (\frac{87}{100} \text{ of } 14) = 4.4790$ . Ans.

13.

 $\log 730.84 = 2.8633 + (\frac{84}{100} \text{ of } 6) = 2.8638$ . Ans.

$$\log 0.008765 = 7.9425 + (\frac{5}{10} \text{ of } 5) - 10 = 7.9428 - 10.$$
 Ans.

15.

log 
$$8.0808 = 0.9074 + (\frac{8}{100} \text{ of } 5) = 0.9074$$
. Ans.

16.

$$\log 5.0009 = 0.6990 + (\frac{9}{100} \text{ of } 8) = 0.6991$$
. Ans.

17.

$$\log 0.3769 = 9.5752 + (\frac{9}{10} \text{ of } 11) - 10 = 9.5762 - 10.$$
 Ans.

**18**.

$$\log 0.070707 = 8.8494 + (\frac{7}{100} \text{ of } 6) - 10 = 8.8494 - 10$$
. Ans.

19.

$$\log 0.03723 = 8.5705 + (\frac{8}{10} \text{ of } 12) - 10 = 8.5709 - 10$$
. Ans.

20.

$$\log 98.871 = 1.9948 + (\frac{71}{100} \text{ of } 4) = 1.9951$$
. Ans.

#### 21. Find antilog 3.9017.

The number corresponding to the mantissa 9015 is 7970. The number corresponding to the mantissa 9020 is 7980. The difference between these numbers is 10, and  $7970 + \frac{2}{5}$  of 10 = 7974. Ans.

#### 22. Find antilog 1.2076.

The number corresponding to the mantissa 2068 is 1610. The number corresponding to the mantissa 2095 is 1620. The difference between these numbers is 10,

and  $1610 + \frac{8}{27}$  of 10 = 1613.

Therefore, the number required is 16.13. Ans.

#### 23. Find antilog 0.4442.

The number corresponding to the mantissa 4440 is 2780. The number corresponding to the mantissa 4456 is 2790. The difference between these numbers is 10,

and  $2780 + \frac{2}{16}$  of 10 = 2781.

Therefore, the number required is 2.781. Ans.

#### 24. Find antilog 1.0090.

The number corresponding to the mantissa 0086 is 1020. The number corresponding to the mantissa 0128 is 1030. The difference between these numbers is 10,

and

 $1020 + \frac{4}{42}$  of 10 = 1021.

Therefore, the number required is 10.21. Ans.

#### 25. Find antilog 2.9850.

The number corresponding to the mantissa 9850 is 9660. Therefore, the number required is 966. Ans.

#### 26. Find antilog 4.5388.

The number corresponding to the mantissa 5378 is 3450. The number corresponding to the mantissa 5391 is 3460. The difference between the numbers is 10, and  $3450 + \frac{19}{2}$  of 10 = 3458.

Therefore, the number required is 34,580. Ans.

#### 27. Find antilog 0.8550.

The number corresponding to the mantissa 8549 is 7160. The number corresponding to the mantissa 8555 is 7170. The difference between these number is 10,

and  $7160 + \frac{1}{2}$  of 10 = 7162.

Therefore, the number required is 7.162. Ans.

#### 28. Find antilog 9.9992 - 10.

The number corresponding to the mantissa 9991 is 9980. The number corresponding to the mantissa 9996 is 9990.

The difference between these numbers is 10,

and  $9980 + \frac{1}{3}$  of 10 = 9982.

Therefore, the number required is 0.9982. Ans.

#### **29.** Find antilog 8.7324 - 10.

The number corresponding to the mantissa 7324 is 5400. Therefore, the number required is 0.0540. Ans.

#### **30.** Find antilog 9.5555 - 10.

The number corresponding to the mantissa 5551 is 3590. The number corresponding to the mantissa 5563 is 3600.

The difference between these numbers is 10,

$$3590 + \frac{4}{12}$$
 of  $10 = 3593$ .

Therefore, the number required is 0.3593. Ans.

#### 31. Find antilog 6.0216 - 10.

The number corresponding to the mantissa 0212 is 1050. The number corresponding to the mantissa 0253 is 1060.

The difference between these numbers is 10,

and

$$1050 + \frac{4}{41}$$
 of  $10 = 1051$ .

Therefore, the number required is 0.0001051. Ans.

#### 32. Find antilog 7.0080 - 10.

The number corresponding to the mantissa 0043 is 1010.

The number corresponding to the mantissa 0086 is 1020.

The difference between these numbers is 10,

and

$$1010 + \frac{37}{43}$$
 of  $10 = 1019$ .

Therefore, the number required is 0.001019. Ans.

#### 33. Find by logarithms the product $948.22 \times 0.4387$ .

$$\log 948.22 = 2.9769$$
  
 $\log 0.4387 = 9.6422 - 10$ 

$$2.6191 - \log 416$$
. Ans.

#### 34. Find by logarithms the product $1.9704 \times 0.0786$ .

$$\log 1.9704 = 0.2946$$

$$\log 0.0786 = 8.8954 - 10$$

$$9.1900 - 10 = \log 0.1549$$
. Ans.

#### 35. Find by logarithms the product $380.25 \times 0.00673$ .

$$\log 380.25 = 2.5801$$

$$\log 0.00673 = 7.8280 - 10$$

$$0.4081 = \log 2.559$$
. Ans.

36. Find by logarithms the product  $216.21 \times 0.76312$ .

$$\log 216.21 = 2.3349$$

$$\log 0.76312 = 9.8826 - 10$$

$$2.2175 = \log 165. Ans.$$

37. Find by logarithms the product  $0.56127 \times 1.2312$ .

$$\log 0.56127 = 9.7492 - 10$$

$$\log 1.2312 = 0.0903$$

$$9.8395 - 10 = \log 0.691$$
. Ans.

38. Find by logarithms the product  $0.86311 \times 56.371$ .

$$\log 0.86311 = 9.9361 - 10$$

$$\log 56.371 = 1.7511$$

$$1.6872 - \log 48.67$$
Ans.

39. Find by logarithms the product  $59.795 \times 0.7955$ .

$$\log 59.795 = 1.7767 
\log 0.7955 = 9.9007 - 10 
\hline
1.6774 = 47.58. Ans.$$

40. Find by logarithms the product  $270.05 \times 0.0087$ .

$$\log 270.05 = 2.4315 
\log 0.0087 = 7.9395 - 10 
0.3710 = \log 2.349. Ans.$$

41. Find by logarithms the product  $11.163 \times 0.3333$ .

$$\log 11.163 = 1.0478$$

$$\log 0.3333 = 9.5228 - 10$$

$$0.5706 = \log 3.721. Ans.$$

42. Find by logarithms the product  $777.78 \times 0.0787$ .

$$\log 777.78 = 2.8909$$

$$\log 0.0787 = 8.8960 - 10$$

$$1.7869 = \log 61.21. Ans.$$

43. Find by logarithms the product  $2.6537 \times 0.2313$ .

$$\log 2.6537 = 0.4238$$

$$\log 0.2313 = 9.3642 - 10$$

$$9.7880 - 10 = \log 0.6137. Ans.$$

44. Find by logarithms the product  $37.587 \times 12.371$ .

$$\log 37.587 = 1.5750 
\log 12.371 = 1.0924 
2.6674 - \log 464.9. Ans.$$

45. Find by logarithms the product  $89.313 \times 2.3781$ .

$$\log 89.313 = 1.9510$$

$$\log 2.3781 = 0.3762$$

$$2.3272 = \log 212.4. Ans.$$

46. Find by logarithms the product  $9.1765 \times 0.00089$ .

$$\log 9.1765 = 0.9627$$

$$\log 0.00089 = 6.9494 - 10$$

$$7.9121 - 10 = \log 0.008168. Ans.$$

**47.** Find the quotient of  $\frac{56.407}{13.045}$ .

$$\log \quad 56.407 = 1.7513$$

$$\operatorname{colog} 13.045 = 8.8846 - 10$$

$$0.6359 = \log 4.324. \text{ Ans.}$$

**48.** Find the quotient of  $\frac{857.06}{3079.8}$ 

$$\log 857.06 = 2.9330$$

$$\operatorname{colog} 3079.8 = 6.5114 - 10$$

$$9.4444 - 10 = \log 0.2783. \text{ Ans.}$$

**49.** Find the quotient of  $\frac{0.9387}{598.6}$ .

$$\begin{array}{c} \log & 0.9387 = 9.9726 - 10 \\ \text{colog} & 598.6 = 7.2229 - 10 \\ \hline & 7.1955 - 10 = \log 0.001569. \ \textit{Ans.} \end{array}$$

50. Find the quotient of  $\frac{3069}{0.7891}$ .

$$\log \quad 3069 = 3.4870$$

$$\operatorname{colog} 0.7891 = \underbrace{10.1028 - 10}_{3.5898} = \log 3889. \text{ Ans.}$$

**51.** Find the quotient of  $\frac{75.46 \times 0.0765}{93.08 \times 98.071}$ .

$$\begin{array}{c} \log & 75.46 = 1.8777 \\ \log & 0.0765 = 8.8837 - 10 \\ \operatorname{colog} & 93.08 = 8.0312 - 10 \\ \operatorname{colog} & 98.071 = 8.0084 - 10 \\ \hline & 6.8010 - 10 & = \log 0.0006324. \ \textit{Ans.} \end{array}$$

**52.** Find the quotient of  $\frac{98 \times 537 \times 0.0079}{67309 \times 0.0947}$ .

53. Find the quotient of  $\frac{314 \times 7.18 \times 8132}{519 \times 827 \times 3.215}$ 

log 
$$314 = 2.4969$$
  
log  $7.18 = 0.8561$   
log  $8132 = 3.9102$   
colog  $519 = 7.2848 - 10$   
colog  $827 = 7.0825 - 10$   
colog  $3.215 = 9.4928 - 10$   
 $1.1233 = \log 13.28$ . Ans.

**54.** Find the quotient of  $\frac{212 \times 2.16 \times 8002}{536 \times 351 \times 7.256}$ 

log 
$$212 = 2.3263$$
  
log  $2.16 = 0.3345$   
log  $8002 = 3.9032$   
colog  $536 = 7.2708 - 10$   
colog  $351 = 7.4547 - 10$   
colog  $7.256 = 9.1393 - 10$   
 $0.4288 = \log 2.684$ . Ans.

55. Find by logarithms 5.068.

$$3 \log 5.06 = 3 \times 0.7042 = 2.1126$$
  
 $2.1126 = \log 129.6$ . Ans.

56. Find by logarithms 2.5015.

$$5 \log 2.501 = 5 \times 0.3981 = 1.9905$$
  
1.9905 =  $\log 97.84$ . Ans.

57. Find by logarithms 1.7167.

$$7 \log 1.716 = 7 \times 0.2345 = 1.6415$$
  
 $1.6415 = \log 43.8$ . Ans.

**58.** Find by logarithms 1.17810.

$$10 \log 1.178 = 10 \times 0.0712 = 0.7120$$
  
 $0.7120 = \log 5.153$ . Ans.

**59.** Find by logarithms 0.76856.

$$6 \log 0.7685 = 6 \times (9.8857 - 10) = 9.3142 - 10$$
  
 $9.3142 - 10 = \log 0.2061$ . Ans.

60. Find by logarithms 0.96118.

$$8 \log 0.9611 = 8 \times (9.9828 - 10) = 9.8624 - 10$$
  
 $9.8624 - 10 = \log 0.7285$ . Ans.

61. Find by logarithms 0.02312.

$$2 \log 0.0231 = 2 \times (8.3636 - 10) = 6.7272 - 10$$
  
 $6.7272 - 10 = \log 0.0005336$ . Ans.

62. Find by logarithms 0.85678.

$$3 \log 0.8567 - 3 \times (9.9329 - 10) - 9.7987 - 10$$
  
 $9.7987 - 10 - \log 0.629$ . Ans.

63. Find by logarithms  $(\frac{61}{2})^4$ .

$$4 \log 61 - 4 \times 1.7853 - 7.1412$$
  
 $4 \operatorname{colog} 73 - 4 \times (8.1367 - 10) - 2.5468 - 10$   
 $9.6880 - 10 - \log 0.4876$ . Ans.

64. Find by logarithms (1).

$$3 \log 13 = 3 \times 1.1139 = 3.3417$$
  
 $3 \operatorname{colog} 71 = 3 \times (8.1487 - 10) = 4.4461 - 10$   
 $7.7878 - 10 = \log 0.006134$ . Ans.

65. Find by logarithms (16)5.

$$5 \log 16 = 5 \times 1.2041$$
 =  $5.0205$   
 $5 \operatorname{colog} 9 = 5 \times (9.0458 - 10) = 5.2290 - 10$   
 $0.2495$  =  $\log 17.76$ . Ans.

66. Find by logarithms (35)8.

$$3 \log 35 = 3 \times 1.5441$$
 =  $4.6323$   
 $3 \operatorname{colog} 4 = 3 \times (9.3979 - 10) = 8.1937 - 10$   
 $2.8260$  =  $\log 699.9$ . Ans.

67. Find by logarithms  $(5\frac{5}{11})^2$ .

$$2 \log 60 = 2 \times 1.7782 = 3.5564$$
  
 $2 \operatorname{colog} 11 = 2 \times (8.9586 - 10) = \frac{79172 - 10}{1.4736} = \log 29.76$ . Ans.

68. Find by logarithms  $(44)^{3}$ .

$$3 \log 128 = 3 \times 2.1072 = 6.3216$$
  
 $3 \operatorname{colog} 31 = 3 \times (8.5086 - 10) = 5.5258 - 10$   
 $1.8474 = \log 70.37$ . Ans.

69. Find by logarithms (233).

$$5 \log 103 = 5 \times 2.0128 = 10.0640$$
  
 $5 \operatorname{colog} 37 = 5 \times (8.4318 - 10) = 2.1590 - 10$   
 $2.2230 = \log 167.1$ . Ans.

70. Find by logarithms  $(\frac{871}{71})^8$ .

$$3 \log 871 = 3 \times 2.9400 = 8.8200$$
  
 $3 \operatorname{colog} 711 = 3 \times (7.1481 - 10) = 1.4443 - 10$   
 $0.2643 = \log 1.838$ . Ans.

71. Find by logarithms 131.

$$\frac{1}{2} \log 13 = \frac{1}{2} \text{ of } 1.1139 = 0.3713 = \log 2.351.$$
 Ans.

72. Find by logarithms 29<sup>1</sup>/<sub>5</sub>.

$$\frac{1}{5}\log 29 = \frac{1}{5} \text{ of } 1.4624 = 0.2925 = \log 1.961. Ans.$$

73. Find by logarithms 87916.

$$\frac{1}{10} \log 879 = \frac{1}{10}$$
 of  $2.9440 = 0.2944 = \log 1.97$ . Ans.

74. Find by logarithms  $0.609^{\frac{1}{2}}$ .

$$\log 0.609 = 9.7846 - 10$$

$$30. \quad -30$$

$$4)39.7846 - 40$$

$$9.9462 - 10 = \log 0.8834. Ans.$$

**75.** Find by logarithms 93.73<sup>1</sup>/<sub>2</sub>.

$$\frac{1}{2} \log 93.73 = \frac{1}{2}$$
 of  $1.9719 = 0.9860 = \log 9.683$ . Ans.

76. Find by logarithms 21.978.

$$\frac{5}{6} \log 21.97 = \frac{5}{6} \text{ of } 1.3418 = 1.1182 = \log 13.13. Ans.}$$

77. Find by logarithms 7.935.

$$\frac{5}{7} \log 7.935 = \frac{5}{7} \text{ of } 0.8996 = 0.6426 = \log 4.391. Ans.}$$

78. Find by logarithms 0.815<sup>3</sup>/<sub>4</sub>.

$$\log 0.815 = .9.9112 - 10$$

$$3$$

$$29.7336 - 30$$

$$10 - 10$$

$$4)39.7336 - 40$$

$$9.9334 - 10 = \log 0.8578$$
Ans.

79. What weight of sulphuric acid, specific gravity 1.841, will fill a silver sphere 138<sup>mm</sup> in diameter?

$$\log 138^{8} = 6.4197$$

$$\log 0.5236 = 9.7190 - 10$$

$$\log 1.841 = 0.2650$$

$$6.4037 = \log 2534000.$$

That is, 2534000cmm = 2.534ks. Ans.

80. What is the area of a circle 13.75 in. in diameter?

$$\log 6.875^2 = 1.6746$$

$$\log 3.1416 = 0.4971$$

$$2.1717 = \log 148.5.$$

That is, 148.5 sq. in. Ans.

81. Find the depth of a cubical bin that holds 75 bu.

That is, 54.44 in. Ans.

82. Find the diameter of a 24-lb. shot, specific gravity 7.6.

That is, 5.504 in. Ans.

#### EXERCISE LXXXIV.

1. What number is 3 less than its square?

**Assume 2.3 and 2.4.** 

$$2.3^2 - 2.3 = 5.29 - 2.3 = 2.99$$
, an error of  $-0.01$ .

$$2.4^2 - 2.4 = 5.76 - 2.4 = 3.36$$
, an error of  $+ 0.36$ .

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.37.

Hence, error of 2.3:0.1::0.01:0.37,

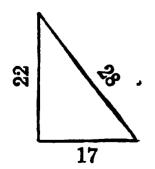
or, error of 2.3:0.1::1:37.

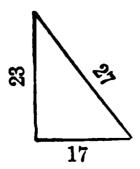
Therefore, the error of  $2.3 = \frac{1 \times 0.1}{37} = 0.0028$ .

2.3 + 0.0028 = 2.3028. Ans.

2. A flag-staff 50 ft. high broke, and the top falling over rested one end on the stump and the other 17 ft. from its base. How high was the stump?

Assume 22 ft. and 23 ft.





$$22^2 + 17^2 = 484 + 289 = 773$$
, an error of  $-11$ .

$$23^2 + 17^2 = 529 + 289 = 818$$
, an error of +89.

The difference of the assumed numbers is 1, and the difference of the errors is 100.

Hence, the error of 22:1::11:100.

Therefore, the error of  $22 - \frac{1 \times 11}{100} = 0.11$ .

22 + 0.111 - 22.11 ft. Ans.

#### 3. What number added to eight times its reciprocal is equal to 8?

Assume 1.1 and 1.2.

$$1.1 + 8 \times \frac{1}{1.1} = 1.1 + 7.273 = 8.373$$
, an error of + 0.373.

$$1.2 + 8 \times \frac{1}{1.2} = 1.2 + 6.667 = 7.867$$
, an error of  $-0.133$ .

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.506.

Hence, the error of 1.1:0.1::0.373:0.506,

or, the error of 1.1:0.1::373:506.

Therefore, the error of  $1.1 = \frac{1 \times 373}{506} = 0.0737$ .

1.1 + 0.0737 = 1.1737. Ans.

Assume 6.8 and 6.9.

$$6.8 + 8 \times \frac{1}{6.8} = 6.8 + 1.177 = 7.977$$
, an error of  $-0.023$ .

$$6.9 + 8 \times \frac{1}{6.9} = 6.9 + 1.159 = 8.059$$
, an error of + 0.059.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.082.

Hence, the error of 6.8: 0.1::0.023:0.082,

or, the error of 6.8:0.1::23:82.

Therefore, the error of  $6.8 = \frac{1 \times 23}{82} = 0.028$ .

$$6.8 + 0.028 = 6.828$$
. Ans.

#### 4. Find a number whose reciprocal is equal to 4 minus the number.

Assume 3 and 4.

$$\frac{1}{3} = 4 - 3$$
, or  $\frac{1}{3} = 1$ , an error of  $+ \frac{2}{3}$ .

$$\frac{1}{4} = 4 - 4$$
, or  $\frac{1}{4} = 0$ , an error of  $\frac{1}{4}$ .

The difference of the assumed numbers is 1, and the difference of the errors is  $\frac{1}{12}$ .

Hence, the error of  $3:1::\frac{2}{3}:\frac{11}{12}$ ,

or, the error of 3:1::8:11.

Therefore, the error of  $3 = \frac{1 \times 8}{11} = 0.73$ .

3 + 0.73 = 3.73. Ans.

Assume 0.26 and 0.27.

$$\frac{1}{0.26} = 4 - 0.26$$
, or  $3.846 = 3.74$ , an error of  $-0.106$ .

$$\frac{1}{0.27} = 4 - 0.27$$
, or  $3.704 = 3.73$ , an error of  $+ 0.026$ .

The difference of the assumed numbers is 0.01, and the difference of the errors is 0.132.

Hence, the error of 0.26:0.01::0.106:0.132,

or, the error of 0.26: 0.01::53:66.

Therefore, the error of  $0.26 = \frac{0.01 \times 53}{66} = 0.008$ .

0.26 + 0.008 = 0.268. Ans.

#### 5. What number is ten times its own logarithm?

Assume 1.3 and 1.5.

$$1.3 = 10 \times 0.1139$$
, or  $1.3 = 1.139$ , an error of  $-0.161$ .

$$1.5 = 10 \times 0.1761$$
, or  $1.5 = 1.761$ , an error of  $+0.261$ .

The difference of the assumed numbers is 0.2, and the difference of the errors is 0.422.

Hence, the error of 1.3:0.2::0.161:0.422,

or, the error of 1.3: 0.2:: 161: 422.

Therefore, the error of  $1.3 = \frac{161 \times 0.2}{422} = 0.07$ 

Assume 1.37 and 1.38.

 $1.37 - 10 \times 0.1367$ , or 1.37 - 1.367, an error of -0.003.

 $1.38 - 10 \times 0.1399$ , or 1.38 - 1.399, an error of + 0.019.

The difference of the assumed numbers is 0.01, and the difference of the errors is 0.022.

Hence, the error of 1.37: 0.01:: 0.003: 0.022.

or, the error of 1.37:0.01::3:20

Therefore, the error of  $1.37 - \frac{3 \times 0.01}{22} - 0.0013$ .

Therefore the number is 1.37 + 0.0013 = 1.3713. Ans. The number 10 also satisfies the conditions.

#### 6. What number is double its own cube root?

Assume 2.8 and 2.9.

 $2\sqrt[8]{2.8} = 2.82$ , an error of + 0.02.

 $2\sqrt[3]{2.9}$  = 2.85, an error of = 0.05.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.07.

Hence, the error of 2.8:0.1::0.02:0.07,

or, the error of 2.8: 0.1::2:7.

Therefore, the error of  $2.8 - \frac{0.1 \times 2}{7} = 0.0284$ .

2.8 + 0.0284 = 2.8284. Ans.

#### 7. What number exceeds its cube root by 61?

Assume 8.2 and 8.3.

 $8.2 - \sqrt[3]{8.2} = 6.184$ , an error of -0.066.

 $8.3 - \sqrt[8]{8.3} = 6.275$ , an error of +0.025.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.091.

Hence, the error of 8.2: 0.1:: 0.066: 0.091,

or, the error of 8.2: 0.1:: 66:91.

Therefore, the error of  $8.2 - \frac{0.1 \times 66}{91} = 0.072$ .

8.2 + 0.072 = 8.272. Ans.

#### 8. What is the number which added to its own square makes 11?

Assume 2.8 and 2.9.

 $2.8 + 2.8^2 = 10.64$ , an error of -0.36.

 $2.9 + 2.9^2 = 11.31$ , an error of + 0.31.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.67.

Hence, the error of 2.8:0.1::0.36:0.67,

or, the error of 2.8: 0.1::36:67.

Therefore, the error of  $2.8 = \frac{0.1 \times 36}{67} = 0.054$ .

2.8 + 0.054 = 2.854. Ans.

### 9. What is the number which multiplied by 10 makes 8 more than the square of the number?

Assume 9.1 and 9.2.

 $10 \times 9.1 = 9.1^2 + 8$ , or 91 = 90.81, an error of -0.19.

 $10 \times 9.2 = 9.2^2 + 8$ , or 92 = 92.64, an error of + 0.64.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.83.

Hence, the error of 9.1:0.1::0.19:0.83

or, the error of 9.1:0.1::19:83.

Therefore, the error of  $9.1 = \frac{0.1 \times 19}{83} = 0.023$ .

9.1 + 0.023 = 9.123. Ans.

Assume 0.87 and 0.88.

 $10 \times 0.87 = 0.87^2 + 8$ , or 8.7 = 8.7569, an error of + 0.0569.

 $10 \times 0.88 = 0.88^2 + 8$ , or 8.8 = 8.7744, an error of -0.0256.

The difference of the assumed numbers is 0.01, and the difference of the errors is 0.0825.

Hence, the error of 0.87:0.01::0.0569:0.0825,

or, the error of 0.87:0.01::569:825.

Therefore, the error of  $0.87 = \frac{0.01 \times 569}{825} = 0.0069$ .

0.87 + 0.0069 = 0.8769. Ans.

10. A certain number is equal to the sum of \(\frac{1}{6}\) its own cube plus \(\frac{1}{6}\) its own square. What is the number?

Assume 1.81 and 1.82.

$$\frac{1.81^8}{6} + \frac{1.81^2}{4} = 1.8073$$
, an error of  $-0.0027$ .

$$\frac{1.82^6}{6} + \frac{1.82^2}{4} = 1.8329$$
, an error of + 0.0128.

The difference of the assumed numbers is 0.01, and the difference of the errors is 0.0156.

Hence, the error of 1.81: 0.01:: 0.0027: 0.0156, or, the error of 1.81: 0.01:: 9:52.

Therefore, the error of  $1.81 = \frac{0.01 \times 9}{52} = 0.0017$ .

1.81 + 0.0017 = 1.8117. Ans.

11. What number is equal to its square minus three times its logarithm?

Assume 1.1 and 1.2.

 $1.1^2 - 3 \times 0.0414 = 1.0858$ , an error of -0.0142.

 $1.2^2 - 3 \times 0.0792 = 1.2024$ , an error of + 0.0024.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.0166.

Hence, the error of 1.1:0.1::0.0142:0.0166, or, the error of 1.1:0.1::71:83.

Therefore, the error of  $1.1 = \frac{0.1 \times 71}{83} = 0.086$ .

1.1 + 0.086 = 1.186. Ans.

12. The sum of the square and the square root of a number, being divided by 1 plus the number, gives a quotient of  $2\frac{1}{4}$ . What is the number?

Assume 2.7 and 2.8.

$$\frac{2.7^2 + \sqrt{2.7}}{1 + 2.7} = \frac{8.933}{3.7} = 2.415$$
, an error of  $-0.085$ .

$$\frac{2.8^2 + \sqrt{2.8}}{1 + 2.8} = \frac{9.513}{3.8} = 2.503$$
, an error of + 0.003.

The difference of the assumed numbers is 0.1, and the difference of the errors is 0.088.

Hence, the error of 2.7: 0.1:: 0.085: 0.088, or, the error of 2.7: 0.1:: 85: 88.

Therefore, the error of  $2.7 = \frac{0.1 \times 85}{88} = 0.096$ .

2.7 + 0.096 - 2.796. Ans.

#### EXERCISE LXXXV.

1. Convert \$\frac{2}{11}\$, \$\frac{13}{75}\$, \$\frac{29}{127}\$, \$\frac{135}{64}\$ into continued fractions.

3)11(3  

$$\frac{9}{2}$$
)3(1  
 $\frac{2}{1}$ )2(2  
 $\frac{2}{2}$ 

13)75(5  

$$\frac{65}{10}$$
)13(1  
 $\frac{10}{3}$ )10(3  
 $\frac{9}{1}$ )3(3  
 $\frac{3}{2}$ 

29)127(4
$$\frac{116}{11)29(2}$$

$$\frac{22}{7})11(1)$$

$$\frac{7}{4})7(1$$

$$\frac{4}{3})4(1$$

$$\frac{3}{1})3(3$$

$$\frac{3}{1})7(7$$

$$\frac{(3)}{4+\frac{1}{4+\frac{1}{2+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{3}}}}}}}$$

$$\frac{(4)}{9+\frac{1}{7}}$$

$$\frac{135}{64} = 2\frac{7}{64}$$

$$\frac{135}{64} = 2 + \frac{1}{9+\frac{1}{7}}$$
Ans.

2. Find the approximate values of  $\frac{39}{29}$ ;  $\frac{53}{47}$ ;  $\frac{734}{851}$ .

Find the approximate values of 
$$\frac{20}{27}$$
;  $\frac{83}{47}$ ;  $\frac{784}{651}$ .

$$\begin{array}{c}
20)27(1 \\
\underline{20} \\
7)20(2 \\
\underline{14} \\
6)7(1 \\
\underline{6} \\
1)6(6 \\
\underline{6} \\
1)6(7 \\
\underline{6} \\
1)6(7 \\
\underline{6} \\
1)6(1 \\
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734)851(1 (3) 
$$\frac{734}{117)734(6}$$
  $\frac{702}{32)117(3}$   $\frac{96}{21)32(1}$   $\frac{21}{11)21(1}$   $\frac{11}{10)11(1}$   $\frac{10}{11+\frac{1}{6}}=\frac{6}{7}$   $\frac{1}{1+\frac{1}{6}+\frac{1}{3}}=\frac{1}{6+\frac{1}{3}}$   $\frac{1}{1+\frac{1}{6}+\frac{1}{3}}=\frac{69}{80}$   $\frac{1}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{29}$   $\frac{1}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{1+\frac{1}{6}+\frac{1}{3}}=\frac{1}{1+\frac{1}{1}+\frac{1}{1}}=\frac{69}{80}$   $\frac{1}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{1+\frac{1}{6}+\frac{1}{3}}=\frac{25}{1+\frac{1}{6}+\frac{1}{3}}=\frac{1}{1+\frac{1}{1}+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1}}=\frac{1}{1+\frac{1}{1$ 

3. Find common fractions approximating to 0.236; 0.2361; 1.609.

Find common fractions approximating to 0.236; 0.2361
$$\begin{array}{c}
(1) \\
0.236 \neq \frac{236}{1000} = \frac{59}{150}. \\
59)250(4 \\
\frac{236}{14})59(4 \\
\frac{56}{3})14(4 \\
\frac{12}{2})3(1 \\
\frac{2}{1})2(2 \\
\frac{2}{2})
\end{array}$$

$$\frac{1}{4} = \frac{1}{4}.$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{4}{17}.$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{17}{72}.$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{17}{17}.$$

$$0.2361 = \frac{2861}{10000}.$$

$$2361)10000(4)$$

$$\frac{9444}{556)2361(4)}$$

$$\frac{2224}{137)556(4)}$$

$$\frac{548}{8)137(17)}$$

$$\frac{136}{1)8(8)}$$

$$\frac{8}{8}$$

$$\frac{1}{4} = \frac{1}{4}$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{4}{17}$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{293}{1241}$$

$$\frac{1}{4 + \frac{1}{4}} = \frac{4}{17}$$

$$\frac{1}{4 + \frac{1}{4 + \frac{1}{4}}} = \frac{17}{72}$$

(3)
$$1.609 = 1 + \frac{609}{10000}.$$

$$609)10000(1) \frac{609}{391)609(1} \therefore 1 + \frac{609}{10000} = 1 + \frac{1}{1 + \frac$$

4. Find common fractions approximating to 0.382; 1.732; 0.6253.

4. Find common fractions approximating to 0.382; 1.732; 0.6253.

(1)

0.382 = 
$$\frac{1882}{18050} = \frac{1}{180}$$
.

191)500(2

 $\frac{382}{118}$ )191(1

 $\frac{118}{73}$ )118(1

 $\frac{73}{45}$ )73(1

 $\frac{45}{28}$ )45(1

 $\frac{28}{17}$ )28(1

 $\frac{17}{11}$ )17(1

 $\frac{11}{6}$ )11(1

 $\frac{6}{5}$ )6(1

 $\frac{5}{1}$ )5(6

$$\frac{1}{2} + \frac{1}{1} = \frac{1}{3}$$
.

 $\frac{1}{2 + \frac{1}{1 + \frac{1}{1}}} = \frac{2}{5}$ .

 $\frac{1}{2 + \frac{1}{1 + \frac{1}{1}}} = \frac{3}{8}$ .

 $\frac{1}{2 + \frac{1}{1 + \frac{1}{1}}} = \frac{3}{8}$ .

 $\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{8}{21}$ .

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$$\frac{1}{2 + \frac{1}{1 + \frac{1$$

$$1 + \frac{1}{1} = 2. \qquad 1 + \frac{1}{1 + \frac{1}{2}} = \frac{71}{41}$$

$$1 + \frac{1}{1 + \frac{1}{2}} = \frac{5}{3}$$

$$1 + \frac{1}{1 + \frac{1}{2}} = \frac{7}{4}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{97}{56}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{19}{11}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{168}{97}.$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{28}{15}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{168}{97}.$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}}$$

$$2, \frac{5}{5}, \frac{7}{4}, \frac{16}{15}, \frac{25}{15}, \frac{71}{47}, \frac{57}{56}, \frac{157}{47}. Ans.$$

$$(3)$$

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{1}} = \frac{262}{419}$$

$$\frac{1}{1 + \frac{1}{1}} = \frac{1}{2}$$

$$\frac{1}{1 + \frac{1}{1}} = \frac{2}{3}$$

$$\frac{1}{1 + \frac{1}{1}} = \frac{5}{8}$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{5}{8}$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{257}{411}$$

$$1, \frac{1}{2}, \frac{3}{3}, \frac{3}{3}, \frac{257}{417}, \frac{252}{419}, \frac{781}{1249}$$

$$Ans.$$

5. Find approximate values of  $\frac{1}{457}$ ;  $\frac{618}{557}$ ;  $\frac{211}{518}$ ;  $\frac{237}{118}$ .

$$\begin{array}{c}
171)457(2 \\
\frac{342}{115})171(1 \\
\underline{115} \\
56)115(2 \\
\underline{112} \\
3)56(18 \\
\underline{54} \\
2)3(1 \\
2 \\
1)2(2 \\
\underline{1})2(2 \\
2
\end{array}$$

$$\begin{array}{c}
1 \\
\frac{171}{457} = \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}}}} \\
\frac{1}{2 + \frac{1}{1 + \frac{1}{2}}} \\
\underline{1} = \frac{1}{3} \\
\underline{1} = \frac{1}{3}
\end{array}$$

$$\frac{1}{2 + \frac{1}{1 + \frac{1}{2}}} - \frac{3}{8}$$

$$\frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{18}}}} = \frac{55}{147}$$

$$\frac{\frac{1}{2+\frac{1}{1+\frac{1}{2+\frac{1}{18+\frac{1}{1}}}}} = \frac{58}{155}$$

1, 1, 8, 55, 58. Ans.

$$\therefore \frac{$13}{787} = \frac{1}{1 + \frac{1}{4 + \frac{1}{3 + \frac{1}{4 + \frac{1}{4}}}}}$$

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{4}} = \frac{4}{5}$$

$$\frac{1}{1+\frac{1}{4+\frac{1}{3}}} = \frac{13}{16}$$

$$\frac{1}{1+\frac{1}{4+\frac{1}{3+\frac{1}{1}}}} - \frac{17}{21}$$

$$\frac{1}{1+\frac{1}{4+\frac{1}{3+\frac{1}{1+\frac{1}{8}}}}} = \frac{\frac{149}{184}}{1}$$

1, 4, 18, 17, 112. Ane.

(3)

$$\frac{711}{818} = \frac{287}{271}.$$

237)271(1 237 34)237(6 204 33)34(1 33 1)33(33 33

$$\therefore \frac{247}{1+\frac{1}{6+\frac{1}{1+\frac{1}{33}}}} = \frac{1}{1+\frac{1}{33}}$$

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{6 + \frac{1}{1}}} = \frac{7}{8}.$$

$$\frac{1}{1 + \frac{1}{6}} = \frac{6}{7}.$$

$$1, \frac{4}{7}, \frac{7}{8}. Ans.$$

(4)

$$\frac{987}{113} = 8\frac{88}{113}$$
.

33)113(3 99 14)33(2 28 5)14(2 10 4)5(1 4 1)4(4 4

$$\therefore 8\frac{33}{1113} = 8 + \frac{1}{3 + \frac{1}{2 + \frac{1}{2 + \frac{1}{1 + \frac{1}{4}}}}}$$

$$8 = 8.$$

$$8 + \frac{1}{3} = 8\frac{1}{3}.$$

$$8 + \frac{1}{3 + \frac{1}{2}} = 8\frac{1}{3}.$$

$$8 + \frac{1}{3 + \frac{1}{2 + \frac{1}{2}}} = 8\frac{5}{17}.$$

$$8 + \frac{1}{3 + \frac{1}{2 + \frac{1}{1}}} = 8\frac{7}{24}.$$

8, 81, 87, 85, 87, 87. Ans.

6. Find the proper fraction that, when reduced to a continued fraction, will have 2, 3, 5, 6, 7 as quotients.

$$\frac{1}{2 + \frac{1}{3 + \frac{1}{5 + \frac{1}{6 + \frac{1}{7}}}} = \frac{709}{1640}. \quad Ans. \qquad \frac{1}{6\frac{1}{7}} = \frac{7}{43}; \qquad \frac{1}{5\frac{7}{43}} = \frac{43}{222}; \\ \frac{1}{3\frac{43}{222}} = \frac{222}{709}; \qquad \frac{1}{2\frac{233}{763}} = \frac{709}{1640};$$

7. Find a series of fractions approximating to the ratio of the pound troy (5760 grs.) to the pound avoirdupois (7000 grs.).

8. Find a series of fractions approximating to the ratio of the side of a square to its diagonal; that ratio being 1: 1.414214 nearly.

of a square to its diagonal; that ratio being 1: 1.414214 nearly. 
$$\frac{1}{1.414214} = \frac{1000000}{1414214} = \frac{7071}{10000}.$$

$$7071)10000(1) \quad \therefore \frac{7071}{2929} = \frac{1}{1 + \frac{1}{2 + \frac{1}{2$$

9. Find a series of fractions approximating to the ratio of the ar to the square chain, from the equality 1 ar = 0.2471 of a square chain.

10. Find a series of fractions approximating to the ratio of the 48pound shot to the weight of the French shot of 24kg.

$$48 \text{ lbs.} = 48 \times 0.45359 = 21.77232 \frac{1}{1000} = \frac{907}{1000}.$$

$$907)1000(1) \frac{21.77232}{93)907(9} = \frac{907}{1000}.$$

$$\frac{837}{70)93(1} \frac{70}{23)70(3} = \frac{1}{1 + \frac{1}{3 + \frac{1}{23}}}$$

$$\frac{69}{1)23(23)}$$

$$\frac{1}{1} = 1. \frac{1}{1 + \frac{1}{9}} = \frac{9}{10}. \frac{1}{1 + \frac{1}{9 + \frac{1}{1}}} = \frac{10}{11}. \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{3}}}} = \frac{39}{43}.$$

$$1, \frac{9}{10}, \frac{10}{11}, \frac{39}{43}. Ans.$$

11. If the mean diameter of the Earth is reckoned at 7912 mi., and that of Mars 4189 mi., find a series of fractions approximating to the ratio of the mean diameters of these two planets.

12. Find a series of fractions approximating to the ratio of a cubic yard to a cubic meter from the equality

1 cu. yd. = 0.76453 of a cubic meter.

 $0.76453 = \frac{76453}{1000000}.$  76453)100000(1)  $\frac{76453}{23547)76453(3)}$   $\frac{70641}{5812)23547(4)}$   $\frac{23248}{23248}$  0.764533  $\frac{76453}{1000000} = \frac{1}{1 + \frac{1}{3 + \frac{1}{4 + \frac{1}{19 + \frac{1}{2}}}}}$ 

$$\frac{1}{1} = 1.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{3}{4}.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{3}{4}.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{13}{17}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4}}} = \frac{13}{17}.$$

$$1, \frac{3}{4}, \frac{13}{17}, \frac{350}{327}.$$
Ans.

13. Find a series of fractions approximating to the ratio of the kilometer to the mile, from the equality  $1^m = 1.09362$  yds.

13. Find a series of fractions approximating to the ratio of the illometer to the mile, from the equality 
$$1^{m} = 1.09362$$
 yds.  $1^{km} = 1.09362$  yds.  $1^{km} = 0.621$  mi.  $0.621 = \frac{621}{10000}$ .  $0.621 = \frac{621}{11}$ .

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{3}}}}} = \frac{18}{29}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3 + \frac{1}{3}}}}}} - \frac{59}{95}$$

### EXERCISE LXXXVI.

1. Find the seventh term of the series 3, 5, 7.....

$$3 + (6 \times 2) = 3 + 12 = 15$$
, Ans.

2. Find the fifteenth term of the series 2, 7, 12.....

$$2 + (14 \times 5) = 2 + 70 = 72$$
. Ans.

3. Find the sixth term of the series 2, 25, 35.....

$$2 + (5 \times 5) = 2 + 35 = 55$$
. Ans

4. Find the twentieth term of the series 2, 31, 41.....

$$2 + (1\frac{1}{4} \times 19) = 2 + 23\frac{3}{4} = 25\frac{3}{4}$$
.

5. Find the seventh term of the series 21, 19, 17.....

$$21 - (6 \times 2) = 21 - 12 = 9$$
. Ans.

6. Find the twelfth term of the series 18, 171, 162.....

$$18 - (11 \times \frac{2}{3}) = 18 - 7\frac{1}{3} = 10\frac{2}{3}$$
.

7. When the first term of a series is 5, and the common difference 2½, find the thirteenth and eighteenth terms.

$$5 + (12 \times 2\frac{1}{4}) = 5 + 27 = 32.$$
 (1)

$$5 + (17 \times 2\frac{1}{4}) = 5 + 38\frac{1}{4} - 43\frac{1}{4}$$
. (2)

8. Find the common difference in a series whose fourth term is 12 and seventh term 27.

$$\frac{27-12}{3}=5$$
. Ans.

9. Find the common difference in a series whose first term is 20 and fourth term 40.

$$\frac{40-20}{3}=6$$
2. Ans.

10. Find the common difference in a series whose first term is 2 and eleventh term 20.

$$\frac{20-2}{10}=1\frac{4}{5}. Ans.$$

11. Find the common difference in a series whose third term is 7 and eighth term 12½.

$$\frac{12\frac{1}{5}-7}{5}=1.1. \ Ans.$$

12. Find the common difference in a series whose first term is 1 and fourth term 19.

$$\frac{19-1}{3}=6$$
. Ans.

## EXERCISE LXXXVII.

1. Find the sum of 1+5+9+.... to twenty terms.

$$l = 1 + (19 \times 4) = 77.$$
  
 $s = 20 \times \frac{1 + 77}{2} = 780.$  Ans.

2. Find the sum of  $4 + 5\frac{1}{2} + 7$  + .... to eight terms.

$$l=4+(7\times 1\frac{1}{2})=14\frac{1}{2}$$
.  
 $s=8\times \frac{4+14\frac{1}{2}}{2}=74$ . Ans.

3. Find the sum of  $8 + 7\frac{3}{5} + 7\frac{1}{5}$ + .... to sixteen terms.

$$l = 8 - (15 \times \frac{1}{3}) = 3.$$
  
 $s = 16 \times \frac{8+3}{2} = 88.$  Ans.

4. Find the sum of  $20 + 18\frac{1}{4} + 16\frac{1}{2} + \cdots$  to seven terms.

$$l = 20 - (6 \times 1\frac{3}{4}) = 9\frac{1}{2}.$$

$$s = 7 \times \frac{20 + 9\frac{1}{2}}{2} = 103\frac{1}{4}. Ans.$$

5. Find the sum of the first twenty natural numbers.

$$s = 20 \times \frac{1+20}{2} = 210$$
. Ans.

6. Find the sum of the natural numbers from 37 to 53 inclusive.

$$s = 17 \times \frac{37 + 53}{2} = 765$$
. Ans.

7. Find the sum of a series of thirty terms, of which the first is 21 and the last 59.

$$s = 30 \times \frac{21 + 59}{2} = 1200$$
. Ans.

8. Find the sum of the series whose first two terms are 3 and 9 and last 75.

$$l = a + (n - 1) d.$$

$$75 = 3 + 6n - 6.$$

$$6n = 78.$$

$$n = 13.$$

$$s = 13 \times \frac{3 + 75}{2} = 507. Ans.$$

9. Find the sum of a series of twenty terms whose third and fifth terms are 10 and 15.

$$d = \frac{10 + 15}{2} - 2\frac{1}{2}.$$

$$l = 5 + (19 \times 2\frac{1}{2}) = 52\frac{1}{2}.$$

$$s = 20 \times \frac{5 + 52\frac{1}{2}}{2} = 575. \text{ Ans.}$$

10. A stone, when dropped from a height, falls through 16.1 ft. in the first second, 48.3 in the next, 80.5 in the third, and so on, in arithmetical progression. How far will it fall in the seventh second? and how far in 7 sec.?

7th term is 
$$16.1 + (6 \times 32.2) = 209.3$$
 ft. (1) Ans.  
 $s = 7 \times \frac{16.1 + 209.3}{2} = 788.9$  ft. (2) Ans.

11. A, who travels 8 mi. the first day, 11 the second, 14 the third, and so on, overtakes in 17 dys. B, who started at the same time, and travelled uniformly. What is B's rate per day?

$$l = 8 + (16 \times 3) = 56.$$
  
 $s = 17 \times \frac{8 + 56}{2} = 544.$   
 $\frac{544}{17} = 32 \text{ mi. } Ans.$ 

12. One hundred stones lie in a straight line, 1 yd. apart. A boy starts at the first stone, brings each of the others in separately, and piles them with the first stone. How far does he travel?

$$l = 2 + (98 \times 2) = 198 \text{ yds.}$$
  
 $s = 99 \times \frac{1}{2}(2 + 198) = 9900 \text{ yds.}$   
 $9900 \text{ yds} = 53 \text{ mi. } Ans.$ 

# EXERCISE LXXXVIII.

1. Find the eighth term of the series 2, 6, 18.....

$$2 \times 3^7 = 2 \times 2187 = 4374$$
. Ans.

2. Find the fifth term of the series 8, 4, 2.....

$$8 \times (\frac{1}{2})^4 = 8 \times \frac{1}{16} = \frac{1}{2}$$
. Ans.

3. Find the seventh term of the series 2, 3, 4½....

$$2 \times (\frac{3}{2})^6 = 2 \times \frac{729}{64} = 22\frac{25}{32}$$
. Ans.

4. Find the sixth term of the series 4,  $2\frac{2}{3}$ ,  $1\frac{7}{5}$ .....

$$4 \times (\frac{2}{3})^5 = 4 \times \frac{89}{243} = \frac{128}{243}$$
. Ans.

5. Find the eighth term of the series 4, 10, 25.....

$$4 \times (\frac{5}{2})^7 = 4 \times \frac{75125}{128} = 2441\frac{3}{2}$$

6. Write the first three terms of the series whose fifth and sixth terms are 112 and 224, respectively.

$$r = 2$$
.  
 $\frac{112}{2^4} = 7$ . (1) Ans.  
 $2 \times 7 = 14$ . (2) Ans.  
 $2^2 \times 7 = 28$ . (3) Ans.

7. The seventh and ninth terms of a series are 100 and 144, respectively. Find the twelfth term.

The 9th term = 7th term 
$$\times r^2$$
.  
 $\therefore r^2 = \frac{144}{166}$ .  
 $\therefore r = \frac{13}{16} = \frac{6}{3}$ .  
12th term =  $144 \times (\frac{6}{3})^3$   
=  $144 \times \frac{7}{125}$   
=  $248.832$ . Ans

8. A capital of \$1000 is increased by  $\frac{1}{10}$  of itself each year. What will it be at the beginning of the fifth year?

$$$1000 \times (\frac{11}{10})^4 = $1000 \times \frac{14841}{10000}$$
  
= \$1464.10. Ans.

9. A capital of \$1000 is increased by 180 of itself each year. What will it be at the beginning of the sixth year?

$$\$1000 \times (\frac{188}{188})^{5}$$
=  $\$1000 \times \frac{18888888888}{1338.23}$ . Ans.

## EXERCISE LXXXIX.

1. Find the sum of  $2+6+18+\cdots$  to six terms.

$$s = 2 \times \frac{3^6 - 1}{3 - 1} = 2 \times \frac{728}{2} = 728$$
. Ans.

2. Find the sum of  $1+2+4+\cdots$  to nine terms.

$$s=1\times\frac{2^{9}-1}{2-1}=1\times\frac{5+1}{2}=511$$
. Ans.

3. Find the sum of  $3 + 9 + 27 + \dots$  to five terms.

$$s = 3 \times \frac{3^5 - 1}{3 - 1} = 3 \times \frac{242}{2} = 363$$
. Ans.

4. Find the sum of  $2+3+4\frac{1}{2}+\cdots$  to eight terms.

$$s = 2 \times \frac{(\frac{3}{2})^8 - 1}{\frac{3}{4} - 1} = 2 \times \frac{24\frac{161}{256}}{\frac{1}{2}} = 98\frac{38}{64}$$
. Ans.

5. Find the sum of  $1 + \frac{1}{2} + \frac{1}{3} + \cdots$  to eight terms.

$$s = 1 \times \frac{1 - (\frac{1}{3})^8}{1 - \frac{1}{3}} = \frac{1 - \frac{1}{6561}}{\frac{2}{3}} = \frac{6560}{6561} \times \frac{3}{2} = 1\frac{1098}{2187}. Ans.$$

6. Find the sum of  $1 + \frac{1}{2} + \frac{1}{4} + \cdots$  to ten terms.

$$s = 1 \times \frac{1 - (\frac{1}{2})^{10}}{1 - \frac{1}{4}} = 1 \times \frac{1 - \frac{1}{10^{24}}}{\frac{1}{4}} = 1 \times \frac{10^{24}}{10^{24}} \times 2 = 1^{\frac{6}{6}\frac{1}{4}}. Ans.$$

7. Find the sum of  $\frac{1}{2} + \frac{1}{2} + \frac{2}{3} + \cdots$  to eight terms.

$$s = \frac{1}{2} \times \frac{1 - (\frac{2}{3})^8}{1 - \frac{2}{3}} = \frac{1}{2} \times \frac{1 - \frac{256}{1561}}{\frac{1}{3}} = \frac{1}{2} \times \frac{6805}{6561} \times 3 = 1\frac{1981}{2574}. Ans.$$

8. Find the sum of the first six terms of the series whose first term is 3 and ratio 5.

$$s = 3 \times \frac{5^6 - 1}{5 - 1} = 3 \times \frac{15694}{4} = 11718$$
. Ans.

9. Find the sum of the first eight terms of the series whose first term is 3 and ratio \(\frac{1}{4}\).

$$s = 3 \times \frac{1 - (\frac{1}{3})^{6}}{1 - \frac{1}{3}} = 3 \times \frac{1 - \frac{1}{6\sqrt{1 + 1}}}{\frac{3}{3}} = 3 \times \frac{5560}{5561} \times \frac{3}{3} = 45\frac{4}{2}\frac{4}{3}. Ans.$$

10. A person saved in one year \$64, and in each succeeding year, for 9 years more, 1½ times as much as in the preceding year. Find the whole amount saved.

$$s = \$64 \times \frac{(\frac{8}{2})^{10} - 1}{\frac{8}{4} - 1} = \$64 \times \frac{56 \cdot 681}{\frac{1}{2}} = \$7253.13.$$
 Ans.

#### EXERCISE XC.

1. Find the sum of the infinite series  $\frac{1}{2} + \frac{1}{4} + \frac{1}{8} + \cdots$ 

$$s = \frac{\frac{1}{1-\frac{1}{4}}}{1-\frac{1}{4}} = \frac{\frac{1}{2}}{\frac{1}{4}} = 1$$
. Ans.

2. Find the sum of the infinite series  $\frac{2}{3} + \frac{4}{9} + \frac{8}{27} + \cdots$ 

$$s = \frac{\frac{2}{1}}{1-\frac{2}{1}} = \frac{2}{1} = 2. Ans.$$

3. Find the sum of the infinite series  $\frac{1}{4} + \frac{1}{16} + \frac{1}{64} + \cdots$ 

$$s = \frac{\frac{1}{4}}{1 - \frac{1}{4}} = \frac{\frac{1}{4}}{\frac{3}{4}} = \frac{1}{8}$$
. Ans.

4. Find the sum of the infinite series  $\frac{1}{5} + \frac{1}{125} + \frac{1}{125} + \cdots$ 

$$s = \frac{1}{1 - \frac{1}{4}} = \frac{1}{4} = \frac{1}{4}$$
. Ans.

5. Find the sum of the infinite series 0.171717.

$$s = \frac{0.17}{1 - 0.01} = \frac{0.17}{0.99} = \frac{17}{99}$$
. Ans.

6. Find the sum of the infinite series 0.212121.....

$$s = \frac{0.21}{1 - 0.01} = \frac{0.21}{0.99} = \frac{21}{99}$$
. Ans.

7. Find the sum of the infinite series 0.9999.....

$$s = \frac{0.9}{1 - 0.1} = \frac{0.9}{0.9} = 1$$
. Ans.

8. Find the sum of the infinite series 0.232323.....

$$8 = \frac{0.23}{1 - 0.01} = \frac{0.23}{0.99} = \frac{23}{99}$$
. Ans.

9. Find the sum of the infinite series 0.36848484....

$$s = \frac{0.0084}{1 - 0.01} = \frac{0.0084}{0.99} = \frac{84}{9900}.$$

$$\frac{36}{100} + \frac{84}{9900} = \frac{3648}{9900}$$
. Ans.

10. Find the sum of the infinite series 0.15272727.

$$s = \frac{0.0027}{1 - 0.01} = \frac{0.0027}{0.99} = \frac{27}{9900}.$$

$$\frac{15}{100} + \frac{27}{9900} = \frac{1512}{9900}$$
. Ans.

# EXERCISE XCI.

1. A deposits \$60 in a savings bank, and draws it out at the end of 8 yrs., with 4% compound interest. What does he receive?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log A = \log 60 + 8 \times \log 1.04.$$

$$\log 60 = 1.7782$$

$$8 \times \log 1.04 = 0.1360$$

$$1.9142 = \log 82.08$$

That is, \$82.08. Ans.

2. What will \$100 amount to in 7 years, interest at 8% per annum, compounded semi-annually?

$$\log A = \log P + n \times \log (1+r),$$
  
$$\log A = \log 100 + 14 \times \log 1.04.$$

$$\log 100 = 2.0000$$

$$14 \times \log 1.04 = 0.2380 = \log 173.$$

$$2.2380$$

That is, \$173. Ans.

3. In how many years will a sum of money double itself at 6%, compounded annually?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 2 = \log 1 + n \times \log 1.06,$$

$$\log 2 - \log 1 = n \times \log 1.06.$$

$$\frac{\log 2 - \log 1}{\log 1.06} = n.$$

$$\therefore \frac{0.3010}{0.0253} = 11.8 = n.$$

That is, 11.8 yrs. Ans.

4. In how many years will a sum of money treble itself at 6%, compounded annually?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 3 = \log 1 + n \times \log 1.06,$$

$$\log 3 - \log 1 = n \times \log 1.06,$$

$$\frac{\log 3 - \log 1}{\log 1.06} = n.$$

$$\frac{0.4771}{0.0253} = 18.9 = n.$$

That is, 18.9 yrs. Ans.

5. In how many years will \$87 amount to \$99 at 3%, compounded annually?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 99 = \log 87 + n \times \log 1.03,$$

$$\log 99 - \log 87 = n \times \log 1.03,$$

$$\frac{\log 99 - \log 87}{\log 1.03} = n.$$

$$\frac{0.0561}{0.0128} = 4.38 = n.$$

That is, 4.38 yrs. Ans.

6. In how many years will \$100 amount to \$175 at 4% compounded annually?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 175 = \log 100 + n \times \log 1.04,$$

$$\log 175 - \log 100 = n \times \log 1.04,$$

$$\frac{\log 175 - \log 100}{\log 1.04} = n.$$

$$\frac{0.2430}{0.00170} = 14.29 = n.$$
That is, 14.29 yrs. Ans.

7. At what rate per cent will a sum of money double itself in 12 years, compound interest?

$$\log A = \log P + n \times \log (1+r),$$

$$\log 2 = \log 1 + 12 \times \log (1+r),$$

$$\log 2 - \log 1 = 12 \times \log (1+r),$$

$$\frac{\log 2 - \log 1}{12} = \log (1+r).$$

$$\therefore \frac{0.3010}{12} = 0.0251 = \log (1+r).$$

$$\therefore 1.0595 = 1 + r, \text{ or } r = 0.0595.$$
That is, 5.95%. Ans.

8. At what rate will a sum of money treble itself in 15 years, at compound interest?

$$\log A = \log P + n \times \log(1+r),$$

$$\log 3 = \log 1 + 15 \times \log(1+r),$$

$$\log 3 - \log 1 = 15 \times \log(1+r),$$

$$\frac{\log 3 - \log 1}{15} = \log(1+r).$$

$$\therefore \frac{0.4771}{15} = 0.0318 = \log(1+r).$$

$$\therefore 1 + r = 1.076, \text{ or } r = 0.076.$$
That is, 7.6%. Ans.

9. At what rate will \$80 at compound interest amount to \$110 in 8 yrs.?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 110 = \log 80 + 8 \times \log (1 + r),$$

$$\log 110 - \log 80 = 8 \times \log (1 + r),$$

$$\frac{\log 110 - \log 80}{8} = \log (1 + r).$$

$$\therefore \frac{0.1383}{8} = 0.0173 = \log (1 + r).$$

$$\therefore 1 + r = 1.041, \text{ or } r = 0.041.$$
That is, 4.1%. Ans.

10. What sum must be invested at 5%, compound interest, to amount to \$1200 in 7 yrs.

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 1200 = \log P + 7 \times \log 1.05,$$

$$\log P = \log 1200 - 7 \times \log 1.05.$$

$$\log 1200 = 3.0792$$

$$7 \times \log 1.05 = 0.1484$$

$$2.9308$$

$$= \log 852.8.$$
That is, \$852.80. Ans.

11. What sum must be invested at 4%, compound interest, to amount to \$2000 in 10 yrs.? To amount to \$5000 in 8 yrs.?

$$\log A = \log P + n \times \log (1 + r),$$

$$\log 2000 = \log P + 10 \times \log 1.04,$$

$$\log P = \log 2000 - 10 \times \log 1.04.$$

$$\log 2000 = 3.3010$$

$$10 \times \log 1.04 = 0.1700$$

$$3.1310$$

$$= \log 1352.$$
That is, \$1352. (1) Ans.
$$\log A = \log P + n \times \log (1 + r),$$

$$\log 5000 = \log P + 8 \times \log 1.04,$$

$$\log P = \log 5000 - 8 \times \log 1.04.$$

$$\log 5000 = 3.6990$$

$$8 \times \log 1.04 = 0.1360$$

$$3.5630$$

$$= \log 3656.$$

That is, \$3656. (2) Ans.

12. If A puts \$100 a year into a savings bank that pays 4% per annum, compound interest, what will he have in the bank at the end of 10 years?

From § 438.

$$s = \frac{a(r^{n} - 1)}{r - 1}$$

$$s = \frac{\$100 \times 0.479}{0.04}$$

$$s = \frac{\$100 (1.04^{10} - 1)}{1.04 - 1}$$

$$s = \frac{\$47.9}{0.04}$$

$$s = \frac{\$100 (1.479 - 1)}{0.04}$$

$$s = \$1197.50. Ans.$$

13. What will be the amount in the last problem if the bank pays 41% per annum?

$$s = \frac{a(r^{n} - 1)}{r - 1} = \frac{\$100(1.045^{10} - 1)}{1.045 - 1} = \frac{\$100(1.5525 - 1)}{0.045}$$
$$= \frac{\$100 \times 0.5525}{0.045} = \frac{\$55.25}{0.045} = \$1227.78. \text{ Ans.}$$

14. What should be paid to-day for an annuity of \$500 a year, for 12 years, if money is worth 31%, compound interest?

$$s = \frac{a(r^{n} - 1)}{r - 1} = \frac{500(1.035^{12} - 1)}{0.035}$$

Present worth of s is

esent worth of 
$$\bullet$$
 is 
$$\frac{500 \times 0.509}{0.035 \times 1.035^{12}} = \log 1.035 = 0.1788$$
$$= \log 1.509.$$

$$\log 0.509 = 9.7067 - 10$$

$$colog 0.035 = 1.4559$$

$$colog 1.035 = 9.8212 - 10$$

$$3.6828$$

- log 4818,

That is, \$4818. Ans.

15. What should be paid to-day for an annuity of \$300 a year, for 10 years, if money is worth 4 %, compound interest?

$$s = \frac{300 (1.04^{10} - 1)}{0.04}.$$

Present worth of s 
$$\frac{300 \times 0.479}{0.04 \times 1.04^{10}} = \frac{10}{0.1700}$$

$$\log 300 = 2.4771$$

$$\log 0.479 = 9.6803 - 10$$

$$\operatorname{colog} 0.04 = 1.3979$$

$$\operatorname{colog} 1.04^{10} = 9.8300 - 10$$

$$3.3853$$

$$= \log 2428.$$
That is, \$2428. Ans.

16. What should be paid to-day for the assurance that 5 years hence I shall begin to receive \$500 a year, for 8 years, if money is worth 4½, compound interest?

$$s = \frac{500(1.045^8 - 1)}{0.045}$$

Present worth of s is 
$$\frac{500 \times 0.422}{0.045 \times 1.045^{13}}$$
 
$$\log 500 = 2.6990$$
 
$$\log 0.422 = 9.6253 - 10$$
 
$$\cosh 0.045 = 1.3468$$
 
$$\cosh 1.045^{13} = 9.7517 - 10$$
 
$$3.4228$$
 
$$= \log 2647.50.$$
 That is, \$2647.50. Ans.

17. If interest is reckoned at 6%, what sum of money must be paid annually, beginning a year hence, to clear off a debt of \$10,000 in 5 equal payments?

$$s = \frac{(1.06^5 - 1)}{0.06}$$
, the amount of \$1 annually deposited at 6% for 5 yrs.

Each payment must be 
$$\frac{10000 \times 1.06^{5}}{(1.06^{5} - 1)} = \frac{10000 \times 1.06^{5} \times 0.06}{0.338}.$$

$$\begin{array}{c} \log 10000 = 4.0000 & \log 1.06 = 0.0253 \\ \log 1.06^5 = 0.1265 & 5 \\ \log 0.06 = 8.7782 - 10 & 0.1265 = \log 1.338. \\ \hline 3.3758 = \log 2376. & \text{That is, $2376. Ans.} \end{array}$$

18. If interest is reckoned at 6%, what is the amount of each of 12 equal semi-annual payments, the first to be paid 6 months hence, required to clear off a debt of \$24,000?

$$s = \frac{(1.03^{12} - 1)}{0.03}$$
, the amount of \$1 annually deposited at 3% for 12 yrs.

Each payment must be 
$$\frac{24000 \times 1.03^{12}}{\frac{(1.03^{12} - 1)}{0.03}} = \frac{24000 \times 1.03^{12} \times 0.03}{0.424}$$

$$\log 24000 = 4.3802 \qquad \log 1.03 = 0.0128$$

$$\log 1.03^{12} = 0.1536 \qquad 12$$

$$\log 0.03 = 8.4771 - 10$$

$$\operatorname{colog} 0.424 = 0.3726$$

$$3.3835 = \log 2418. \qquad \text{That is, $2418. Ans.}$$

#### MISCELLANEOUS PROBLEMS.

with the digits 1, 2, 3, and find their sum.

2. Make six different numbers with the digits 2, 3, 5, and find,

1. Make six different numbers by logarithms, their continued product.

$$235 \times 253 \times 325$$
  
 $\times 352 \times 523 \times 532$ .  
 $\log 235 = 2.3711$   
 $\log 253 = 2.0431$   
 $\log 325 = 2.5119$   
 $\log 352 = 2.5465$   
 $\log 523 = 2.7185$   
 $\log 532 = 2.7259$   
 $15.2770$   
 $\log 1,892,000,000,000,000$ 

3. Make six different numbers with the digits 8, 7, 3, and find, by logarithms, their continued product.

$$873 \times 837 \times 783$$
  
 $\times 738 \times 387 \times 378.$   
 $\log 873 = 2.9410$   
 $\log 837 = 2.9227$   
 $\log 783 = 2.8938$   
 $\log 738 = 2.8681$   
 $\log 387 = 2.5877$   
 $\log 378 = 2.5775$   
 $16.7908$ 

- $-\log 61,770,000,000,000,000$ .
- 4. Find, by logarithms, the missing term in each of the following proportions:

(1)
$$7.13:3.57::4.18:?$$

$$\frac{3.57 \times 4.18}{7.13} = ?$$

$$\log 3.57 = 0.5527$$

$$\log 4.18 = 0.6212$$

$$\cosh 7.13 = 9.1469 - 10$$

$$0.3208$$

$$= \log 2.093. Ans.$$

$$(2)$$

$$5.89 : 76.3 : : ? : 38.7.$$

$$\frac{5.89 \times 38.7}{76.3} = ?$$

$$\log 5.89 = 0.7701$$

$$\log 38.7 = 1.5877$$

$$\operatorname{colog} 76.3 = 8.1175 - 10$$

$$0.4753$$

$$= \log 2.987. \quad Ans.$$

$$(3)$$

$$7.37 : ? : : 86.1 : 43.7.$$

$$\frac{7.37 \times 43.7}{86.1} = ?$$

$$\log 43.7 = 1.6405$$

$$\operatorname{colog} 86.1 = 8.0650 - 10$$

$$0.5730$$

$$= \log 3.741. \quad Ans.$$

$$(4)$$

$$? : 69.7 : : 3.79 : 29.4.$$

$$\frac{69.7 \times 3.79}{29.4} = ?$$

$$\log 69.7 = 1.8432$$

$$\log 3.79 = 0.5786$$

$$\operatorname{colog} 29.4 = 8.5317 - 10$$

$$0.9535$$

$$= \log 8.984. \quad Ans.$$

5. Find, by logarithms, the values of  $0.08^{\frac{1}{3}}$ ;  $2734^{\frac{1}{3}}$ ;  $21.97^{\frac{1}{3}}$ ;  $7^{3.6}$ .  $\frac{1}{3} \log 0.08 = \frac{1}{3} \text{ of } (8.9031 - 10) = 9.6344 - 10 = \log 0.4309$ .  $\frac{1}{3} \log 2734 = \frac{1}{3} \text{ of } 3.4368 = 1.1456 = \log 13.98$ .  $\frac{1}{3} \log 21.97 = \frac{1}{3} \text{ of } 1.3418 = 0.4473 = \log 2.801$ .  $\frac{1}{3} \log 7 = 3.6 \times 0.8451 = 3.0424 = \log 1103$ . 6. Find, by logarithms, the values of  $9.71^{\frac{7}{3}}$ ;  $7.935^{\frac{5}{7}}$ .

$$\frac{7}{8}\log 9.71 = \frac{7}{8} \times 0.9872 = 2.3035 = \log 201.1.$$
 (1) Ans.

$$\frac{1}{7} \log 7.935 = \frac{1}{7} \times 0.8996 = 0.6426 = \log 4.391$$
. (2) Ans.

7. What is the horizontal distance between two points, when the air-line distance is 1534 ft., and the difference of level 34 ft.?

$$\sqrt{1534^2-34^2} = \sqrt{2352000} = 1533.623$$
 ft. Ans.

8. Find the horizontal distance when the road distance is 1 mile, and the rise 347 ft.

$$\sqrt{(5280+347)(5280-347)} = \sqrt{27757991} = 5268.585$$
 ft. Ans.

9. If the road distance is half a mile, and the horizontal distance 2513 ft., find the difference of level.

$$\sqrt{(2640 + 2513)(2640 - 2513)} = \sqrt{654431} = 808.97$$
 ft. Ans.

10. The diagonal of a rectangular floor is 34.6 ft., and the width is 17.8 ft. Find the length of the floor.

$$\sqrt{(34.6+17.8)(34.6-17.8)} = \sqrt{880.32} = 29.67$$
 ft. Ans.

11. The height of a tower on a river's bank is 55 ft., the length of a line from the top to the opposite bank is 78 ft. Find the breadth of the river.

$$\sqrt{(78+55)(78-55)} = \sqrt{3059} = 55.31$$
 ft. Ans.

12. The number of seamen at Portsmouth is 800, at Charlestown 404, and at Brooklyn 756. A ship is commissioned whose complement is 490 seamen. Determine the number to be drafted from each place in order to obtain a proportionate number from each.

800 + 404 + 756 = 1960. 
$$\frac{404}{1960} \times \frac{490}{1} = 101$$
, C.  $\frac{800}{1960} \times \frac{490}{1} = 200$ , P.  $\frac{756}{1960} \times \frac{490}{1} = 189$ , B.

13. Show, without division, that 36,432 contains 8, 9, 11 as factors  $432 = 54 \times 8$ .

$$3+6+4+3+2=18$$
.  
 $3+4+2=6+3$ . (See § 222.)

14. Find the smallest multiplier that will make 47,250 a perfect cube.

$$47,250 = 2 \times 3^{3} \times 5^{3} \times 7.$$
  
 $2^{3} \times 7^{2} = 4 \times 49 = 196.$  Ans.

15. Find the proper fraction which, when reduced to a continued fraction, has for quotients, 1, 3, 5, 7, 2, 4.

$$\frac{1}{1+\frac{1}{3+\frac{1}{5+\frac{1}{7+\frac{1}{2+\frac{1}{4}}}}} = \frac{1099}{1443}. Ans.$$

16. If the meter is equal to 1.09362 yds., find a series of four fractions that will express more and more nearly the true ratio of the meter to the yard.

$$1.09362 = 1\frac{33882}{1000000} = 1\frac{4681}{500000}.$$

$$4681)500000(10$$

$$\frac{46810}{3190)4681(1)}$$

$$\frac{3190}{1491)3190(2)}$$

$$\frac{2982}{208)1491(7)}$$

$$\frac{1456}{35}$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{11}{10}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{12}{11}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{35}{32}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{35}{32}.$$

$$\frac{11}{10}, \frac{12}{11}, \frac{35}{32}, \frac{257}{235}.$$
Ans.

17. Find the square factors contained in 33,075.

$$33075 = 3^{3} \times 5^{2} \times 7^{2}$$
.  $3^{2} \times 5^{2} = 225$ ,  $3^{2} \times 7^{2} = 441$ ,  $5^{2} = 25$ ,  $5^{2} \times 7^{2} = 1225$ ,  $7^{2} = 49$ .  $3^{2} \times 5^{2} \times 7^{2} = 11025$ .

9, 25, 49, 225, 441, 1225, 11,025.

18. The top of St. Peter's, Rome, is  $\frac{1}{10}$  of a mile above the ground, and that of St. Paul's, London, is  $\frac{17}{264}$  of a mile. By how many feet does the height of St. Peter's exceed that of St. Paul's?

$$\frac{9}{119}$$
 of  $\frac{48}{5289} = 432$  ft.  $\frac{17}{264}$  of  $\frac{20}{5289} = 340$  ft.  $\frac{432}{1}$  ft.  $\frac{340}{1}$  ft.  $\frac{17}{264}$  of  $\frac{17}{1}$  ft.  $\frac{17}{11}$  ft.  $\frac{17}{$ 

19. How many days elapsed between the annular eclipse of May 15, 1836, and that of March 15, 1858?

$$365 \times 21 = 7665$$
.  $7665 + 304 + 5 = 7274$  days. Ans.

20. In a gale, a flag-staff 60 ft. high snaps 28.8 ft. from the bottom; and, not being wholly broken off, the top touches the ground. If the ground is level, how far is the top from the bottom?

The distance = 
$$\sqrt{(31.2 + 28.8)(31.2 - 28.8)} = \sqrt{60 \times 2.4}$$
  
=  $\sqrt{144} = 12$  ft. Ans.

21. Seventeen trees are standing in a line, 20 yds. apart from each other; a person walks from the first to the second and back, then to the third and back, and so on to the end. How far does he walk?

The total distance is the sum of an arithmetical series in which

$$n = 16$$
,  $d = 40$ ,  $a = 40$ .

$$l = a + (n - 1)d = 40 + 15 \times 40 = 640.$$

$$s = \frac{n}{2} (a + l) = \frac{16}{2} \times (40 + 640) = 5440 \text{ yds.} = 3 \text{ mi. } 160 \text{ yds.}$$
 Ans

22. A level reach in a canal is 14\frac{3}{4} mi. long and 4\frac{9}{6} ft. broad. At one end is a lock 80 ft. long, 12 ft. broad, and with a fall of 8 ft. 6 in. How many barges can pass through the lock before the water in the canal is lowered 1 in.?

The amount of water that can be drained off in lowering the level 1 in. is  $14\frac{3}{4} \times 5280 \times 48 \times \frac{1}{12} = 311,520$  cu. ft. The amount of water wasted each time a barge goes through the lock is  $80 \times 12 \times 8\frac{1}{2} = 8160$  cu. ft. Hence,

$$311,520 + 8160 = 38$$
 barges. Ans.

23. Find the capacity, in liters and in bushels, of a box 1.7<sup>m</sup> long, 87<sup>cm</sup> wide, and 31<sup>cm</sup> deep.

$$1.7^{m} = 170^{cm}$$
.  
 $1^{1} = 0.908 \text{ qt.}$   
 $170 \times 87 \times 31 = 458,490^{ccm} = 458.49^{1}$ . (1) Ans.  
 $458.49 \times 0.908 = 416.309 \text{ qts.}$   
 $1 \text{ bu.} = 32 \text{ qts.}$   
 $416.309 + 32 = 13 \text{ bu.}$  (2) Ans.

24. Find the number of kilograms of olive oil, specific gravity 0.915, to fill a vessel 2.3<sup>m</sup> long, 1.8<sup>m</sup> wide, and 74<sup>cm</sup> deep.

$$74^{\text{cm}} = 0.74^{\text{m}}$$
.  
 $2.3 \times 1.8 \times 0.74 = 3.0636^{\text{cbm}} = 3063.6^{\text{kg}}$ .  
 $3063.6^{\text{kg}} \times 0.915 = 2803.194^{\text{kg}}$ . Ans.

25. How many tons in a block of marble 4 ft. long, 34 in. wide, 17.3 in. thick, if its specific gravity is 2.73?

$$4 ext{ ft.} = 48 ext{ in.}$$
 $48 imes 34 imes 17.3 = 28233.6 ext{ cu. in.}$ 
 $28233.6 \div 1728 = 16.34 ext{ cu. ft.}$ 
 $16.34 imes 62\frac{1}{2} ext{ lbs.} = 1021.25 ext{ lbs.}$ 
 $1021.25 ext{ lbs.} imes 2.73 = 2788.0125 ext{ lbs.} = 1.394 ext{ t. } ext{ Ans.}$ 

26. Find the surface of a sphere 18.3 in. in diameter.

The radius = 9.15 in.  

$$9.15 \times 9.15 \times 3.1416 = 263.0226$$
 sq. in.  
 $263.0226 \times 4 = 1052.09$  sq. in. Ans.

27. Find the number of acres in a circular field 213 yds. 2 ft.

213 yds. 2 ft. = 641 ft. in diameter.  
The radius is 320.5 ft.  
1 A. = 43560 sq. ft.  
Area = 
$$\frac{3.1416 \times 320.5^2}{43560}$$
  
 $\log 3.1416 = 0.4971$   
 $\log 320.5^2 = 5.0116$   
 $\operatorname{colog} 43560 = 5.3609 - 10$   
 $0.8696 = \log 7.407$ .  
7.407 A. Ans.

28. How many cubic inches in a 10-inch globe? in a 20-inch globe? What is the ratio of their volumes?

The ratio of their volumes is  $10^8 : 20^8 = 1^8 \cdot 2^8 = 1 : 8$ . Ans.  $10^8 \times 0.5236 = 523.6$  cu in. (1). Ans.  $523.6 \times 8 = 4188.8$  cu. in. (2). Ans.

29. How many balls 3 in. in diameter can be cast from a pig of iron 7 ft. long, 6.7 in. wide, 3.8 in. thick, if the waste in melting and casting is reckoned at 31%?

$$7 \text{ ft.} = 84 \text{ in.}$$
No. of balls =  $\frac{84 \times 6.7 \times 3.8 \times 0.9675}{3^3 \times 5236}$ 

$$\log \quad 84 = 1.9243$$

$$\log \quad 6.7 = 0.8261$$

$$\log \quad 3.8 = 0.5798$$

$$\log 0.9675 = 9.9857 - 10$$

$$\cosh \quad 3^3 = 8.5686 - 10$$

$$\cosh \quad 0.5236 = 0.2810$$

$$2.1655 = \log 146.4$$

Hence, number of balls is 146. Ans.

30. Find the difference in length, at 80° F., of a glass and a steel rod, each 3 ft. long at freezing point, if the expansion at 100° C. is 0.00085 for glass and 0.0012 for steel.

$$80^{\circ} \text{ F} = \frac{5}{9} (80^{\circ} - 32^{\circ}) \text{ C.} = 26\frac{2}{9}^{\circ} \text{ C.}$$
  
Difference in length at  $100^{\circ} \text{ C.}$  is  $0.0012 - 0.00085 = 0.00035$ .  
 $3 \text{ ft.} = 36 \text{ in.}$   
 $0.00035 \times 36 \times 0.26\frac{2}{3} = 0.00366 \text{ in.}$  Ans.

31. A grain of gold is beaten out in leaf to cover 56 sq. in. What weight will be required for gilding the faces of a cube whose edge is 3½ ft.?

$$6 \times 3\frac{1}{2} \times 3\frac{1}{2} = 73\frac{1}{2}$$
 sq. ft.  
 $144 \times 73\frac{1}{2}$  sq. ft. = 10584 sq. in.  
 $10584 + 56 = 189$  grs. = 7 dwt. 21 grs. Ans.

32. What premium must be paid, at the rate of 17%, for insuring a vessel worth \$117,750, in order that in the event of loss the owner may receive both the value of the ship and the premium?

$$1 - 0.01875 = 0.98125$$
.  
 $$117,750 + 0.98125 = $120,000$ .  
 $$120,000 - 117,750 = $2250$ . Ans.

33. By selling goods at 60 cts. a pound, 8% on the cost is lost; what advance must be made in the price in order to gain 15% on the cost?

If the selling price is 92, and we wish it to be 115, we must add 23, or \(\frac{1}{4}\) of 92. That is, we must add \(\frac{1}{4}\) of 60 cts. = 15 cts. a pound. Ans.

34. Divide \$27.12½ among three persons, giving the second \$5 less than the first, and twice as much as the third.

Let a represent the amount given to the first.

a-5 will represent the amount given to the second.

 $\frac{a}{2} - \frac{5}{2}$  will represent the amount given to the third.

Then,  $2\frac{1}{2}a - 7\frac{1}{2}$  will represent the amount given to all three.

But \$27.121 is the amount given to all three.

Hence,  $2\frac{1}{2}a - 7\frac{1}{2} = 27.12\frac{1}{2}$ .

Add to each side  $7\frac{1}{2}$ ,  $2\frac{1}{2}a = 34.625$ 

Divide each side by  $2\frac{1}{2}$ , a = 13.85

a-5=8.85

 $\frac{1}{2}(a-5) = 4.42\frac{1}{2}$ 

Hence, 1st gets \$13.85; 2d, \$8.85; 3d, \$4.42\. Ans.

35. The population of a city in 1880 was 12,298, showing a decrease of  $8\frac{1}{3}\%$  on its population in 1870; in 1870 there was an increase of  $7\frac{1}{3}\%$  on the census of 1860. What was its population in 1860?

 $12,298 + 0.91\frac{2}{3} = 13,416$ , population in 1870. 13,416 + 1.075 = 12,480, population in 1860. Ans.

36. Find the increase of income obtained by transferring \$2500 from 3% stocks at 94½ to 4% stocks at 105.

0.03 of \$2500 = \$75, income from the 3% stock.

 $0.94\frac{1}{2}$  of \$2500 = \$2362.50, amount from the 3% stock.

\$1.05 is paid for \$1 worth of 4% stock.

Hence, \$2362.50 is paid for 2362.50 + 1.05 = \$2250 stock.

0.04 of \$2250 = \$90, income from 4% stock.

\$90 - \$75 = \$15, increase of income. Ans.

37. Each person breathing in a closed room spoils the air at the rate of about 8 cu. ft. a minute. A congregation of 400 persons enter a closed room 70 ft. by 40 ft. and 20 ft. high. How long will it take them to spoil the air?

The air in the room will last one person  $\frac{70 \times 40 \times 20}{8}$  min., or 400 persons,

$$\frac{\frac{7}{79 \times 49 \times 29}}{\underset{2}{8 \times 499}} = \frac{35}{2} = 17\frac{1}{2} \text{ min. Ans.}$$

38. How long can the windows and doors of a school-room be safely kept closed when occupied by 50 children, if the room is 25 ft. by 20 ft. and 10 ft. high?

The air in the room will last one person  $\frac{25 \times 20 \times 10}{8}$  min., or

50 persons,

$$\frac{25 \times 29 \times 19}{3 \times 59} = \frac{25}{2} = 12\frac{1}{2} \text{ min. Ans.}$$

39. Find the square root to four decimal places, of the reciprocal of 0.0043.

$$\frac{1}{2}$$
 colog  $0.0043 = 1.1833 = \log 15.25$ . Ans.

40. A pays B \$230 as the present value of \$300 due in 5 yrs. Which gains by the payment, and how much, if interest is reckoned at 5%?

The present worth of \$300 due in 5 yrs. is  $\frac{100}{127.63}$  of \$300

- = \$235.05. Hence, A gains \$5.05 by the transaction.
- 41. Find the quantity of coal required by a steamer for a voyage o. 4043 mi., if her rate per hour is 14.04 knots, and her consumption of coal 87 t. per day.

$$14.04 \times 6086 \times 24 = 2,050,738.56$$
 ft. per day.  
 $4043 \times 5280 = 21,347,040$  ft. '  
 $21,347,040 + 2,050,738.56 = 10.40944$  days.  
 $10.40944 \times 87$  t. = 905 t. 1392 lbs. Ans.

42. Find the area of a circular ring of which the inner and outer diameters are 7.36 and 10.64 in.

Area = 
$$0.7854(10.64^2 - 7.36^2)$$
  
=  $0.7854(113.2096 - 54.1696)$   
=  $0.7854 \times 59.04$   
=  $46.37$  sq. in. Ans.

43. A and B can do a piece of work in 13\frac{1}{3} dys., A and C in 10\frac{3}{2} dys., A, B, and C in 7\frac{1}{2} dys. In how many days can A do it alone?

In 1 day A and B can do  $\frac{3}{40}$  of the work. In 1 day A and C can do  $\frac{3}{82}$  of the work. In 1 day A, B, and C can do  $\frac{2}{15}$  of the work. .: in 1 day B can do  $\frac{2}{15} - \frac{3}{32}$  of the work. And in 1 day C can do  $\frac{2}{15} - \frac{3}{40}$  of the work. And in 1 day A can do  $\frac{3}{40} - (\frac{2}{15} - \frac{3}{32})$  of the work.  $\frac{3}{40} - (\frac{2}{15} - \frac{3}{32}) = \frac{3}{40} - \frac{2}{15} + \frac{3}{32} = \frac{36 - 64 + 45}{480} = \frac{17}{480}$ .: it will take A  $\frac{430}{17} = 28\frac{4}{17}$  dys. Ans.

44. If 3 men working 11 hrs. a day can reap 20 A. in 11 dys., how many men working 12 hrs. a day can reap a field 360 yds. long and 320 yds. broad in 4 dys.?

$$360 \text{ yds.} \times 320 \text{ yds.} = 115,200 \text{ sq. yds.}$$
  
 $115,200 + 30\frac{1}{4} + 160 = \frac{2880}{121} \text{ A.}$ 

- 45. Find the area of a triangle whose sides are 12, 5, and 13 in.
  - Observe that  $13^2 = 12^2 + 5^2$ . Hence the triangle is a right triangle. Area =  $\frac{1}{2}$  of  $12 \times 5 = 30$  sq. in. Ans.
- 46. Find the area of a triangle whose sides are 73, 57, and 48 ft.

$$\frac{53 + 57 + 48}{2} = 89.$$
Area =  $\sqrt{89 \times 16 \times 32 \times 41}$ .
$$\log 89 = 1.9494$$

$$\log 16 = 1.2041$$

$$\log 32 = 1.5051$$

$$\log 41 = 1.6128$$

$$2)6.2714$$

$$3.1357 = \log 1367$$

$$1367 \text{ sq. ft. } Ans.$$

47. Find the number of hektars in a triangular field whose sides are 37.5<sup>m</sup>, 91.7<sup>m</sup>, and 78.9<sup>m</sup>.

$$\frac{37.5 + 91.7 + 78.9}{2} = 104.05.$$

$$\text{Area} = \sqrt{104.05 \times 66.55 \times 12.35 \times 25.15}.$$

$$\log 104.05 = 2.0172$$

$$\log 66.55 = 1.8232$$

$$\log 12.35 = 1.0917$$

$$\log 25.15 = 1.4006$$

$$\frac{2)6.3327}{3.1663} = \log 1467.$$

$$1467^{\text{qm}} = 0.1467^{\text{ha}}, Ans.$$

48. Find the number of hektars in a triangular field whose sides are 67.5<sup>m</sup>, 81.2<sup>m</sup>, and 102.7<sup>m</sup>.

$$\frac{67.5 + 81.2 + 102.7}{2} = 125.7.$$

$$Area = \sqrt{125.7 \times 58.2 \times 44.5 \times 23}$$

$$\log 125.7 = 2.0994$$

$$\log 58.2 = 1.7649$$

$$\log 44.5 = 1.6484$$

$$\log 23 = 1.3617$$

$$2)6.8744$$

$$3.4372 = \log 2736.$$

$$2736qm = 0.2736hs. Ans.$$

49. Find the number of acres in a triangular field whose sides are 227, 342, and 416 ft.

$$1 A. = 43,560 \text{ sq. ft.}$$

$$\frac{227 + 342 + 416}{2} = 492.5.$$

$$\text{Area} = \frac{\sqrt{492.5 \times 265.5 \times 150.5 \times 76.5}}{43560} A.$$

50. Find the number of acres in a triangular field whose sides are 79 chains 8 links, 57 chains 3 links, and 102 chains 19 links.

$$\frac{79.08 + 57.03 + 102.19}{2} = 119.15.$$

$$Area = \frac{\sqrt{119.15 \times 40.07 \times 62.12 \times 16.96}}{10}$$

$$\log 119.15 = 2.0761$$

$$\log 40.07 = 1.6028$$

$$\log 62.12 = 1.7932$$

$$\log 16.96 = 1.2294$$

$$2)6.7015$$

$$3.3508$$

$$\operatorname{colog} 10 = 90000 = 10$$

$$2.3508 = \log 224.3.$$

$$224.3 \text{ A. Ans.}$$

51. Find the number of square rods in a triangle whose sides are rds. 2 yds., 6 rds. 5 yds., and 9 rds. 41 ft.

7 rds. 2 yds. = 121.5 ft.  
6 rds. 5 yds. = 114 ft.  
9 rds. 
$$4\frac{1}{2}$$
 ft. = 153 ft.  
1 rd. = 272.25 sq. ft.  

$$\frac{121.5 + 114 + 153}{2} = 194.25.$$
Area =  $\sqrt{194.25 \times 72.75 \times 80.25 \times 41.25}$ 

$$\log 194.25 = 2.2884$$

$$\log 72.75 = 1.8618$$

$$\log 80.25 = 1.9043$$

$$\log 41.25 = \frac{1.6155}{2)7.6700}$$

$$3.8350$$

$$\cosh 272.25 = \frac{7.5650 - 10}{1.4000 - \log 25.12}$$
25.12 sq. rds. Ans.

52. Find the number of acres in a four-sided field, the sides of which are in order 361, 561, 443, and 357 ft.; and the distance from the beginning of the first side to the end of the second side is 682 ft.

$$\frac{361 + 561 + 682}{2} = 802.$$

$$Area = \frac{\sqrt{802 \times 441 \times 241 \times 120}}{43560} A.$$

$$\log 802 = 2.9042$$

$$\log 441 = 2.6444$$

$$\log 241 = 2.3820$$

$$\log 120 = 2.0792$$

$$2)10.0098$$

$$\overline{5.0049}$$

$$\cosh 43560 = \frac{5.3609}{0.3658} = \log 2.322.$$

$$\frac{357 + 443 + 682}{2} = 741.$$

$$Area = \frac{\sqrt{741 \times 384 \times 298 \times 59}}{43560}$$

$$\log 741 = 2.8698$$

$$\log 384 = 2.5843$$

$$\log 298 = 2.4742$$

$$\log 59 = \frac{1.7709}{2.99.6992}$$

$$\frac{2)9.6992}{4.8496}$$

$$\cosh 43560 = \frac{5.3609}{0.2105} = 1.624$$

$$1.624 + 2.322 = 3.946 A. Ans.$$

53. Find the number of hektars in a field of three sides, one of which is 82.1<sup>m</sup>, and the distance from this side to the opposite corner is 47.3<sup>m</sup>.

$$\frac{1}{2}(82.1 \times 47.3) = 1941.67^{qm} = 0.194167^{ha}$$
. Ans.

54. Find the number of acres in a triangular lot, one side of which is 343.6 ft., and the distance from this side to the opposite corner is 163.2 ft.

$$\frac{1}{2}(343.6 \times 163.2) = 28037.76 \text{ sq. ft.}$$
  
 $28037.76 + 43560 = 0.6436 \text{ A.}$  Ans.

55. Find the altitude of a triangle, if each side is 1000 ft.

$$\frac{1000 + 1000 + 1000}{2} = 1500.$$

$$Area = \sqrt{1500 \times 500 \times 500 \times 500}$$

$$= 250000\sqrt{3} = 433012.5 \text{ sq. ft.}$$

$$433012.5 + 500 = 866.025 \text{ ft. } Ans.$$

56. Find the distances of the vertices from the opposite sides of a triangle, when these sides are 17.8mm, 23.6mm, and 31.5mm.

$$\frac{17.8 + 23.6 + 31.5}{2} = 36.45.$$

$$Area = \sqrt{36.45 \times 18.65 \times 12.85 \times 4.95}.$$

57. If the four sides of a field measured in succession are 237, 253, 244, and 261 ft., and the diagonal measured from the end of the first side to the end of the third side is 351 ft.; find its area.

$$\frac{237 + 261 + 351}{2} = 424.5.$$

Area of triangle =  $\sqrt{424.5 \times 187.5 \times 163.5 \times 73.5}$ .

Area of triangle

$$= \sqrt{424 \times 171 \times 180 \times 73}.$$

58. If the four sides of a field are 237, 253, 244, and 261 ft., taken in order, and if the corner formed by the second and third sides is a square corner; find the diagonal from the beginning of the second side to the end of the third side, and also find the area of the field.

$$Diagonal = \sqrt{253^2 + 244^2} = \sqrt{123545} = 351.489.$$

The area is the same as in the last problem.

59. Find the area of a circle that has a radius of 10 in.; of a circle that has a diameter of 10 ft.; of a circle that has a circumference of 30 in.

Area = 
$$\pi R^2$$
 = 3.1416 × 100 = 314.16 sq. in. (1) Ans.  
Area =  $\pi R^2$  = 3.1416 × 25 = 78.54 sq. ft. (2) Ans.  
Circumference =  $2\pi R$ .  
 $30 = 2\pi R$ .  
 $R = \frac{15}{\pi}$ .  
Area =  $\pi R^2 = \frac{\pi}{1} \times \frac{225}{\pi^2} = \frac{225}{3.1416} = 71.62$  sq. in. (3) Ans.

60. A horse is tied by a rope 28.8<sup>m</sup> long; what part of a hektar can he graze?

Area = 
$$\pi R^2$$
 = 3.1416 × 27.8<sup>2</sup> = 3.1416 × 772.84  
= 2427.95qm = 0.2428ha. Ans.

61. How many square feet in a circle that has a diameter of 17‡ yds.?

17% yds. = 53 ft.  
Area = 
$$\pi R^2$$
 = 3.1416 × 26.5°.  
log 26.5° = 3.8464  
log 3.1416 = 0.4971  
3.3435 = log 2205.5  
2205.5 sq. ft. Ans.

62. How many square feet in a circle that has a circumference of 117 yds.?

117 yds. = 351 ft. 
$$\log 351^2 = 5.0906$$
  
Circumference =  $2\pi R$ .  $\operatorname{colog} 3.1416 = 9.5029 - 10$   
 $351 = 2\pi R$ .  $\operatorname{colog} 4 = 9.3979 - 10$   
 $R = \frac{351}{2\pi}$ .  $3.9914$   
 $= \log 9804$ .  $= \log 9804$ .  $= \log 9804$ .  $= \log 9804$  sq. ft. Ans.

63. How many square inches in the surface of a globe that has a radius of 12.37 in.?

Area = 
$$4 \pi R^2$$
  
=  $4 \pi \times 12.37^2$ .  
 $\log 4 = 0.6021$   
 $\log 3.1416 = 0.4971$   
 $\log 12.37^2 = 2.1848$   
 $3.2840 = \log 1923$ .  
1923 sq. in. Ans.

64. Find the area of the surface of the largest globe that can

be turned out from a joist 4 in. by 6 in.

Area = 
$$4\pi 2^2 = 16\pi$$
  
=  $16 \times 3.1416$   
=  $50.266$  sq. in. Ans.

65. How many cubic inches in a globe that has a diameter of 10 in.?

Volume = 
$$0.5236 \times \text{diam.}^3$$
  
=  $0.5236 \times 1000$   
=  $523.6 \text{ sq. in. } Ans.$ 

66. If a tree be round, and the girt is 17 ft. 6 in., find its diameter. Find the area of a cross-section, and find the number of cubic feet in the largest sphere that can be cut from it.

Diameter = 
$$\frac{17.5}{3.1416}$$
  
= 5.57 ft. (1) Ans.  
Area =  $\pi R^2$ .  
 $\log 3.1416 = 0.4971$   
 $\log 5.57^2 = 1.4918$   
 $\operatorname{colog} 2^2 = 9.3979 - 10$   
 $\log \operatorname{Area} = 1.3868 = \log 24.37$ .  
 $24.37 \operatorname{sq.} \operatorname{ft.} (2) \operatorname{Ans.}$   
Volume =  $0.5236 \times \operatorname{diam.}^3$   
 $\log 0.5236 = 9.7190 - 10$   
 $\log 5.57^3 = 2.2377$   
 $1.9567 = \log 90.52$ .  
90.52 cu. ft. (3) Ans.

67. Find the weight in kilograms and in pounds of an iron ball 21.5cm in diameter, specific gravity 7.47; of a tin ball 13cm in diameter, specific gravity 7.29; of a lead ball 17.3cm in diameter, specific gravity 11.35; of a silver ball 1.31cm in diameter, specific gravity 10.47.

Iron.  

$$V = 0.5236 \times 21.5^{3}$$
  
 $\log 0.5236 = 9.7190 - 10$   
 $\log 21.5^{3} = 3.9972$   
 $\log 7.47 = 0.8733$   
 $\operatorname{colog} 1000 = 7.0000 - 10$   
 $1.5895 = \log 38.86$ .  
 $38.86^{kg}$ . (1) Ans.  
 $\log 2.205 = 0.3434$   
 $\log 38.86 = 1.5895$   
 $1.9329 = \log 85.68$ .  
 $85.68 \text{ lbs.}$  (2) Ans.

## Lead.

$$\log 17.3^{8} = 3.7140 
\log 0.5236 = 9.7190 - 10 
\log 11.35 = 1.0550 
\operatorname{colog} 1000 = 7.0000 - 10 
1.4880 = \log 30.76.$$

$$30.76^{kg}. (1) Ans.$$

$$\log 2.205 = 0.3434 
\log 30.76 = 1.4880 
1.8314 = \log 67.83.$$

## Tin.

67.83 lbs. (2) Ans.

$$V = 0.5236 \times 13^8$$
.  
 $\log 0.5236 = 9.7190 - 10$   
 $\log 13^8 = 3.3417$   
 $\log 7.29 = 0.8627$   
 $\cosh 1000 = 7.0000 - 10$   
 $0.9234 = \log 8.383$ .  
 $8.383^{\text{kg}}$ . (1) Ans.

$$\begin{array}{c} \log & 2.205 = 0.3434 \\ \log & 8.383 = 0.9234 \\ \hline & 1.2668 = \log 18.48, \\ 18.48 \text{ lbs. (2) } \textit{Ans.} \end{array}$$

## Silver.

$$\log 1.31^{8} = 0.3519$$

$$\log 0.5236 = 9.7190 - 10$$

$$\log 10.47 = 1.0199$$

$$\operatorname{colog} 1000 = \frac{7.0000 - 10}{8.0908 - 10}$$

$$= \log 0.01233.$$

$$0.01233^{kg}. (1) Ans.$$

$$\log 2.205 = 0.3434$$

$$\log 0.01233 = \frac{8.0908 - 10}{8.4342 - 10}$$

$$= \log 0.02717.$$

0.02717 lbs. (2) Ans.

68. A slab of cast-iron 4 ft. 2½ in. long, 17 in. wide, and 8½ in. thick, specific gravity 7.31, is cast into 2-lb. balls. If there is a loss of 5% in melting, how many balls are obtained, and what is the diameter of each?

The slab will make 
$$\frac{50.5 \times 17 \times 25 \times 0.95 \times 62.5 \times 7.31}{2 \times 3 \times 1728}$$
 balls.

log  $50.5 = 1.7033$ 
log  $17 = 1.2304$ 
log  $25 = 1.3979$ 
log  $0.95 = 9.9777 - 10$ 
log  $62.5 = 1.7959$ 
log  $7.31 = 0.8639$ 
colog  $2 = 9.6990 - 10$ 
colog  $3 = 9.5229 - 10$ 
colog  $1728 = 6.7625 - 10$ 
 $2.9535 = \log 898$ .

898 balls. (1) Ans.

1 The diameter will be

 $\frac{50.5 \times 17 \times 25 \times 0.95}{0.5236 \times 3 \times 898}$ 
log  $50.5 = 1.7033$ 
log  $17 = 1.2304$ 
log  $25 = 1.3979$ 
log  $0.95 = 9.9777 - 10$ 
colog  $0.95$ 

69. How many pounds avoirdupois would a ball of such iron 30 in. in diameter weigh?

log 
$$30^{8} = 4.4313$$
  
log  $0.5236 = 9.7190 - 10$   
log  $62.5 = 1.7959$   
log  $7.31 = 0.8639$   
colog  $1728 = 6.7625 - 10$   
 $3.5726 = \log 3732.5$ ,  
 $3732.5$  lbs. Ans.

70. If the specific gravity of ice is 0.921, find the weight and the surface of each of three spheres of ice whose diameters are 1<sup>cm</sup>, 10<sup>cm</sup>, and 1<sup>m</sup>. Which of these spheres would roll first on a plain, in a gradually-increasing wind?

$$V=1^8 \times 0.5236 = 0.5236^{\text{corm}}$$
.  
 $0.5236^{\text{corm}} = 523.6^{\text{mg}}$ .  
 $0.921 \times 523.6^{\text{mg}} = 482.24^{\text{mg}}$ . (1) Ans.  
 $V=10^3 \times 0.5236 = 523.6^{\text{corm}}$ .  
 $523.6^{\text{corm}} = 523.6^{\text{g}}$ .  
 $0.921 \times 523.6^{\text{g}} = 482.24^{\text{g}}$ . (2) Ans.  
 $V=1^8 \times 0.5236 = 0.5236^{\text{cbm}}$ .  
 $0.5236^{\text{cbm}} = 523.6^{\text{kg}}$ .  
 $0.921 \times 523.6^{\text{kg}} = 482.24^{\text{kg}}$ . (3) Ans.  
Area =  $4\pi R^2 = \pi D^2 = 3.1416 \times 1^3 = 3.1416^{\text{qcm}}$ . (1) Ans.  
Area =  $4\pi R^2 = \pi D^2 = 3.1416 \times 10^2 = 314.16^{\text{qcm}}$ . (2) Ans.  
Area =  $4\pi R^2 = \pi D^2 = 3.1416 \times 100^2 = 31.416^{\text{qcm}}$ . (3) Ans.  
The first, if we take no account of friction. (4) Ans.

71. Given a cylinder 10 in. in diameter and 12 in. long; required the area of each end, the convex area, the total area, and the contents in gallons.

Area of end =  $3.1416 \times 5^2 = 3.1416 \times 25 = 78.54$  sq. in. (1) Ans. Convex area =  $\pi \times 10 \times 12 = 3.1416 \times 120 = 376.99$  sq. in. (2) Ans. Total surface =  $376.99 + 2 \times 78.54 = 534.07$  sq. in. (3) Ans.  $V = \frac{78.54 \times 12}{231}$  gals. = 4.08 gals. (4) Ans.

72. Find the capacity in gallons of a round cistern 13 ft. in diameter and 9 ft. deep.

$$V = \frac{3.1416 \times 6.5^2 \times 9 \times 1728}{231}$$

$$\log 3.416 = 0.4971$$

$$\log 6.5^2 = 1.6258$$

$$\log 9 = 0.9542$$

$$\log 1728 = 3.2375$$

$$\operatorname{colog} 231 = 7.6364 - 10$$

$$3.9510 = \log 8935.$$

$$8935 \text{ gals. } Ans.$$

73. What must be the diameter of a cylinder 10 in. deep, in order that it may hold 1 gallon?

$$V = \pi R^2 \times h$$
.  $231 = \pi R^2 \times 10$ .  $R = \sqrt{\frac{231}{10 \pi}}$   $\log 231 = 2.3636$   $\operatorname{colog} 10 = 9.0000 - 10$   $\operatorname{colog} 3.1416 = 9.5029 - 10$   $2)0.8665$   $0.4333 = \log 2.712$ .  $2.712 \text{ in. } \times 2 = 5.424 \text{ in. } Ans.$ 

- 74. Find the volume of a cylinder 8 in. in diameter and 11 in. high.  $V = \pi \times 4^2 \times 11 = 3.1416 \times 16 \times 11 = 552.92$  cu. in. Ans.
- 75. Find the dimensions of three cylinders that have the diameters equal to the heights, and hold 1 gal., 1 qt., and 11 respectively.

$$V = \pi R^3 h = \pi \left(\frac{D}{2}\right)^3 D = \frac{\pi D^3}{4}.$$

$$231 = \frac{\pi D^2}{4}.$$

$$D = \sqrt[3]{\frac{4 \times 231}{3.1416}}.$$

$$\log 4 = 0.6021$$

$$\log 231 = 2.3636$$

$$\cosh 3.1416 = 9.5029 - 10$$

$$3) \frac{2.4686}{0.8229} = \log 6.651$$

$$6.65 \text{ in. (1) } Ans.$$

$$V = \frac{\pi D^3}{4}.$$

$$1 \text{ qt. } = \frac{2 \text{ $1$}}{4} \text{ cu. in.}$$

$$2 \text{ $3$} = \pi D^3.$$

$$D = \sqrt[3]{\frac{231}{3.1416}}.$$

$$\log 231 = 2.3636$$

$$0.6222 = \log 4.19.$$

$$4.19 \text{ in. (2) } Ans.$$

$$V = \frac{\pi D^3}{4}.$$

$$1^{1} = 1000^{\text{com}}.$$

$$1^{1} = 1000^{\text{com}}.$$

$$1000 = \frac{\pi D^3}{4}.$$

$$109 \text{ $4000} = 3.6021$$

$$1000 = 3.6021$$

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76. Find the volume of a triangular prism 11 in. long, the sides of the ends being 2, 3, and 4 in. long.

Area of end = 
$$\sqrt{4.5 \times 2.5 \times 1.5 \times 0.5}$$
 = 2.9047.  
 $V = 11 \times 2.9047 = 31.952$  cu. in. Ans.

77. Find the capacity in bushels of a bin 6 ft. long, the end of which is a square measuring 3 ft. 3 in. on a side.

$$V=6 \times 3\frac{1}{4} \times 3\frac{1}{4} = 6 \times \frac{13}{4} \times \frac{13}{4} = \frac{507}{8} = 63\frac{3}{8}$$
 cu. ft.  
 $0.80356$  bu. = 1 cu. ft.  
 $0.80356 \times 63\frac{3}{8} = 50.93$  bu. Ans.

78. Find the number of cubic yards in a square prism 200 ft. on a side, and 40 ft. long.

$$V = \frac{200^2 \times 40}{27} = 59259\frac{7}{27}$$
 cu. yds. Ans.

79. How many cubic yards in a square pyramid 210 ft. on a side, and 123 ft. high?

210 ft. = 70 yds.  
123 ft. = 41 yds.  

$$V = \frac{1}{3}(70^2 \times 41) = 66966\frac{3}{3}$$
 cu. yds. Ans.

80. Find the capacity of a cup, the mouth of which is a square 4 in. on a side, and the sides of which are four equilateral triangles.

$$\frac{1}{2}$$
 the diagonal of base  $= \frac{1}{2}\sqrt{16+16} = \frac{1}{2}\sqrt{32}$ .  
Altitude  $= \sqrt{4^2 - (\frac{1}{2}\sqrt{32})^2} = \sqrt{16-8} = \sqrt{8} = 2.8285$ .  
 $V = \frac{1}{2}$  of  $16 \times 2.8285 = 15.085$  cu. in. Ans.

81. The largest of the Egyptian pyramids is 147<sup>m</sup> high, with a base 231<sup>m</sup> square. Find its volume in cubic meters.

$$\frac{1}{3}$$
 of  $231^2 \times 147 = 2,614,689^{\text{cbm}}$ . Ans.

82. The slant depth of a conically-shaped drinking-cup is  $93^{mm}$  and the diameter at the top  $8^{cm}$ . What is its capacity?

93<sup>mm</sup> = 9.3<sup>cm</sup>.  
Height = 
$$\sqrt{9.3^2 - 4^2} = 8.3958$$
<sup>cm</sup>.  
 $V = \frac{1}{8}\pi \times 4^2 \times 8.3958$ <sup>cm</sup>  
=  $\frac{1}{8}$  of 3.1416 × 16 × 8.3958 = 140.67<sup>ccm</sup> = 0.14067<sup>1</sup>. Ans.

83. The volume of a cone is 1°bm; its height is equal to the radius of its base. Find the dimensions of the cone.

$$V = \frac{\pi R^{2}h}{3} \qquad V = \frac{\pi R^{2}}{3} \qquad R^{2} = \frac{3V}{\pi} \qquad R = \sqrt{\frac{3 \times 1000000}{\pi}}$$

$$\log 3,000,000 = 6.4771$$

$$\cosh 3.1416 = 9.5029 - 10$$

$$3)5.9800$$

$$1.9933 = \log 98.47.$$

$$98.47^{\text{cm}}. Ans.$$

84. Find the capacity of a wash-bowl 30 in diameter and 5 deep.

$$\frac{1}{4}$$
 of  $30^2 - \frac{1}{4}$  of  $900 - 225$ .  
 $\frac{1}{8}$  of  $5^2 - \frac{1}{8}$  of  $25 - 8.33$ .  
 $225 + 8.33 - 233.33$ .  
 $\frac{1}{4}$  of  $5 \times 233.33 - 1833.31$  and  $\frac{1}{8}$ . Ans.

85. Find the capacity in liters of a boiler 89 in diameter and 31 cm deep.

$$\frac{1}{3}$$
 of  $89^2 = \frac{1}{4}$  of  $7921 = 1980.25$ .  
 $\frac{1}{3}$  of  $31^2 = \frac{1}{3}$  of  $961 = 320.33$ .  
 $1980.25 + 320.33 = 2300.58$ .  
 $\frac{1}{4}$  of  $31 \times 2300.58 = 112,071.11^{\text{com}} = 112.07^{\text{l}}$ . Ans.

86. Find the capacity in quarts of a bowl 10 in. in diameter and 4 in. deep.

\$\frac{1}{2}\$ of 
$$10^2 = \frac{1}{4}$ of  $100 = 25$ .

$\frac{1}{2}$ of  $4^2 = \frac{1}{8}$ of  $16 = 5.333$ .

$25 + 5.333 = 30.333.

$\frac{1}{2}$ of  $4 \times 30.333 = 190.66$ cu. in.

$1$ qt. = 57.75 cu. in.

$190.66 + 57.75 = 3.3$ qts. Ans.$$$$

87. Find the capacity in pints of a saucer 6 in. across and 1½ in. deep; of a bowl 7 in. across and 3 in. deep; of a bowl 8 in. across and 3½ in. deep.

1 pt. = 
$$\frac{1}{8}$$
 of 231 cu. in. = 28.875 cu. in.  
 $\frac{1}{4}$  of  $6^2 = \frac{1}{4}$  of  $36 = 9$ .  
 $\frac{1}{8}$  of  $(1\frac{1}{2})^2 = \frac{1}{8}$  of  $\frac{9}{4} = 0.75$ .  
 $9 + 0.75 = 9.75$ .  
 $\frac{1}{7}$  of  $1.5 \times 9.75 = 22.982$  cu. in.  
1 pt. = 28.875 cu. in.  
22.982 + 28.875 = 0.8 pt. (1) Ans.  
 $\frac{1}{4}$  of  $7^2 = \frac{1}{4}$  of  $49 = 12.25$ .  
 $\frac{1}{8}$  of  $3^2 = \frac{1}{8}$  of  $9 = 3$ .  
12.25 + 3 = 15.25.  
 $\frac{1}{7}$  of  $3 \times 15.25 = 71.893$  cu. in.  
71.893 + 28.875 = 2.5 pts. (2) Ans.  
 $\frac{1}{8}$  of  $(\frac{7}{2})^2 = \frac{1}{8}$  of  $\frac{49}{4} = 4\frac{1}{12}$ .  
 $16 + 4\frac{1}{12} = 20\frac{1}{12}$ .  
 $\frac{4}{7} \times \frac{7}{2} \times \frac{241}{12} \times \frac{8}{231} = \frac{241}{63} = 3.8$  pts. (3) Ans.

88. How many gallons will a boiler 5 ft. in diameter and 2 ft. deep hold?

$$\frac{1}{4}$$
 of  $5^2 = \frac{1}{4}$  of  $25 = 6.25$ .  
 $\frac{1}{8}$  of  $2^2 = \frac{1}{8}$  of  $4 = 1.333$ .  
 $6.25 + 1.333 = 7.583$ .  
 $\frac{1}{4}$  of  $2 \times 7.583 = 23.832$  cu. ft.  
 $23.832 \times 1728 + 231 = 178.3$  gals. Ans.

89. How many gallons will a boiler 30 in. in diameter and 1 ft. deep hold?

1 of 
$$30^2 = \frac{1}{4}$$
 of  $900 = 225$ .  
225 + 48 = 273.  
1 of  $12 \times 273 = 5148$  cu. in.  
5148 + 231 = 22.3 gals. Ans.

**90.** Find the capacity in pints of a cylinder 1.9375 in. in diameter, 2.4375 in. high; of a cylinder  $3\frac{1}{6}$  in. in diameter,  $3\frac{1}{6}$  in. high; of a cylinder  $3\frac{1}{6}$  in. high.

1 pt. = 28.875 cu. in.  

$$V = \frac{3.1416 \times 0.96875^2 \times 2.4375}{28.875}$$

$$\log 3.1416 = 0.4971$$

$$\log 0.96875^2 = 9.9724 - 10$$

$$\log 2.4375 = 0.3870$$

$$\text{colog} 28.875 = 8.5394$$

$$9.3959 - 10 = \log 0.2488.$$

$$0.249 \text{ pt. (1)} \quad Ans.$$

$$V = \frac{3.1416 \times 1.5625^2 \times 3.625}{28.875}$$

$$\log 3.1416 = 0.4971$$

$$\log 1.5625^2 = 0.3876$$

$$\log 3.625 = 0.5593$$

$$\text{colog} 28.875 = 8.5394 - 10$$

$$9.9834 = \log 0.9625.$$

$$0.963 \text{ pt. (2)} \quad Ans.$$

$$V = \frac{3.1416 \times 1.90625^2 \times 5.06}{28.875}$$

$$\log 3.1416 = 0.4971$$

$$\log 1.90625^2 = 0.5605$$

$$\log 3.1416 = 0.4971$$

$$\log 1.90625^2 = 0.5605$$

$$\log 5.0625 = 0.7044$$

$$\cosh 28.875 = 8.5394 - 10$$

$$0.3014 = \log 2.002.$$

$$2.002 \text{ pt. (3)} \quad Ans.$$

91. Find the capacity in pecks of a cylinder 15.865 in. in diameter, 12.5 in. high; of a cylinder 9.25 in. in diameter, 4.25 in. deep; of a cylinder 18.5 in. in diameter, 8 in. deep.

$$V = \frac{0.7854 \times 15.865^2 \times 12.5 \times 4}{2150.42}$$

$$\log 0.7854 = 9.8950 - 10$$

$$\log 15.865^{2} = 2.4009$$

$$\log 12.5 = 1.0969$$

$$\log 4 = 0.6021$$

$$\operatorname{colog} 2150.42 = 6.6675 - 10$$

$$0.6624 = \log 4.596.$$

4.596 pks. (1) Ans.

$$V = \frac{0.7854 \times 9.25^{2} \times 4.25 \times 4}{2150.42}$$

$$\log 0.7854 = 9.8950 - 10$$

$$\log 9.25^{2} = 1.9322$$

$$\log 4.25 = 0.6284$$

$$\log 4 = 0.6021$$

$$\operatorname{colog} 2150.42 = 6.6675 - 10$$

$$9.7252 - 10 = \log 0.531$$

0.531 pks. (2) Ans.

$$V = \frac{0.7854 \times 18.5^{2} \times 8 \times 4}{2150.42}$$

$$\log 0.7854 = 9.8950 - 10$$

$$\log 18.5^{2} = 2.5344$$

$$\log 8 = 0.9031$$

$$\log 4 = 0.6021$$

$$\text{colog } 2150.42 = 6.6675 - 10$$

$$0.6021 = \log 4.$$

92. What must be the diameter of a circle, in order that it may contain 78.54 sq. ft.? to contain 314.16 sq. ft.?

4 pks. (3) Ans.

Area = 
$$0.7854 \times D^2$$
.  
 $78.54 = 0.7854 \times D^2$ .  
 $D^2 = 100$ .  
 $D = 10$  ft. (1) Ans.  
Area =  $0.7854 \times D^2$ .  
 $314.16 = 0.7854 \times D^2$ .  
 $D^2 = 400$ .  
 $D = 20$  ft. (2) Ans.

93. What must be the diameter of a circle to contain 1 A.? to contain 9 A.?

94. What must be the diameter of a circle to contain 1<sup>ha</sup>? to contain 25<sup>ha</sup>?

$$\begin{array}{c} 1^{\text{ha}} = 10,000^{\text{qm}}, & D = \sqrt{\frac{10000}{0.7854}}. \\ \log 10,000 = 4.0000 \\ \operatorname{colog} 0.7854 = 0.1049 \\ 2)\underline{4.1049} \\ 2.0525 = \log 112.8. \\ 112.8^{\text{m}}. & (1) \ \textit{Ans.} \\ \sqrt{25} = 5. & 5 \times 112.8^{\text{m}} = 564^{\text{m}}. & (2) \ \textit{Ans.} \end{array}$$

95. Find the number that exceeds its square root by 20.

On testing the square numbers exceeding 20, namely, 25, 36, etc., we see that 25 is the number; and no process of approximation is needed.

25. Ans.

96. How much water will a hemispherical bowl hold that is 10 in. in diameter?

$$V = \frac{1}{4}$$
 of  $0.5236 \times D^{0} = \frac{1}{4}$  of  $0.5236 \times 1000 = 261.8$  cu. in. Ans.

97. What will it cost to gild a hemispherical dome 10 ft. in diameter, at 50 cents a square foot?

$$S = 2 \times 0.7854 \times 10^{3} = 157.08$$
 sq. ft.  $157.08 \times \$0.50 = \$78.54$ . Ans.

98. If the moon is a sphere 2170 miles in diameter, about how many million bushels would she hold if hollow? and how many yards of cloth a yard wide would it take to cover her?

$$2170 \text{ mi.} = 137,491,200 \text{ in.}$$
 $V = 0.5236 \times D^3.$ 
 $\log 137,491,200^3 = 24.4149$ 
 $\log 0.5236 = 9.7190 - 10$ 
 $\cosh 2150.42 = 6.6675 - 10$ 
 $\log V = 20.8014$ 
 $V = 633,000,000,000,000,000,000 \text{ bu.}$  (1) Ans.
 $2170 \text{ mi.} = 3,819,200 \text{ yds.}$ 
 $S = \pi D^2.$ 
 $\log 3,819,200^3 = 13.1640$ 
 $\log 3.1416 = 0.4971$ 
 $\log S = 13.6611$ 
 $S = 45,800,000,000,000,000 \text{ yds.}$  (2) Ans.

99. If the earth is 7920 miles in diameter, and the air is 40 miles deep, how many cubic miles of air are there about the planet?

100. What is the difference between 2 feet square and 2 square feet? between a foot square and a square foot? between half a foot square and 6 in. square?

- "2 feet square" means a square 2 ft. on a side; "2 square feet," any surface equivalent in area to two squares each 1 foot on a side. A "foot square" is a square; while a square foot is an equivalent area in any shape. "Half a foot square" is ambiguous. Half "a foot square" is half a square foot, while "half a foot" square is 6 inches square; that is, one-fourth a square foot.
- 101. Find the volume of a square frustum of which the base is 3 ft. square, top 2 ft. square, and height 4 ft.

$$V = \frac{1}{8} \times 4 \left[ \sqrt{3^2 \times 2^2} + 3^2 + 2^2 \right] = \frac{4}{8} (6 + 9 + 4) = 25\frac{1}{8}$$
 cu. ft. Ans.

102. Find the capacity in liquid quarts of a tin pan 10 in. in diameter at top, 8 in. in diameter at bottom, and 4 in. deep.

Volume of whole cone =  $\frac{1}{8} \times 0.7854 D^2 h = \frac{1}{8} \times 0.7854 \times 100 \times 20$ = 523.6 cu. in.

Volume of part cut off =  $\frac{1}{4}$  of  $0.7854 D^2 h = \frac{1}{4} \times 0.7854 \times 64 \times 16$ = 268.08 cu. in.

523.6 - 268.08 = 255.52 cu. in. 255.52 + 221 = 442 qts. Ans.

103. How many hektoliters will a circular vat hold  $5^m$  in diameter at the top,  $4.57^m$  at the bottom, and  $1.17^m$  deep?

Area of top  $-5^2 \times 0.7854 = 19.635^{qm}$ .

Area of base =  $4.57^{2} \times 0.7854 = 16.403^{qm}$ .

 $\sqrt{19.635 \times 16.403} = 17.946.$ 

 $\frac{1}{8}(19.635 + 16.403 + 17.946) \times 1.17 = 21.054^{\text{obm}} = 210.54^{\text{hl}}$ . Ans.

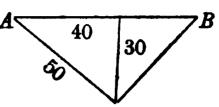
104. Find the area of an ellipse 8 in. by 11 in.; of an ellipse 15 in. by 21 in.

 $0.7854 \times 11 \times 8 = 69.115$  sq. in. (1) Ans.

 $0.7854 \times 15 \times 21 = 247.401$  sq. in. (2) Ans.

105. The ends of a cord 100 ft. long are fastened to stakes placed

80 ft. apart on level ground. A ring, to which a kid is tied, plays freely on the cord. How far from the straight line joining the stakes can the ring be pulled? What are the diameters of the ellipse which the



kid can graze? How many square feet in the ellipse?

The cord can be pulled from AB

$$\sqrt{50^2 - 40^2} = \sqrt{900} = 30$$
 ft. (1) Ans.

The diameters are 100 ft. and 60 ft. (2) Ans.

$$0.7854 \times 60 \times 100 = 4712.4$$
 sq. ft. (3) Ans.

106. Using the same rope as in the last problem, but putting the stakes 25 ft. apart, how many per cent is the kid's pasturage increased?

The rope can now be pulled from AB a distance of

$$\sqrt{50^2-12.5^2}=\sqrt{2343.75}=48.4$$
 ft.

Hence the diameters are 96.8 and 100.

Area 
$$= 96.8 \times 100 \times 0.7854 = 7602.7$$
.

Hence, 
$$\frac{7602.7 - 4712.4}{4712.4}$$
 of  $100 = 61.3$ . 61.3%. Ans.

107. A cylindrical log, 11 in. in diameter, is sawed off on such a slant that the pieces are 8 in. longer on the longest than on the shortest side. Find the dimensions of the ellipse thus made, and its area.

The shorter diameter is evidently the diameter of the log, or 11 in. The longer diameter is

$$\sqrt{11^2 + 8^2} = \sqrt{121 + 64} = \sqrt{185} = 13.6$$
 ft.  
Area =  $13.6 \times 11 \times 0.7854$ .  
log  $13.6 = 1.1335$   
log  $11 = 1.0414$   
log  $0.7854 = 9.8951 - 10$   
 $2.0700 = \log 117.5$  sq. in. Ans.

108. Find the length of a pendulum beating half-seconds; of a pendulum beating quarter-seconds.

The length of pendulums is inversely as the square of the number of vibrations in a given time.

Hence, a half-seconds pendulum will be  $\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$  the length of a seconds pendulum, or  $\frac{1}{4}$  of 39.138 in. = 9.784 in. (1) Ans.

A quarter-seconds pendulum will be  $\frac{1}{4} \times \frac{1}{4} = \frac{1}{18}$  the length of the seconds pendulum, or  $\frac{1}{18}$  of 39.138 in. = 2.446 in. (2) Ans.

109. How many centimeters long is a pendulum swinging 80 times a minute? A pendulum swinging 30 times a minute?

The first pendulum must be  $(\frac{60}{80})^3$  of 39.138 in. = 22.014 in.  $2.54 \times 22.014 = 55.92^{\text{om}}$ . (1) Ans.

The second pendulum must be  $(\frac{40}{30})^2$  of 39.138 in. = 156.552 in.  $2.54 \times 156.552 = 397.64$ cm. (2) Ans.

110. If a cannon-ball be suspended by a fine wire 176 ft. long in the central well of the Bunker Hill Monument, how many times a minute will it swing?

$$\sqrt{2112} : \sqrt{39.138} : : 60 : x.$$

$$x = \frac{60 \times \sqrt{39.138}}{\sqrt{2112}}$$

$$\log \quad 60 = 1.7782$$

$$\log \sqrt{39.138} = 0.7963$$

$$\cosh \sqrt{2112} = 8.3377 - 10$$

$$0.9122 = \log 8.17. \quad 8.17. Ans.$$

111. Find the lifting-power of a hydraulic press, the plunger being 1<sup>cm</sup> in diameter and driven with a force of 100<sup>kg</sup>, if the lifting-piston is 1<sup>m</sup> in diameter.

Suppose the plunger and piston square: the one would press on a surface of 10,000 pcm, the other on a surface of 10,000 pcm. By driving the plunger in 10 pcm, you force 10 pcm of water under the piston. But as this is spread under 10,000 pcm, you raise the piston thereby only 0.001 pcm; that is, only 0.0001 part of the way you move the plunger. Hence, by the principle of virtual velocity (what is lost in time is gained in power), you lift the piston with 10,000 times your force of 100 pcm applied. The lifting power, in other words, is 1,000,000 pcm, or 1000 pcm.

112. If the plunger is  $\frac{1}{2}$  in. in diameter, and is driven with a force of 1000 lbs., how much can it lift with a lifting-piston 4 ft. in diameter?

$$\frac{1}{2}$$
 in. : 4 ft. = 1 : 96,  
 $1^2$  :  $96^2$  = 1 : 9216.  
 $9216 \times 1000$  lbs. = 9,216,000 lbs. Ans.

113. If the plunger is 2 in. in diameter, and is driven with a force of 1000 lbs., how much can it lift with a lifting-piston 2 ft. in diameter?

2 in.: 2 ft.:: 1:12,  

$$1^2: 12^2 = 1:144.$$
  
 $144 \times 1000 \text{ lbs.} = 144,000 \text{ lbs.}$  Ans.

114. The water stands in a fissure in a rock 10<sup>m</sup> high and 12<sup>m</sup> long. What pressure is exerted to split the rock on the lowest meter's width? on the highest meter's width? in the whole fissure?

$$1 \times 12 \times 9.5 = 114^{\text{cbm}} = 114 \text{ t. (1)}$$
 Ans.  
 $1 \times 12 \times 0.5 = 6^{\text{cbm}} = 6 \text{ t. (2)}$  Ans.  
 $10 \times 12 \times 5 = 600^{\text{cbm}} = 600 \text{ t. (3)}$  Ans.

115. A dam is 100 ft. long and 10 ft. deep, and the water is just flowing over it. What pressure is exerted over the lowest two feet of the dam?

$$2 \times 9 \times 100 = 1800$$
 cu. ft.  
 $1800 \times 62\frac{1}{2}$  lbs. = 112,500 lbs.  
 $112,500 \div 2000 = 56\frac{1}{2}$  t. Ans.

116. What velocity in meters a second will a cannon-ball acquire in falling three-quarters of a second? in falling three and a quarter seconds?

$$\frac{3}{4}$$
 of  $9.806^{m} = 7.3545^{m}$ . (1) Ans.  $3\frac{1}{4}$  of  $9.806^{m} = 31.869^{m}$ . (2) Ans.

117. How long will it take a leaden ball, rolling off a table 29 in. high, to reach the floor?

29 in. = 
$$0.7366^{m}$$
.  
4.903:  $0.7366 = 1^{2}$ :  $x^{2}$ .  
 $x = \sqrt{\frac{0.7366}{4.903}}$ .

$$\log 0.7366 = 9.8673 - 10$$

$$\cos 4.903 = 9.3095 - 10$$

$$9.1768 - 10$$

$$10.0000 - 10$$

$$2)19.1768 - 20$$

$$9.5884 - 10 = \log 0.3876$$

118. What velocity will a crowbar attain in falling endwise from a balloon 2000<sup>m</sup> high? How long will it be in coming down?

$$4.903^{m}: 2000^{m} = 1^{2}: x^{2}.$$

$$x = \sqrt{\frac{2000}{4.903}}.$$

$$\log 2000 = 3.3010$$

$$\operatorname{colog} 4.903 = 9.3095 - 10$$

$$2) 2.6105$$

$$20.2 \text{ sec. (2) } Ans.$$

$$1.3053 = \log 20.2.$$

$$20.2 \times 9.806^{m} = 198.0812^{m}.$$

$$198^{m} \text{ per sec. (1) } Ans.$$

119. What velocity will a crowbar attain in falling endwise from a balloon one mile and a quarter high? How long will it be coming down?

$$4.903^{m} = 16.086 \text{ ft.}$$

$$1\frac{1}{4} \text{ mi.} = 6600 \text{ ft.}$$

$$16.086 : 6600 = 1^{2} : x^{2}.$$

$$x = \sqrt{\frac{6600}{16.086}}.$$

$$\log 6600 = 3.8195$$

$$\operatorname{colog} 16.086 = 8.7936 - 10$$

$$2) 2.6131$$

$$20.26 \text{ sec.} (2) Ans.$$

$$2 \times 20.26 \times 16.086 \text{ ft.} = 651.80 \text{ ft.}$$

$$651.8 \text{ ft. per sec.} (1) Ans.$$

120. If Carisbrook Well is 210 ft. deep, how long after a pebble is dropped will it be before it is heard to strike the bottom, if its velocity is reckoned at 32 ft. at the end of a second, and the velocity of sound is 1120 ft. a second?

$$16: 210 = 1^{2}: x^{2}$$

$$x = \sqrt{\frac{210}{16}}$$

$$\log 210 = 2.3222$$

$$\operatorname{colog} 16 = 8.7959 - 10$$

$$2)1.1181$$

$$0.5591 = \log 3.623.$$

$$3.623 \text{ sec. in falling.}$$

$$\frac{210}{1120} = 0.188 \text{ sec. sound in rising.}$$

$$3.623 + 0.188 = 3.811 \text{ sec. } Ans.$$

121. On the same suppositions as in Ex. 120, how long after a pebble is dropped will it be heard to strike the bottom of a ventilating shaft 1600 ft. deep?

$$16:1600 = 1^{2}: x^{2}$$

$$x = \sqrt{\frac{1600}{18}} = \sqrt{100} = 10 \text{ sec.}$$

$$\frac{1600}{180} = 1.429 \text{ sec.}$$

$$10 + 1.429 = 11.429 \text{ sec.}$$
Ans.

122. If a pebble is dropped over a precipice, and is heard to strike the bottom in 7½ sec., how far has it fallen, on the same suppositions as in Ex. 120?

Assume 745 ft. and 750 ft. to be the distance.

$$16:745 = 1^2:x^2$$

$$x = \sqrt{\frac{745}{16}}$$

$$\log 745 = 2.8722$$

$$\cosh 16 = 8.7959 - 10$$

$$2)1.6681$$

$$- \log 6.825.$$

$$\frac{745}{1120} = 0.665.$$

$$6.825 + 0.665 = 7.49 \text{ sec.}$$

$$An error of -0.01.$$

$$16:750 = 1^2:x^2$$

$$x = \sqrt{\frac{750}{16}}$$

$$\log 750 = 2.8751$$

$$\cosh 16 = 8.7959 - 10$$

$$2)1.6710$$

$$0.8355$$

$$= \log 6.847.$$

$$\frac{750}{1120} = 0.670.$$

$$6.847 + 0.670 = 7.517 \text{ sec.}$$

$$An error of +0.017.$$

Difference between errors is 0.027.

Error of 745:5 = 0.01:0.027. Error of 745:5 = 10:27. Error of  $745 \times 27 = 50$ . Error of  $745 = \frac{5}{27} = 1.8$ . 745 + 1.8 = 746.8 ft. 747 ft. Ans.

123. A pebble dropped down a shaft is heard to strike the bottom in 3 sec. after it begins to fall. Find the depth of the shaft.

## **Assume 130 and 140.**

$$16: 130 = 1^{2}: x^{2}.$$

$$x = \sqrt{\frac{130}{16}}.$$

$$\log 130 = 2.1139$$

$$0.4549$$

$$\cos 16 = 8.7959 - 10$$

124. How long will it take a ball, rolling off a table, to drop 1<sup>--</sup>? 1 in.? 10<sup>--</sup>? 6 in.?

$$4.903^{m}: 1^{cm} = 1^{2}: x^{2}.$$

$$4.903^{m}: 1 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903^{m}: 1 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903: 0.0254 = 1^{2}: x^{2}.$$

$$x = \sqrt{\frac{0.01}{4.903}}.$$

$$x = \sqrt{\frac{0.0254}{4.903}}.$$

$$\log 0.01 = 8.0000 - 10$$

$$\cosh 4.903 = 9.3095 - 10$$

$$2)17.3095 - 20$$

$$8.6548 - 10$$

$$= \log 0.04517.$$

$$0.04517 \text{ sec. (1) } Ans.$$

$$0.07198 \text{ sec. (2) } Ans.$$

$$4.903^{m}: 10^{mm} = 1^{2}: x^{2}.$$

$$4.903^{m}: 6 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903^{m}: 6 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903^{m}: 6 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903: 0.1524 = 1^{2}: x^{2}.$$

$$x = \sqrt{\frac{0.1524}{4.903}}.$$

$$x = \sqrt{\frac{0.1524}{4.903}}.$$

$$\log 0.1 = 9.0000 - 10$$

$$\cosh 4.903 = 9.3095 - 10$$

$$2) 18.3095 - 20$$

$$9.1548 - 10$$

$$= \log 0.1428.$$

$$0.1428 \text{ sec.} (3) \text{ Ans.}$$

$$4.903^{m}: 6 \text{ in.} = 1^{2}: x^{2}.$$

$$4.903: 0.1524 = 1^{2}: x^{2}.$$

$$2\cos (0.1524 = 9.1830 - 10$$

$$\cos (0.1524 = 9.1830 - 10$$

125. With what velocity will water flow through a hole 9 ft. below the surface?

$$\sqrt{9}$$
:  $\sqrt{16} = 3$ : 4.  $\frac{1}{2}$  of  $32 = 24$  ft. Ans.

126. With what velocity will water leave a fountain having free play, and a head of 25 ft.? a head of 100 ft.?

$$\sqrt{25}$$
:  $\sqrt{16} = 5:4$ .  $\frac{5}{4}$  of  $32 = 40$  ft. (1) Ans.  $\sqrt{100}$ :  $\sqrt{16} = 10:4=5:2$ .  $\frac{5}{4}$  of  $32 = 80$  ft. (2) Ans.

127. If a hole in the side of a cistern 4 ft. below the surface of the water is delivering 10 gals. an hour, how many gallons would it deliver with 5 ft. more head?

$$\sqrt{4}$$
:  $\sqrt{9} = 10$ : x.  $2: 3 = 10: x$ .  $x = \frac{30}{2} = 15$  gals. Ans.

128. If a pipe 2 in. in diameter, and 1 ft. long, inserted in a dam, the head of water being kept constant, delivers 4 gals. a minute, how many gallons a minute may be expected when another pipe of the same length, but 2½ in. in diameter, is substituted for the two-inch pipe?

$$2^2:(2\frac{1}{2})^2=4:x.$$
  $4:6\frac{1}{4}=4:x.$   $x=6\frac{1}{4}$  gals. Ans.

129. If a one-inch pipe, 20 in. long, is substituted for the two-inch pipe, 1 ft. long, in Ex. 128, and the flow is found to be 5 pts. a minute, what part of the diminution is due to the smaller area of the orifice, and what part to the increased friction on the sides of the longer pipe?

$$2^{2}: 1^{2} = 4: x$$
.  $4: 1 = 4: x$ .  $x = 1$  gal.  $4 - 1 = 3$  gals. (1) Ans. 1 gal.  $= 8$  pts.  $8 - 5 = 3$  pts. (2) Ans.

130. A miller is using water flowing through the gate-way under 4 ft. head. How much more work could he do if the head was raised to 9 ft.? how much more if the head was raised to 25 ft.?

$$\sqrt{4^{3}} : \sqrt{9^{3}} = 1 : x. 
\sqrt{64} : \sqrt{729} = 1 : x. 
8 : 27 = 1 : x. 
x =  $\frac{27}{8}$  =  $3\frac{3}{8}$ . (1) Ans. 
$$\sqrt{4^{3}} : \sqrt{25^{3}} = 1 : x. 
\sqrt{64} : \sqrt{15625} = 1 : x. 
8 : 125 = 1 : x. 
x =  $\frac{125}{8}$  =  $15\frac{5}{8}$ . (2) Ans.$$$$

131. If a top 3 in. in diameter is making 200 revolutions a second, with what force does the outer layer pull away from the centre?

$$1.227 \times \frac{1}{8} \times 200^{2} = 6135$$
.  
6135 times the weight of the material. Ans.

132. If a sling 30 in. long contains a stone, and is whirled round 80 times a minute, what is the force pulling on the string?

$$30 \text{ in.} = 2\frac{1}{2} \text{ ft.}$$
 $1.227 \times 2\frac{1}{2} \times (1\frac{1}{8})^2 = 5.453.$ 
 $5.453 \text{ times weight when even with the hand.}$ 
 $5.453 - 1 = 4.453 \text{ times weight when highest.}$ 
 $5.453 + 1 = 6.453 \text{ times weight when lowest.}$ 

183. With what force does a locomotive running at 30 mi. an hour, on a curve of 800 ft. radius, bear against the outer rail?

30 mi. per hr. =  $\frac{1}{2}$  mi. per min. =  $\frac{1}{120}$  mi. per sec. = 44 ft. per sec. Diameter is 1600 ft.

 $3.1416 \times 1600 = 5026.56$  ft. circumference.

Hence, the locomotive makes  $\frac{44}{5026.56}$  revolutions per sec.

Force = 
$$1.227 \times 800 \times \left(\frac{44}{5026.56}\right)^2$$
.  

$$\log \quad 1.227 = 0.0889$$

$$\log \quad 800 = 2.9031$$

$$\log \quad 44^2 = 3.2870$$

$$\cosh 5026.56^2 = 2.5974 - 10$$

$$\log \text{ force} \qquad = 8.8764 - 10 = \log 0.07523.$$

$$0.07523 \text{ times weight. } Ans.$$

134. If washed wool is put wet into a wire basket 1.2<sup>m</sup> in diameter, and the basket is set to spinning at the rate of 180 revolutions a minute, with what force is water wrung out of the wool?

180 revolutions per min. = 3 revolutions per sec.  $4.025 \times 0.6 \times 3^2 = 21.735$ . 21.735 times its weight. Ans.

135. If steel pens are revolved in a basket 32cm in diameter, 17 revolutions a second, with what force is the oil drained from them?

 $4.025 \times 0.16 \times 17^2 = 186.116$ . 186.116 times weight. Ans.

136. How strong a horizontal pull on a chain, weighing half a pound to the yard, is required to make the lowest part curve with an 18-in. radius? with a 6-ft. radius?

18 in.  $= \frac{1}{2}$  yd. 6 ft. = 2 yds.  $\frac{1}{2}$  yd. weighs  $\frac{1}{4}$  lb. 2 yds. weigh 1 lb.  $\therefore$  tension  $= \frac{1}{4}$ . (1) Ans.  $\therefore$  tension = 1 lb. (2) Ans.

137. A \(\frac{2}{4}\)-in. rope, weighing \(\frac{1}{4}\) of a pound to the yard, is fastened at one end to a staple, and near the other end, on the same level, runs over a pulley, and has a 25-lb. weight hung to it. What is the radius of its curvature at the middle?

The horizontal tension is 25 lbs., which represents 100 yds. of rope. : radius = 100 yds. Ans.

138. A shower wets the rope of Ex. 137, and increases its weight 40%; what does its radius now become?

The weight of the rope being  $\frac{148}{100} = \frac{7}{3}$  of what it was, it takes only \$ of 100 yds. = 71\$ yds. Ans.

139. A steam-tug, in attempting to move a ship, straightened her hawser until the radius of the lowest point was 1980 ft. The rope was wet, and weighed 3½ lbs. to the yard. With what force was it stretched?

1980 ft. = 660 yds., and  $3\frac{1}{4} \times 660 = 2145$  lbs. tension. Ans.

140. A chain 31 ft. long hangs between points on a level, and sags 4 ft.? What is the radius at the lowest point?

$$R = \frac{(\frac{1}{2} \text{ ch.} \times \text{sag})(\frac{1}{2} \text{ ch.} - \text{sag})}{2 \text{ sag}} = \frac{(15.5 + 4)(15.5 - 4)}{2 \times 4}$$
$$= \frac{19.5 \times 11.5}{8} = 28.031 \text{ ft. } Ans.$$

141. The whole chain, in Ex. 140, weighs 18 lbs. What is the What is the distance of the points apart? horizontal tension? What is the slant, or batter, of the end of the chain?

$$T$$
 = weight of  $R$ . 1 ft. weighs  $\frac{18}{31}$  lb. Tension =  $\frac{18}{31} \times 28.031 = 16.27$  lbs. (1)  $Ans$ .

From Prop. III.

From Prop. 111.

$$\log \frac{1}{2} \operatorname{span} = \log 19.5 + \log 11.5 + \log (1.29 - 1.0607) + \operatorname{colog} 4 + 0.0612$$
 $1.29 - 1.0607 = 0.2293$ .

 $\log 19.5 = 1.2900$ 
 $\log 11.5 = 1.0607$ 
 $\log 0.2293 = 9.3604 - 10$ 
 $\operatorname{colog} 4 = 9.3979 - 10$ 
 $0.0612$ 
 $1.1702 = \log 14.79$ .

 $2 \times 14.79 = 29.58$ . (2) Ans.

Batter =  $\frac{28.031}{15.5} = 1.808$ . (3) Ans.

142. A chain weighing 1<sup>kg</sup> to the meter is suspended from points on a level; the length of chain is 31<sup>m</sup>, and it sags 1.3<sup>m</sup>. Find all the conditions, and find how much it falls below a level at 10 m from each end.

$$\frac{1}{2} \text{ ch.} = 15.5^{\text{m}}.$$

$$\text{Radius} = \frac{(\frac{1}{2} \text{ ch.} + \text{sag})(\frac{1}{2} \text{ ch.} - \text{sag})}{2 \text{ sag}} = \frac{16.8 \times 14.2}{2.6}$$

$$= 91.75^{\text{m}}. \text{ (1) } Ans.$$

$$\text{Tension} = 91.75^{\text{kg}}. \text{ (2) } Ans.$$

From Prop. III.

log 
$$16.8 = 1.2253$$
log  $14.2 = 1.1523$ 
log  $0.0730 = 8.8633 - 10$ 
colog  $1.3 = 9.8861 - 10$ 

$$\frac{0.0612}{1.1882} = \log 15.42.$$

$$2 \times 15.42 = 30.84 \text{ span. (3)} \text{ Ans.}$$
Batter  $= \frac{91.75}{15.5} = 5.92$ . (4) Ans.

For drop with hypotenuse of  $10^{\text{cm}}$ ,
$$6: 10::1:x.$$

$$x = 1.667 \text{ depression.}$$
For drop with batter of  $10$ ,
$$5.92: 10::1:x.$$

$$x = 1.689.$$
1.689 depression. (5) Ans.

143. A chain 100<sup>m</sup> long, weighing 14 oz. to the foot, is suspended from points on a level 80<sup>m</sup> apart. What is the sag, the batter at the ends, and the horizontal tension?

Assume that the sag is 26.5<sup>m</sup>.

$$\log \frac{1}{2} \operatorname{span} = \log (\frac{1}{2} \operatorname{ch.} + \operatorname{sag}) + \log (\frac{1}{2} \operatorname{ch.} - \operatorname{sag}) + \log [\log (\frac{1}{2} \operatorname{ch.} + \operatorname{sag}) - \log (\frac{1}{2} \operatorname{ch.} - \operatorname{sag})] + \operatorname{colog} \operatorname{sag} + 0.0612$$

$$= \log (50 + 26.5) + \log (50 - 26.5) + \log [\log (50 + 26.5) - \log (50 + 26.5)] + \operatorname{colog} 26.5 + 0.0612$$

$$= \log 76.5 + \log 23.5 + \log (\log 76.5 - \log 23.5) + \operatorname{colog} 26.5 + 0.0612.$$

$$\log 76.5 = 1.8837$$

$$\log 23.5 = 1.3711$$

$$\log 0.5126 = 9.7098 - 10$$

$$\operatorname{colog} 26.5 = 8.5768 - 10$$

$$\frac{0.0612}{1.6026} = \log 40.05.$$

$$4 \operatorname{span} = 40.05.$$
 An error of + 0.05.

Assume that the sag is 
$$26.6^{m}$$
.

 $\log \frac{1}{2} \operatorname{span} = \log 76.6 + \log 23.4 + \log (\log 76.6 - \log 23.4) + \operatorname{colog} 26.6 + 0.0612$ .

 $\log 76.6 = 1.8842$ 
 $\log 23.4 = 1.3692$ 
 $\log 0.5150 = 9.7118$ 
 $\operatorname{colog} 26.6 = 8.5751$ 
 $0.0612$ 
 $1.6015 = \log 39.95$ .

Error of  $26.5 : 0.1 = 0.05 : 0.1$ .

An error of  $-0.05$ .  $\therefore$  error of  $26.5 : 0.1 = 0.05 : 0.1$ .

An error of  $-0.05$ .  $\therefore$  error of  $26.5 : 0.1 = 0.05$ .

 $\frac{1}{2} \operatorname{sag} = 26.5 + 0.05 = 26.55$ . Ans.

 $R = \frac{(50 + 26.55)(50 - 26.55)}{53.1} = \frac{76.55 \times 23.45}{53.1} = 33.806$ .

Batter  $= \frac{R}{\frac{1}{2} \operatorname{ch}} = \frac{33.806}{50} = 0.6761$ . Ans.

 $1^{m} = 3.28 \operatorname{ft}$ . 1 ft. weighs  $\frac{7}{4} \operatorname{lb}$ .

Tension  $= 33.806 \times 3.28 \times \frac{7}{4} \operatorname{lb}$ .  $= 97 \operatorname{lbs}$ .  $= 44^{\log}$ . Ans.

144. Suppose the points of suspension in Ex. 143 to remain unchanged, and the chain to be shortened 5<sup>m</sup>. What does the tension become?

Assume that the sag is 22.5.

log 
$$\frac{1}{2}$$
 span = log 25 + log 70 + log (log 70 - log 25)  
+ colog 22.5 + 0.0612.  
log 25 = 1.3979  
log 70 = 1.8451  
log 0.4472 = 9.6505 - 10  
colog 22.5 = 8.6478 - 10  
0.0612  
1.6025 = log 40.04.  
 $\frac{0.0612}{1.6025}$  = log 40.04.  
An error of + 0.04.

Assume that the sag is 22.6.

$$\log \frac{1}{2} \operatorname{span} = \log 70.1 + \log 24.9 + \log (\log 70 - \log 24.9) + \operatorname{colog} 22.6 + 0.0612.$$

$$\log 70.1 = 1.8457$$

$$\log 24.9 = 1.3962$$

$$\log 0.4489 = 9.6527 - 10$$

$$\operatorname{colog} 22.6 = 8.6459 - 10$$

$$0.0612$$

$$1.6017 = \log 39.96.$$
Error of  $22.5 : 0.1 = 0.04 : 0.08$ .
An error of  $-0.04$ .
Hence error of  $22.5 : 0.05$ .
$$\therefore \text{ sag is } 22.5 + 0.05 = 22.55^{m}.$$

$$R = \frac{24.95 \times 70.05}{45.1}$$

$$T = \frac{24.95 \times 70.05 \times 3.28087 \times 14}{45.1 \times 16}$$

$$\log 24.95 = 1.3971$$

$$\log 70.05 = 1.8454$$

$$\log 3.28087 = 0.5160$$

$$\log 14 = 1.1461$$

$$\operatorname{colog} 45.1 = 8.3458 - 10$$

$$\operatorname{colog} 45.1 = 8.3458 - 10$$

$$\operatorname{colog} 45.1 = 8.3458 - 10$$

$$\operatorname{colog} 16 = 8.7959 - 10$$

$$2.0463 = \log 111.3 \text{ lbs.}$$

$$T = 111.3 \text{ lbs.} Ans.$$

145. How long a rope is required between points 100 ft. apart to sag 30 ft.? 20 ft.? 10 ft.?

```
Assume that the chain is 120.9 ft.

\log \frac{1}{2} \operatorname{span} = \log (60.45 + 30) + \log (60.45 - 30) + \log [\log (60.45 + 30) - \log (60.45 - 30)] + \log 30 + 0.0612

= \log 90.45 + \log 30.45 + \log (\log 90.45 - \log 30.45) + \operatorname{colog} 30 + 0.0612.

\log 90.45 = 1.9564
\log 30.45 = 1.4836
\log 0.4728 = 9.6747 - 10
\operatorname{colog} 30 = 8.5229 - 10
0.0612
1.6988 = \log 49.99.

An error of -0.01.
```

```
Assume that the chain is 121 ft.
\log \frac{1}{2} \operatorname{span} = \log (60.5 + 30) + \log (60.5 - 30) + \log [\log (60.5 + 30)]
                 -\log(60.5-30) + colog 30 + 0.0612
            -\log 90.5 + \log 30.5 + \log (\log 90.5 - \log 30.5)
                 + \operatorname{colog} 30 + 0.0612
                                    90.5 = 1.9566
                             log
                                    30.5 - 1.4843
                             log
                             \log 0.4723 = 9.6741 = 10
                                      30 = 8.5229 - 10
                          colog
                                            0.0612
                                            1.6991 = \log 50.01.
                                           An error of +0.01.
             \frac{1}{2} span = 50.01.
             Error of 120.9:0.1=0.01:0.02.
             .. error of 120.9 is 0.05.
             \therefore chain is 120.9 + 0.05 = 120.95 ft. (1) Ans.
             Assume that the chain is 109.9 ft.
\log \frac{1}{2} \operatorname{span} = \log (54.95 + 20) + \log (54.95 - 20) + \log [\log (54.95 + 20)]
                 -\log(54.95-20)] + colog 20 + 0.0612
            = \log 74.95 + \log 34.95 + \log (\log 74.95 - \log 34.95)
                 + colog 20 + 0.0612.
                             \log 74.95 = 1.8748
                             \log 34.95 - 1.5435
                             \log 0.3313 - 9.5202 - 10
                                     20 = 8.6990 - 10
                          colog
                                            0.0612
                                            1.6987 = \log 49.97.
             \frac{1}{2} span = 49.97.
                                         An error of -0.03.
             Assume that the chain is 110 ft.
\log \frac{1}{2} \operatorname{span} = \log (55 + 20) + \log (55 - 20) + \log [\log (55 + 20)]
                 -\log(55-20)] + colog 20 + 0.0612
            = \log 75 + \log 35 + \log (\log 75 - \log 35) + \log 20 + 0.0612
                                     75 = 1.8751
                             log
                                     35 = 1.5441
                             log
                             \log 0.3310 = 9.5198 - 10
                                     20 = 8.6990 - 10
                          colog
                                            0.0612
                                            1.6992 = \log 50.02.
```

An error of +0.02.

 $\frac{1}{2}$  span = 50.02.

```
Error of 109.9:0.1 = 0.03:0.05.
             Error of 109.9:0.1=3.5.
             : error of 109.9 -\frac{0.3}{5} = 0.06.
             : chain is 109.9 + 0.06 = 109.96. (2) Ans.
             Assume that the chain is 102.5 ft.
\log \frac{1}{2} \operatorname{span} = \log (51.25 + 10) + \log (51.25 - 10) + \log [\log (51.25 + 10)]
                 -\log(51.25-10)] + colog 10 + 0.0612
            -\log 61.25 + \log 41.25 + \log (\log 61.25 - \log 41.25)
                 + colog 10 + 0.0612.
                            \log 61.25 = 1.7872
                            \log 41.25 = 1.6154
                            \log 0.1718 = 9.2350 - 10
                          colog
                                     10 = 9.0000 - 10
                                           0.0612
                                           1.6988 = \log 49.98.
                                        An error of -0.02.
             \frac{1}{4} span = 49.98.
             Assume that the chain is 102.7 ft.
\log \frac{1}{2} \operatorname{span} = \log (51.35 + 10) + \log (51.35 - 10) + \log [\log (51.35 + 10)]
                 -\log(51.35-10)] + colog 10 + 0.0612
            = \log 61.35 + \log 41.35 + \log (\log 61.35 - \log 41.35)
                 + colog 10 + 0.0612.
                            \log 61.35 = 1.7879
                            \log 41.35 = 1.6165
                            \log 0.1714 = 9.2340
                                     10 - 9.0000 - 10
                          colog
                                           0.0612
                                           1.6996 = \log 50.07.
                                        An error of +0.07.
             \frac{1}{2} span = 50.07.
             Error of 102.5:0.2=0.02:0.09.
            Error of 102.5:0.2=2:9.
             \therefore error of 102.5 = \frac{2}{3} of 0.2 = 0.044.
             Hence the chain is 102.5 + 0.044 = 102.544 ft. (3) Ans.
```

146. If 4 cu. in. of iron weigh 1 lb. avoirdupois, what is the weight of 1 cu. in. in grains? What is the specific gravity of the iron?

1 lb. = 7000 gr.  

$$\therefore$$
 1 cu. in. of the iron weighs  $\frac{1}{4}$  of 7000 = 1750 grs. (1) Ans.  
 $(1728 + 4) \times 16 = 6912$  oz.  $6912 + 1000 = 6.912$ . (2) Ans.

147. If 4 cu. in. of iron weigh 1 lb., what is the diameter of a 6-lb. ball? of a 32-lb. ball?

$$V=4\times 6=24$$
 cu. in.  $V=32\times 4=128$  cu. in.  $V=0.5236$   $D^3$ .  $D=\sqrt[3]{\frac{128}{0.5236}}$ .  $D=\sqrt[3]{\frac{128}{0.5236}}$ .  $O=\sqrt[3]{\frac{128}{0.5236}}$ .  $O=\sqrt[3]{\frac{1.6612}{0.5537}}$   $O=\sqrt[3]{\frac{1.6612}{0.5537}}$ 

148. If a block of iron (with all its corners square) measures 17.36 in. by 8.7 in. by 1.76 in., what does it weigh at ½ lb. to the cubic inch? and what would be the diameter if cast into a ball, if 11% is allowed for waste?

$$\frac{1}{4}$$
 of  $17.36 \times 8.7 \times 1.76 = 66.45$  lbs. (1) Ans.  
 $265.82 - 0.11$  of  $265.82 = 236.58$ .  
 $\log 236.58 = 2.3739$   
 $\operatorname{colog} 0.5236 = 0.2810$   
 $3) 2.6549$   
 $0.8850 = \log 7.673$ .  
7.673 in. (2) Ans.

149. Answer the same questions as in the last example, for a block of which the dimensions are 71.4 in. by 8% in. by 3% in.

$$71.4 \times 3\frac{1}{3} = 238.$$
  
 $238 \times 8\frac{2}{3} = 2062.67.$   
\$\frac{1}{2}\$ of  $2062.67 = 515.67$  lbs. (1) Ans.

$$\log 2062.67 = 3.3145$$

$$\log 0.89 = 9.9494 - 10$$

$$\cosh 0.5236 = 0.2810$$

$$3)3.5449$$

$$1.1816 = \log 15.19.$$

15.19 in. (2) Ans.

150. What is the diameter of a cylinder 11 in. long that holds 2 gals.?

2 gals. = 462 cu. in.  

$$V = \frac{1}{4}\pi D^{2} \times h.$$

$$462 = 0.7854 D^{2} \times 11.$$

$$D = \sqrt{\frac{462}{0.7854 \times 11}} = \sqrt{\frac{42}{0.7854}}.$$

$$\log 42 = 1.6232$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$2)1.7281$$

$$0.8641 = \log 7.313.$$
7.313 in. Ans.

151. What is the diameter of a cylinder 9 in. long that holds 2 gals.?

$$462 = 0.7854 D^{2} \times 9.$$

$$D = \sqrt{\frac{462}{0.7854 \times 9}}.$$

$$\log \quad 462 = 2.6646$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$\operatorname{colog} \quad 9 = 9.0458 - 10$$

$$2)1.8153$$

$$0.9077 = \log 8.086.$$

$$8.086 \text{ in. } Ans.$$

152. What is the diameter of a cylinder 30cm long that holds 1.?

$$10^{1} = 10000^{\text{com}}.$$

$$10000 = 0.7854 D^{2} \times 30.$$

$$D = \sqrt{\frac{1000}{0.7854 \times 3}}.$$

$$\log 1000 = 3.0000$$

$$\text{colog } 0.7854 = 0.1049$$

$$\text{colog } 3 = \frac{9.5229 - 10}{2)2.6278}$$

$$1.3139 = \log 20.6.$$
20.6cm. Ans.

153. What is the circumference of a globe if the square centimeters of its surface are three times the cubic centimeters of its volume?

$$V = 0.5236 \, D^3$$
.  $S = 3.1416 \, D^2$ .  $3.1416 \, D^2 = 3 \times 0.5236 \, D^3$ . Divide both sides by  $3 \times 0.5236 \, D^3$ .  $2 = D$ . Hence, circumference  $= 2 \times 3.1416 = 6.2832^{\text{cm}}$ . Ans.

154. Find the diameter of a circle of which the number of inches in its circumference is equal to the square feet of its area,

Area = 
$$\frac{1}{4}\pi D^2$$
 sq. ft.  
Circumference =  $\pi D$  ft. or  $12\pi D$  in.  
 $12\pi D = \frac{1}{4}\pi D^2$ .  
Multiply each side by 4.  
 $48\pi D = \pi D^2$ .  
Divide each side by  $\pi D$ .  
 $48 = D$ .  
 $\therefore D = 48$  ft. Ans.

155. How many times does a carriage-wheel 3 ft. 2 in. in diameter turn in going a mile on a smooth road?

The circumference of the wheel is
$$3\frac{1}{6} \times 3.1416 = 9.9484 \text{ ft.}$$

$$1 \text{ mi.} = 5280 \text{ ft.}$$

$$\therefore \text{ the wheel turns } \frac{5280}{9.9484} = 530.7 \text{ times. } Ans.$$

156. The top of a wheel is at each instant moving with twice the velocity of the carriage, and is moving in a curve whose centre, at the instant, is as far below ground as the point is above ground. What, then, is the force exerted to separate the mud from the top of a wheel 3 ft. 2 in. in diameter, when the carriage is moving at the rate of 10 mi. an hour?

The carriage going at 10 mi., the top of the wheel goes at 20 mi. per hour, or  $29\frac{1}{3}$  ft. per second. The radius of the curve is  $2 \times 3\frac{1}{6} = 6\frac{1}{3}$  ft., the total circumference of which would be  $12\frac{2}{3} \times 3.1416 = 39.7936$  ft.  $\therefore$  the force is

1.227 × 6
$$\frac{1}{3}$$
 ×  $\left(\frac{29.3333}{39.7936}\right)^2$  = 4 224 times the weight.  
log 1.227 = 0.0889  
log 6 $\frac{1}{3}$  = 0.8016  
log (29 $\frac{1}{3}$ )<sup>2</sup> = 2.9348  
colog (39.7936)<sup>2</sup> = 6.8004 - 10  
0.6257 = log 4.224. Ans.

157. A point in the tire, as a spike-head, moves, while the wheel rolls over once, just four times the diameter of the wheel. How far does the point travel while the wheel, 3 ft. 2 in. in diameter, travels 1 mi.?

In going one mile the wheel turns 530.7 times.  $\therefore$  the point travels  $3\frac{1}{6} \times 4 \times 530.7 = 6722.2$  ft. Ans.

158. An oil-can is formed of two cylinders connected by a frustum of a cone. The upper cylinder, or neck, is 60m in diameter, and 75mm high; the lower cylinder is 130m in diameter, and 153mm high; the total length of the can is 30cm. Find its capacity in liters.

A square shaft to enclose the neck would contain

$$6\times6\times7.5=270^{\text{com}};$$

one to enclose the body would contain

$$13 \times 13 \times 15.3 = 2585.7$$

The frustum to enclose the remainder would contain

$$(\sqrt{6 \times 6 \times 13 \times 13} + 169 + 36) \frac{1}{3} \text{ of } 7.2 = 679.2^{\text{ocm}}.$$
  
 $(270 + 2585.7 + 679.2) \times 0.7854 = 2776^{\text{com}} = 2.776^{1}.$  Ans.

159. A common tunnel is formed of a frustum of a cone terminated with a cylinder. The height of the frustum is 14cm, and the diameters of the two bases are 175mm and 16mm respectively. The cylinder is 8cm long. Find the capacity of the tunnel in liters.

```
16^{\text{mm}} = 1.6^{\text{cm}}.

The cylinder holds 1.6^2 \times 8 \times 0.7854 = 20.48 \times 0.7854^{\text{ccm}}.

The frustum holds \frac{1}{8}(17.5^2 + 1.6^2 + 17.5 \times 1.6) \times 0.7854

= 1571.78 \times 0.7854^{\text{ccm}}.

Both together hold (1571.78 + 20.48) \times 0.7854^{\text{ccm}}

= 1592.26 \times 0.7854^{\text{ccm}} = 1250^{\text{ccm}} = 1.25^1. Ans.
```

160. A pan is in the form of a frustum of a cone. The interior measurement is 10<sup>cm</sup> deep, 12<sup>cm</sup> across the bottom, and 23<sup>cm</sup> across the top. Find the capacity of the pan in liters.

$$\frac{10}{3}(12^{2} + 23^{2} + 12 \times 23) \times 0.7854 = \frac{10}{3}(144 + 529 + 276) \times 0.7854$$

$$= \frac{10}{3} \text{ of } 949 \times 0.7854$$

$$= 3163\frac{1}{3} \times 0.7854 = 2484.5^{\text{com}}$$

$$= 2.4845^{1}. \text{ Ans.}$$

161. A stove-pipe is 4<sup>m</sup> long, 26<sup>cm</sup> in diameter, and 1<sup>mm</sup> thick. Find how many square centimeters of sheet-iron it has taken to make it, if the edges lap one centimeter; and give the weight of the pipe, if the specific gravity of the sheet-iron is 7.8.

$$4^{\text{m}} = 400^{\text{cm}}$$
;  $1^{\text{mm}} = 0.1^{\text{cm}}$ .  
 $S = \pi Dh = (3.1416 \times 26 + 1) \times 400 = 33,072.64^{\text{qcm}}$ . (1) Ans.  
 $0.1 \times 33,072.64 = 3307.26^{\text{ccm}}$ .  
 $7.8 \times 3307.26 = 25,796.659^{\text{g}} = 25.8^{\text{kg}}$ . (2) Ans.

162. A spherical bomb is 32cm in diameter, and the sides 38cm thick. The specific gravity of the metal of which it is made is 7.2. Find its weight and interior capacity.

Inside diameter is 
$$32 - 2 \times 3.8 = 24.4$$
cm.  
 $V = 0.5236 D^8 = 0.5236 \times 24.4^3$ .  
 $\log 5236 = 9.7190 - 10$   
 $\log 24.4^3 = 4.1622$   
 $3.8812 = \log 7607$ .  
 $7607$ cm =  $7.607$ <sup>1</sup>. (1) Ans.

$$V = 0.5236 \times 32^8$$
.  
 $\log 32^8 = 4.5153$   
 $\log 0.5236 = 9.7190 - 10$   
 $4.2343 = \log 17,150$ .  
 $17,150^{\text{com}} = 17.15^1$ .  
 $7.2 \times (17.15 - 7.607) = 68.71^{\text{kg}}$ . (2) Ans.

163. The diameters of a lamp-shade are 25cm and 7cm; its slant height is 134mm. Give its curved surface in square centimeters.

$$134^{mm} = 13.4^{cm}$$
.  
 $\frac{25 + 7}{2} = 16$ , average diameter.  
 $3.1416 \times 16 \times 13.4 = 673.6^{qcm}$ . Ans.

164. A niche is formed like a half-cylinder surmounted by a quarter of a sphere. The height of the cylinder is 1.2<sup>m</sup>, the diameter 0.8<sup>m</sup>. Find the volume of the niche, and the area of its interior surface.

The volume of half-cylinder =  $\frac{1}{2}(0.8^2 \times 0.7854 \times 1.2) = 301.59^4$ . The volume of quarter-sphere =  $\frac{1}{4}(0.8^3 \times 0.5236) = 67.02^4$ .  $301.59 + 67.02 = 368.61^4$ . (1) Ans.

The surface of cylinder is  $\frac{1}{2} \times 0.8 \times 3.1416 \times 1.2 = 1.5080^{qm}$ ; of quarter-sphere,  $\frac{1}{4} \times 4 \times 0.8^2 \times 0.7854 = 0.5027^{qm}$ ; of floor,  $\frac{1}{2}(0.8^2 \times 0.7854) = 0.2513^{qm}$ .

 $1.5080 + 0.5027 + 0.2513 = 2.2620^{qm}. (2) Ans.$ 

165. A steam-boiler is formed of a cylinder terminated at each end by a hemispherical cap of the same diameter. The length of the cylinder is 3.4<sup>m</sup>, interior diameter 0.8<sup>m</sup>. Find the number of hektoliters of water required to fill the boiler half full.

The volume of cylinder is

$$3.4 \times 0.8^2 \times 0.7854 = 1.709^{\text{obm}} = 17.09^{\text{hl}}$$
.

The two caps form a sphere, the volume of which is

$$0.8^{3} \times 0.5236 = 0.268^{\text{cbm}} = 2.68^{\text{hl}}.$$
  
 $\frac{1}{2}(2.68 + 17.09) = 9.89^{\text{hl}}.$  Ans.

166. A hill 482 ft. high is 8 mi. from the shore. How many miles out at sea is it visible?

$$\frac{1}{2} \log 482 = 1.3415$$

$$\frac{0.1215}{1.4630} = \log 29.04.$$

$$29.04 - 8 = 21.04 \text{ mi. } Ans.$$

167. A sailor at the topmast 80 ft. above the sea can just see a sailor at the topmast of a similar ship. How many miles apart are the vessels?

$$\frac{1}{2} \log 80 = 0.9516$$

$$\frac{0.1215}{1.0731} = \log 11.83.$$
 $2 \times 11.83 \text{ mi.} = 23.66 \text{ mi.} Ans.$ 

168. A vessel approaching Valparaiso at daybreak just makes out the peak of Aconcagua, 23,000 ft. high and 140 mi. back from the coast. How far is the vessel from land if the eye of the observer is 30 ft. above the water?

$$\sqrt{\frac{7}{4}}$$
 of  $30 = \sqrt{52.5} = 7.25$  mi.  
 $\sqrt{\frac{7}{4}}$  of  $23000 = \sqrt{40250} = 200.6$  mi.  
 $200.6 - 140 = 60.6$ .  
 $60.6 + 7.25 = 67.85$  mi. Ans.

169. If Mount Washington is 6240 ft. high and 76 mi. in an air-line from Cape Elizabeth, how far out from the Cape will its peak be visible in the ordinary state of the atmosphere?

$$\sqrt{\frac{7}{4}}$$
 of  $6240 = \sqrt{10920} = 104.5$  mi.  $104.5$  mi.  $-76$  mi.  $= 28.5$  mi. Ans.

170. How many acres of water can a man see, standing on a raft with his eyes just 6 ft. above water, and no land in sight?

$$\frac{1}{2} \log 6 = 0.3891$$

$$\frac{0.1215}{0.5106}$$

$$\frac{2}{1.0212}$$

$$\log 3.1416 = 0.4971$$

$$\log 640 = \frac{2.8062}{4.3245} = \log 21,110.$$
21,110 A. Ans.

171. How far would a mountain 30,000 ft. high be visible? one of 5000 ft. high? one of 1000 ft. high?

$$\frac{1}{2} \log 30,000 = 2.2386$$
 $\frac{0.1215}{2.3601} = \log 229.2.$  229.2 mi. (1) Ans.
 $\frac{1}{2} \log 5,000 = 1.8495$ 
 $\frac{0.1215}{1.9710} = \log 93.55.$  93.55 mi. (2) Ans.
 $\frac{1}{2} \log 1,000 = 1.5000$ 
 $\frac{0.1215}{1.6215} = \log 41.83.$  41.83 mi. (3) Ans.

172. How high must a mountain be in order to be visible at sealevel 50 mi.? 100 mi.? 150 mi.?

# of 
$$50^2 = 4$$
 of  $2,500 = 1,429$  ft. (1) Ans.  
# of  $100^2 = 4$  of  $10,000 = 5,714$  ft. (2) Ans.  
# of  $150^2 = 4$  of  $22,500 = 12,860$  ft. (3) Ans.

173. How far is a mountain 1000<sup>m</sup> high visible? 2000<sup>m</sup> high?

$$\sqrt{15 \times 1000} = \sqrt{15000} = 122.5$$
km. (1) Ans.  $\sqrt{15 \times 2000} = \sqrt{30000} = 173.2$ km. (2) Ans.

174. How far can a man see from the shore, if he stands on a bluff that raises his eye 11<sup>m</sup> above the sea?

$$\sqrt{15 \times 11} = \sqrt{165} = 12.85$$
km. Ans.

175. If in steaming away from a mountainous island a sailor estimates his distance at 171km, when the island disappears beneath the wave, how high shall he estimate the mountains?

$$2 \times \log 171 = 4.4660$$
  
 $\operatorname{colog} 15^2 = 8.8239 - 10$   
 $3.2899 = \log 1950$ . 1950... Ans.

176. The flash of a gun is seen  $7\frac{1}{2}$  sec. before the report of the gun is heard; there is no wind, and the thermometer is 73° F. How far off was the gun?

$$73 - 57 = 16$$
.  
 $16 + 1114 = 1130$  ft. per sec.  
 $7\frac{1}{4} \times 1130 = 8475$  ft. Ans.

177. A meteor was seen to burst; the report followed in 4 min. 17 sec. What was its distance if the average temperature of the intervening air was 50° F.?

$$4 \text{ min. } 17 \text{ sec.} = 257 \text{ sec.}$$

$$57 - 50 = 7.$$

$$1114 - 7 = 1107 \text{ ft. per sec.}$$

$$257 \times 1107 + 5280 = 53.88 \text{ mi. } Ans.$$

178. Find the distances of the last two examples by § 461.

$$73^{\circ} \text{ F.} = 22.8 \text{ C.}$$
 $22.8 - 21 = 1.8.$ 
 $1.8 \times 0.53 = 0.95.$ 
 $7\frac{1}{2}(345 + 0.95) = 2594.6^{\text{m}} = 2.5946^{\text{km}}.$  (1) Ans.
 $50^{\circ} \text{ F.} = 10^{\circ} \text{ C.}$ 
 $0.53 \times (21 - 10) = 5.83.$ 
 $257 \times (345 - 5.83) = 87,166^{\text{m}} = 87.16^{\text{km}}.$  (2) Ans.

179. How long will it take for an explosion at the equator to be heard at the antipodes of the place, if the circumference of the earth at the equator be reckoned at 40,000km, and the average temperature at the equator at 23° C.?

$$0.53 \times (23 - 21) = 1.06^{m}$$
.  
 $345 + 1.06 = 346.06^{m} = 0.34606^{km}$   
 $20,000 + 0.34606 = 57,793$  sec.  
 $57,793$  sec. = 16 hrs. 3.2 min. Ans.

180. If an explosion at the equator occurs at sunset, and the average temperature east of the spot is 22° C., and that to the west 24° C., how far from the antipodes would the sounds meet?

The velocity at 22° C. is 345.53<sup>m</sup> per sec. The velocity at 24° C. is 346.59<sup>m</sup> per sec.

692.12<sup>m</sup> per sec. is the velocity with which the two sounds are approaching each other.

$$692.12:346.59::40,000:x.$$

$$x = \frac{346.59 \times 40000}{692.12} \text{ km.} = 20,030.63 \text{ km.}$$

$$20,030.63 - 20,000 = 30.63 \text{ km.} \quad Ans.$$

181. How far off is the lightning when the thunder follows in 13 sec., the temperature being 76° F.?

$$76 - 57 + 1114 = 1133$$
 ft.  
 $13 \times 1133 + 5280 = 2.79$  mi. Ans.

182. How long would it take sound to go through a whispering-tube 3 mi. long, temperature 61° F.?

$$61-57+1114=1118$$
 ft.  
 $3 \text{ mi.} = 3 \times 5280 = 15,840$  ft.  
 $15,804+1118=14.16$  sec. Ans.

183. Sound travels in iron about 10½ times as fast as in air. How long, then, after seeing the blow of a sledge-hammer given on the other end of an iron pipe 1½ mi. long, may I expect to hear the sound by the iron; and how long after, to hear the sound through the air in the pipe; thermometer 63° F.?

$$63 - 57 + 1114 = 1120$$
 ft. per sec.  
 $1\frac{1}{2}$  mi. = 7920 ft.  
 $7920 \div 1120 = 7.07$  sec. through air. (1) Ans.  
 $7.07 \div 10.5 = 0.67$  sec. through iron. (2) Ans.

184. Two gunners fire at each other simultaneously from forts 1½ mi. apart; the wind, at 70° F., blows steadily from one fort to the other, at 11 mi. an hour. How soon will each hear the report of the other's gun? Suppose one ball flies on the average 987 ft. a second, the other 818 ft. a second; when will each receive the other's shot?

$$70-57+1114=1127$$
 ft. per sec.  
 $1\frac{1}{2}$  mi. = 7920 ft.  
11 mi. per hr. = 16.1 ft. per sec

The velocity of the sound with the wind will be 1127 + 16.1 = 1143.1.

The velocity of the sound against the wind will be

1127 - 16.1 = 1110.9.

7920 + 1143.1 = 6.93 sec. (1st sound). Ans.

7920 + 1110.9 = 7.13 sec. (2d sound). Ans.

7920 + 987 = 8.02 sec. (1st ball). Ans.

7920 + 818 = 9.68 sec. (2d ball). Ans.

185. Sound travels in water about 4.26 times as fast as in air. How many seconds sooner would the sound of a torpedo exploded under water 2 mi. off reach you by water than by air, at 68° F.?

$$68 - 57 + 1114 = 1125$$
 ft. per sec.  
 $2 \text{ mi.} = 10,560$  ft.  
 $10,560 + 1125 = 9.387$  sec. in air.  
 $9.387 + 4.26 = 2.203$  sec. in water.  
 $9.387 - 2.203 = 7.18$  sec. Ans.

186. Required the expense of painting the walls and ceiling of a room 22 ft. 6 in. long, 13 ft. 6 in. wide, and 10 ft. high, at 30 cents a square yard.

$$2(22\frac{1}{2} + 13\frac{1}{2}) \times 10 = 720$$
 sq. ft., walls.  
 $22\frac{1}{2} \times 13\frac{1}{2} = 303.75$  sq. ft., ceiling.  
 $\frac{1}{3}(720 + 303.75) \times \$0.30 = \$34.13$ . Ans.

187. In what time would a cistern be filled by three pipes whose diameters are  $\frac{1}{2}$  in.,  $\frac{3}{4}$  in., and 1 in., when the largest alone would fill it in 40 min.; the rates of flow being proportional to the squares of the diameters?

The smallest alone would fill it in  $(\frac{2}{4})^2$  of 40 min. = 160 min. The other alone would fill it in  $(\frac{4}{3})^2$  of 40 min. =  $71\frac{1}{9}$  min. Hence, in 1 min., the largest fills  $\frac{1}{40}$  of the cistern, the smallest fills  $\frac{1}{160}$  of the cistern, the other fills  $\frac{9}{640}$  of the cistern, and all three together fill  $\frac{1}{40} + \frac{9}{160} + \frac{9}{640} = \frac{29}{640}$  of it. Hence, it will take  $1 + \frac{29}{640} = 22\frac{2}{9}$  min. Ans.

188. How many gallons of water are contained in a length of of 50 yds. of a canal, if its width at the top is 8 yds. and at the bottom 7 yds., and its depth 5 ft.?

The average width is  $7\frac{1}{2}$  yds. = 270 in.; 50 yds. = 1800 in.; 5 ft. = 60 in.

Volume = 
$$\frac{1800 \times 60 \times 270}{231}$$
 = 126,233.8 gals. Ans.

189. Find the weight supported by each of two men, A and B, who carry a hundred-weight suspended on a pole 6 ft. long, at a point 2 ft. 3 in. from A's end, if the pole weighs 16 lbs.

$$100 + 16 = 116$$
 lbs., total weight.  
 $6 - 2.25 = 3.75$  ft. from B's end.  
 $6: 3.75 = 100: x.$   
 $x = \frac{100 \times 3.75}{6} = 62.5$  lbs.  
 $62.5 + 8 = 70.5$ , A. (1) Ans.  
 $116 - 70.5 = 45.5$ , B. (2) Ans.

190. A man who rows 4 mi. an hour in still water takes 1 hr. 12 min. to row the same distance up a river. How long will it take him to row down again?

In still water, the man could row  $4 \times 1.2 = 4.8$  miles in 1 hr. 12 min. Hence, the stream bears him down 0.8 mi. in 1.2 hrs., or flows at the rate of  $\frac{2}{3}$  miles per hour. When he rows with the stream he will row  $4\frac{2}{3}$  miles per hour, and row 4 miles in  $\frac{2}{3}$  hr.  $\frac{2}{3}$  min. Ans.

191. How long a ladder will be required to reach a window 40 ft. from the ground, if the distance of the foot of the ladder from the wall is one-fifth of the length of the ladder.

Let l be the length of the ladder.

1 l is the distance of the foot from the wall.

The height of the wall is  $\sqrt{l^2 - \left(\frac{l}{5}\right)^2}$ .

But 40 is the height of the wall.

Therefore 
$$\sqrt{l^2-\left(\frac{l}{5}\right)^2}=40$$
.

*l* /

Square both sides,  $\frac{24}{25}l^2 = 1600$ . Divide both sides by  $\frac{24}{25}$ ,  $l^2 = 1666.67$ .  $\therefore l = \sqrt{1666.67} = 40.8$  ft. Ans.

192. If 3 oz. of gold 15 carats fine are mixed with 7 oz. 12 carats fine, what will be the fineness of the compound? What must be the fineness of 11 oz. so that, when added to this compound, the whole may be 14 carats fine?

$$3 \times 15 = 45$$
 $7 \times 12 = 84$ 

$$10)129$$

$$12.9 \text{ carats. (1) } Ans.$$

$$14 - 12.9 = 1.1 \text{ carats.}$$

$$1.1 \times 10 = 11 \text{ carats.}$$

$$11 + 11 + 14 = 15 \text{ carats. (2) } Ans.$$

193. Find the surface of each face of a cube whose volume is 14 cu. ft. 705.088 cu. in.

14 cu. ft. 705.088 cu. in. = 24,897.088 cu. in.

194. What must be the length of spermaceti candles 3 of an inch in diameter, that 6 of them may weigh a pound, if the specific gravity of spermaceti is 0.943?

$$V = 0.7854 \times \frac{7^2}{8^2} \times h \times 6$$
 cu. in.

1 lb. is the weight of  $\frac{1728}{0.943 \times 62.5}$  cu. in. of spermaceti.

Hence 
$$0.7854 \times \frac{7^2}{8^2} \times h \times 6 = \frac{1728}{0.943 \times 62.5}$$

$$h = \frac{1728 \times 8^2}{0.7854 \times 7^2 \times 6 \times 0.943 \times 62.5}$$

$$\log 1728 = 3.2375$$

$$\log 8^{2} = 1.8062$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$\operatorname{colog} 7^{2} = 8.3098 - 10$$

$$\operatorname{colog} 6 = 9.2218 - 10$$

$$\operatorname{colog} 0.943 = 0.0255$$

$$\operatorname{colog} 62.5 = 8.2041 - 10$$

$$0.9098 = \log 8.124.$$

8.124 in. Ans.

195. A cylinder 10 in. across and 10 in. high contains 0.3927 of a cubic foot of water. How many shot 0.1 in. in diameter must be poured in to raise the water to the top?

The volume of the cylinder is

$$0.785398 \times 10^{3} \times 10 = 785.398$$
 cu. in.  
 $0.3927$  cu. ft. =  $678.5856$  cu. in.  
 $785.398 - 678.5856 = 106.8124$  cu. in.  
 $0.1^{3} \times 0.5236 = 0.0005236$  cu. in., vol. of 1 shot.  
 $106.8124 + 0.0005236 = 203,997$ . Ans.

196. Determine the depth of conical-shaped wine-glasses 21 in. across the top, that 60 of them may hold a gallon.

 $\frac{1}{60}$  of 231 = 3.85 cu. in., the capacity of a glass. 2.5 × 2.5 × 0.7854 = 4.90875, the area of the top. 3 ×  $\frac{3.85}{4.90875}$  = 2.353 in. Ans. 197. A train approaching a station at the rate of 25 mi. an hour passes over two signals placed half a mile apart. Find the interval between the times at which their reports are heard at the station, sound travelling at the rate of 1090.2 ft. per second.

25 mi. an hr. is  $\frac{1}{2}$  mi. in  $1\frac{1}{3}$  min. = 72 sec.

When the train reaches the second signal, the sound of the first signal is  $72 \times 1090.2 - 2640$  ft. ahead of it; and this distance, divided by 1090.2, is  $72 \sec. - 2.4 = 69.6 \sec.$  Ans.

198. The apparent intensity of light varies inversely as the square of its distance. Find the point between two lamps 50 yds. apart at which one appears twice as bright as the other.

The distances are in the proportion  $\sqrt{1}$ :  $\sqrt{2} = 1$ : 1.4142, and 2.4142: 50 = 1: x. x = 20.71 yds., smaller distance. (1) Ans. 50 - 20.71 = 29.29 yds., greater distance. (2) Ans.

199. How deep may a round cistern 4 ft. across be made so as to be lined with the same lead as a cubical cistern 4 ft. each way? Compare their capacities.

 $4 \times 4 \times 4 = 64$  cu. ft. in cubical cistern.  $5 \times 16 = 80$  sq. ft. of lead to line it.  $0.7854 \times 16 = 12.5664$  sq. ft. in bottom of round cistern. 80 - 12.5664 = 67.4336.  $\frac{67.4336}{4 \times 3.1416} = 5.366$ . (1) Ans.  $16 \times 0.7854 \times 5.366 = 67.43$  cu. ft. in round cistern. (2) Ans.

200. The material for lining a cubical cistern cost \$10; find the cost of material for lining two similar cisterns which shall each hold one-half as much.

The cost is proportional to  $(\sqrt[3]{1})^2 : (\sqrt[3]{\frac{1}{2}})^2 = 1^2 : 0.7937^2 = 1 : 0.63$ . 1 : 0.63 = \$ 10 : x.  $x = \frac{\$ 10 \times 0.63}{1} = \$ 6.30$ .  $2 \times \$ 6.30 = \$ 12.60$ . Ans. 201. What distance can be seen from the top of a mountain 4 mi. high?

$$4 \text{ mi.} = 21,120 \text{ ft.}$$

$$\frac{1}{2} \log 21,120 = 2.1622$$

$$0.1215$$

$$192.2 \text{ mi. } Ans.$$

$$2.2837 = \log 192.2.$$

202. If 5 excavators sink a circular shaft 8 ft. in diameter and 125 fathoms deep in 100 dys. of 10 hrs. each, how many nights of 7 hrs. each will 4 excavators be in sinking a shaft 6 ft. in diameter and 75 fathoms deep; if the difficulty of working by night is one-seventh greater than by day, and the hardness of the ground in the smaller shaft is to that in the larger shaft as 7 is to 5?

203. Find the length of a pendulum that oscillates 80 times a minute.

$$80^{2}:60^{2}::39.138:x.$$

$$4^{2}:3^{2}::39.138:x.$$

$$16:9=39.138:x.$$

$$\frac{9\times 39.138}{16}=22.015 \text{ in. } Ans.$$

204. A man whose weight is 160 lbs., wishing to raise a rock, leans with his whole weight on a horizontal crowbar 5 ft. long, which is propped at the distance of 4 in. from the end in contact with the rock. Find what force he exerts on the rock, and what pressure the prop has to sustain, if the weight of the crowbar is not reckoned.

$$4:56 = 160: x.$$

$$\frac{40}{\cancel{4}}$$

$$\frac{56 \times \cancel{100}}{\cancel{4}} = 2240 \text{ lbs. (1) } Ans.$$

$$2240 + 160 = 2400 \text{ lbs. (2) } Ans.$$

205. A child weighing 56 lbs. is at one end of a plank 16 ft. long, and a child weighing 72 lbs. is at the other end. Find the distance of each child from the fulcrum when the plank is used for a see-saw.

$$56:72=7:9.$$

9 ft. and 7 ft. Ans.

206. In a pair of nut-crackers if the nut be placed at a distance of 1 in. from the hinge, and the hand presses at a distance of 8 in. from the hinge, find the pressure upon the nut for every ounce of pressure exerted by the hand.

$$1:8=1 \text{ oz.}: \text{ what ?}$$

8 oz. Ans.

207. A substance is weighed from both arms of a false balance, and its apparent weights are 9 lbs. and 4 lbs. Find the true weight.

$$4: x = x: 9.$$

$$x^2 = 36$$
.

x = 6 lbs. Ans.

208. A rope passes over a single pulley. How much force is required to raise 180 lbs. attached to one end of a rope if 1% of the force applied is required to overcome friction?

$$\frac{100}{9}$$
 of  $180 = 181.82$  lbs. Ans.

209. A cask of lamp-black weighing  $160^{kg}$  is attached to a rope wound on an axle  $19^{cm}$  in diameter; at one end of the axle is a wheel  $175^{cm}$  in diameter. With what force must a man pull down on a rope passing over the wheel to raise the cask if  $1\frac{s}{4}$ % of the pull is required to overcome friction?

$$175:19 = 160^{kg}: x.$$

$$\frac{32}{19 \times 160} = 17.3714^{kg}.$$

$$\frac{175}{35}$$

17.3714 + 0.9825 = 17.69kg. Ans.

210. The circumference of the circle described by the end of the power-arm of a screw is 24 in., and by one turn of the screw the head advances half an inch. If the power is 3 lbs., find the weight lifted.

$$\frac{1}{2}:24=3:x.$$

$$2 \times 3 \times 24 = 144$$
 lbs.

Less than 144 lbs. Ans.

211. In a screw used to raise a load of 10 t. the power is 50 lbs., acting by an arm 4 ft. long. Find the distance between two consecutive threads.

$$4 \text{ ft.} = 48 \text{ in.}$$
 $3.1416 \times 2 \times 48 = 301.5936.$ 
 $20,000: 50 = 301.6: x.$ 
 $400: 1 = 301.6: x.$ 
 $301.6 + 400 = 0.754.$ 
Less than 0.754 in. Ans.

212. What per cent of water is oxygen? what per cent hydrogen?

$$(2 \times 1) + 16 = 2 + 16 = 18.$$
  
 $^{2}_{18}$  of  $100 = 11\frac{1}{9}\%$  H. (1) Ans.  
 $100 - 11\frac{1}{9} = 88\frac{8}{9}\%$  O. (2) Ans.

213. What per cent of quicklime, CaO, is oxygen?

$$40 + 16 = 56$$
.  $\frac{16}{56}$  of  $100 = 284\%$ . Ans.

214. What per cent of water, H<sub>2</sub>O, in slacked lime, CaO<sub>2</sub>H<sub>2</sub>?

Ca = 40  
O<sub>2</sub> = 32  
H<sub>2</sub> = 2  
O = 
$$\frac{16}{18}$$
 $\frac{18}{18}$  of 100 = 24.32%. Ans.

215. What per cent of pure marble, CaCO<sub>3</sub>, is oxygen?

$$40 + 12 + 48 = 100$$
.  $\frac{48}{100}$  of  $100 = 48\%$ . Ans.

216. What per cent of gypsum (plaster of Paris),  $CaSO_4 + 2H_2O_5$ , is sulphur?

$$40 + 32 + 64 + 2(2 + 16) = 136 + 36 = 172.$$
  
 $\frac{3^2}{17^2}$  of  $100 = 18\frac{26}{4}\frac{6}{3}\%$ . Ans.

217. What per cent of washing-soda,  $Na_2CO_3 + 10 H_2O_3$ , is carbon?

$$46 + 12 + 48 + 10(2 + 16) = 106 + 180 = 286.$$
 $\frac{12}{286}$  of  $100 = 4\frac{28}{143}\%$ . Ans.

218. In 118 lbs. of Glauber salts,  $Na_2SO_4 + 10 H_2O$ , how many ounces of sulphur?

$$46 + 32 + 64 + 10(2 + 16) = 142 + 180 = 322$$
.  
 $\frac{32}{322}$  of  $118 \times 16 = 187.6$  oz. Ans.

219 How many ounces of soda,  $Na_2O + H_2O$ , in 7 lbs. of borax,  $Na_2B_4O_7 + 10 H_2O$ ?

$$46 + 16 + 18 = 80.$$
 $46 + 44 + 112 + 10(2 + 16) = 202 + 180 = 382.$ 
 $7 \text{ lbs.} = 112 \text{ oz.}$ 
 $\frac{80}{382} \times 112 = 23.46 \text{ oz.}$  Ans.

220. What per cent of pure alcohol, C<sub>2</sub>H<sub>6</sub>O, is carbon? What per cent of pure white marble, CaCO<sub>3</sub>, is carbon?

$$24 + 6 + 16 = 46$$
.  $40 + 12 + 48 = 100$ .  $\frac{12}{100}$  of  $100 = 52\frac{4}{100}$ %. (1) Ans.  $\frac{12}{100}$  of  $100 = 12\%$ . (2) Ans.

221. What per cent of pure acetic acid (the acid of vinegar) is carbon, the formula being  $C_2H_4O_2$ ?

$$24 + 4 + 32 = 60$$
.  $\frac{24}{60}$  of  $100 = 40\%$ . Ans.

222. How much acetic acid can be obtained from 12 lbs. of alcohol,  $C_2H_6O$ , if there is no waste?

$$C_2H_4O_2 = 60$$
 acid.  $24 + 6 + 16 = 46$  alcohol.

As alcohol contains 16 of O, and acid demands 86, 12 lbs. of alcohol will yield by combustion of H and C

$$\frac{16}{46} \times \frac{60}{32} \times 12 \text{ lbs.} = 7.82 \text{ lbs.}$$
 Ans.

223. How many grains of carbon in 1 oz. avoirdupois of oxalic acid,  $C_2H_2O_4 + 2H_2O$ ?

$$24 + 2 + 64 + 2(2 + 16) = 90 + 36 = 126.$$

$$\begin{array}{c}
1750 \\
3500 \\
\frac{24}{126} \text{ of } \frac{7000}{16} \text{ gr.} = \frac{1750}{21} = 83\frac{1}{8} \text{ grs. } Ans. \\
63 & 2 & 2
\end{array}$$

224. How many milligrams of carbon in 3s of tartaric acid,  $C_4H_6O_6$ ?

$$24 + 3 + 48 = 75.$$
  $3s = 3000^{mg}.$   $\frac{24}{75} \times \frac{3999}{1} = 960^{mg}.$  Ans.

225. How many kilograms of carbon in  $95^{kg}$  of white sugar,  $C_{12}H_{22}O_{11}$ ?

$$144 + 22 + 176 = 342.$$

$$\frac{8}{\cancel{144}} \times \frac{5}{\cancel{95}} = 40^{\text{kg}}. \text{ Ans.}$$

$$\cancel{19}$$

2 + 32 + 64 = 98.

226. The formula of camphor is C<sub>10</sub>H<sub>16</sub>O. How many grams of carbon in 14<sup>kg</sup> of camphor?

$$120 + 16 + 16 = 152.$$

$$\frac{15}{129} \times \frac{14000}{1} = \frac{210000}{19} = 11,052.6s. Ans.$$
19

227. In 20kg of oil of vitriol, H<sub>2</sub>SO<sub>4</sub>, how many grains of sulphur?

$$\frac{\frac{16}{32}}{\frac{32}{98}} \times \frac{20000}{1} = \frac{320000}{49} = 6530.65.$$
 Ans.

228. What per cent of oil of vitriol is water? what per cent sulphuric acid, SO<sub>3</sub>?

$$H_2SO_4 = 98.$$
  $\frac{18}{98}$  of  $100 = 18.37\%$  water.  $H_2O_4 = 18.$   $100 - 18.37 = 81.63\%$  sulphuric acid.

229. In 3.5s of black oxide of iron, FeO, how many milligrams of iron?

3.5s = 3500<sup>mg</sup>. 56 + 16 = 72.  

$$\frac{7}{56}$$
 of  $\frac{3500}{1}$  =  $\frac{24500}{9}$  =  $2722\frac{2}{3}$  ms. Ans.

230. Red iron-rust consists of 70% iron and 30% oxygen. Find its formula.

Fe = 56 and 0 = 16. 16:56=2:7. 30:70=3:7. First seek multiples of 16 and 56 in the proportion of 30 to 70;

that is, of 3 to 7.  $\therefore$  Fe: 0 = 2:3.

Formula - Fe<sub>2</sub>O<sub>2</sub>. Ans.

231. The choking vapor of burning sulphur is equal parts sulphur and oxygen. What is its chemical formula?

S = 32. O = 16.  $O_2 = 32$ .  $SO_2$ . Ans.

232. If the composition of copperas is sulphuric acid 28.9%, oxide of iron 25.7%, water 45.4%, what is its formula?

Water being 18, oxide of iron being 72, and sulphuric acid 80, first seek multiples of 72 and 80, in the proportion of 25.7 to 28.9; that is, of 0.8892 to 1. But it is evident that 72 and 80 are in almost exactly that proportion. This gives FeSO<sub>4</sub> + water; and the remaining question is to find a multiple of 18 which is to 152 as 45.4 is to 54.6; that is, which is 0.8315 of 152, or 126.4. But  $7 \times 18 = 126$ ; and the addition of 7 parts of water gives as the complete formula, FeSO<sub>4</sub> + 7 H<sub>2</sub>O. Ans.

233. Spirits of turpentine is 11.76% hydrogen and 88.24% carbon. Give a chemical formula which will express that fact. Compare now with camphor,  $C_{10}H_{16}O$ . What per cent of oxygen combined with spirits of turpentine are required to make camphor?

Hydrogen being 1 and carbon 12, and 88.24 being almost exactly 7.5 times 11.76, we seek the smallest multiple of 12 that is 7.5 times a whole number. This is evidently 5 times 12, equal to 7.5 times 8. Therefore the formula is  $C_5H_8$ . (1) Ans.

Double it and add O, and we have  $C_{10}H_{16}O$ , the formula of camphor; containing 16 + 136 = 11.76% of oxygen added to spirits of turpentine. (2) Ans.

234. Out of the ten digits, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, how many numbers each consisting of two figures can be formed?

The numbers actually formed are those from 10 to 99; 90 in all. To show how many can be formed, consider that each digit may be followed by itself or by any of the other 9, giving 100 sequences of 2 figures; but 10 of these begin with 0, and are to be rejected, leaving 90. Ans.

235. How many odd numbers consisting of two figures can be formed with the ten digits?

As 10 is even and 99 odd, one-half the 90, viz. 45, are odd. Ans.

236. With the digits 0, 1, 2, 3, 4, 5, how many numbers between 1000 and 4000 can be formed?

The digit in the thousands' place must be 1, 2, or 3. Each of these may be followed in the hundreds' place by each of the 6 given digits, making 18 different hundreds. Each of these may be followed in the tens' place by each of the 6, giving 108 different tens; each of which may have 6 digits, giving 648 numbers if we include the 1000. Ans.

237. How many dominoes are there in a set numbered from double-blank to double-nine?

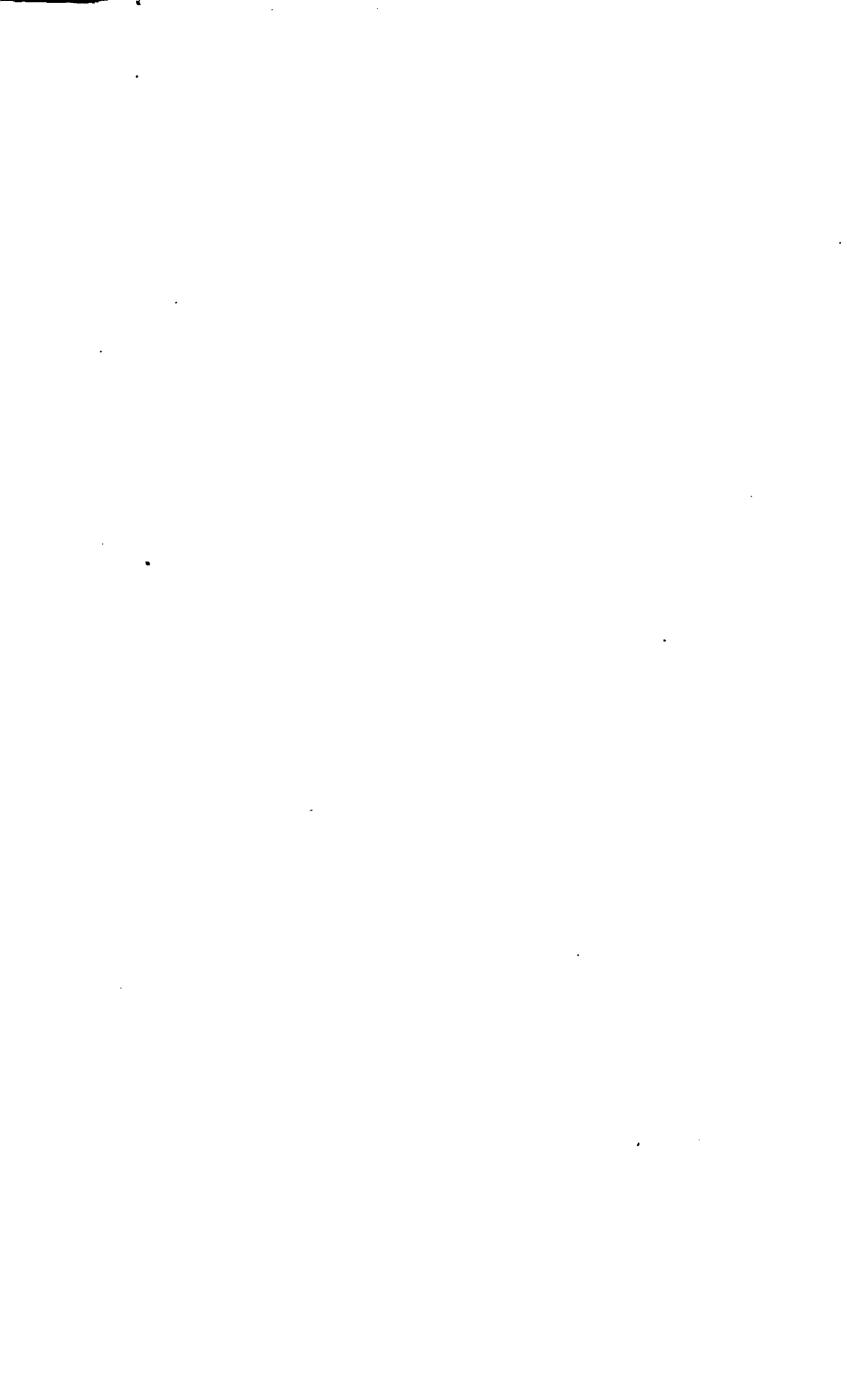
By a domino is meant two numbers, side by side. Double-blank is 00. The next pieces introducing 1 are 01, 11; those introducing 2 are 02, 12, 22. Every number introduced requires new pieces exceeding by one the number introduced. Thus, as we have seen that to go to double-2 requires 6, to go to double-3 will require 6 + 4 = 10 pieces; double-4, 10 + 5 = 15 pieces. The ordinary set is 15 + 6 + 7 = 28 pieces; and for double-9's we should require 28 + 8 + 9 + 10 = 55 pieces.

Ans.

238. How many different amounts can be weighed with 1-lb., 2-lb., 4-lb., 8-lb., and 16-lb. weights?

With a single piece, 5 amounts; with 2 pieces, 4+3+2+1=10 amounts; with 3 pieces, 10 amounts; with 4 pieces, 5 amounts; with all 5 at once, 1 amount; with the 5 in their various combinations, therefore, 5+10+10+5+1=31 amounts. Ans.

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